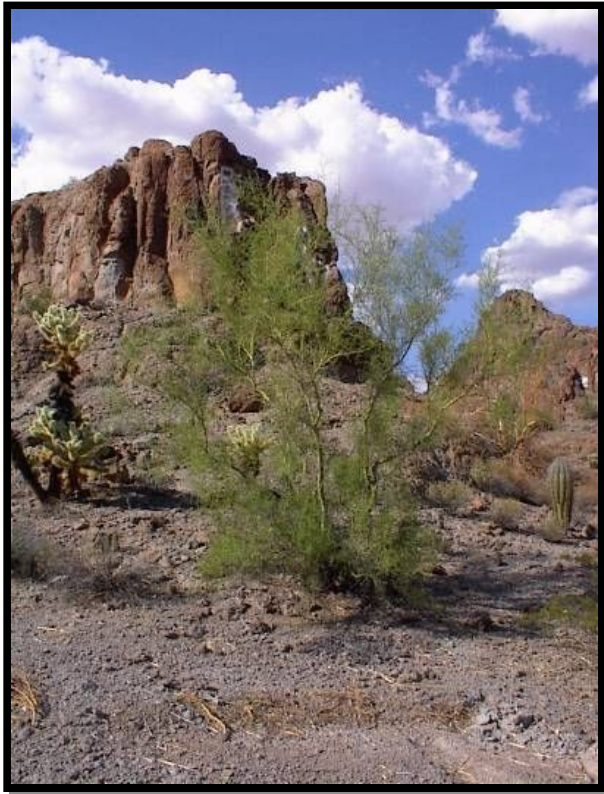




Facilitation and competition in the desert: saguaro cactus and Palo Verde trees

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- **Lucas Paoliello de Medeiros** (*University of São Paulo, Ecology Department, Brazil*)
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- **Nerea Abrego** (*University of the Basque Country, Dept. Plant Biology and Ecology, Spain*)
- **Susana Contreras** (*Universidad de los Andes, Dept. Biomedical Engineering, Colombia*)

INTRODUCTION OF TARGET SPECIES



Palo Verde tree
Cercidium floridum



Saguaro cactus
Carnegiea gigantea

INTRODUCTION OF TARGET SPECIES



Palo Verde tree
Cercidium floridum

Saguaro cactus
Carnegiea gigantea

DESCRIPTION OF THE ENVIRONMENT

Desert

- Water limitations
- Sun exposure
- Freezing
- Predation
- Wind



INTRODUCTION OF THEIR INTERACTIONS

- Nurse plants
protection against such adverse conditions



FACILITATION

- Water stress and nutrients



COMPETITION

POPULATION DYNAMICS BASED ON LITERATURE










Saguaros growing under
Palo Verde tree



Saguaros that have killed
a Palo Verde tree

THE MODEL

- Species-1  needs species-2  to survive in a part of its life-cycle
- Young species-1  consumes the resources that species-2  does not use
- Old species-1  competes with species-2  and kills it
- Species-1  behaves as a parasite!

But not any parasite...

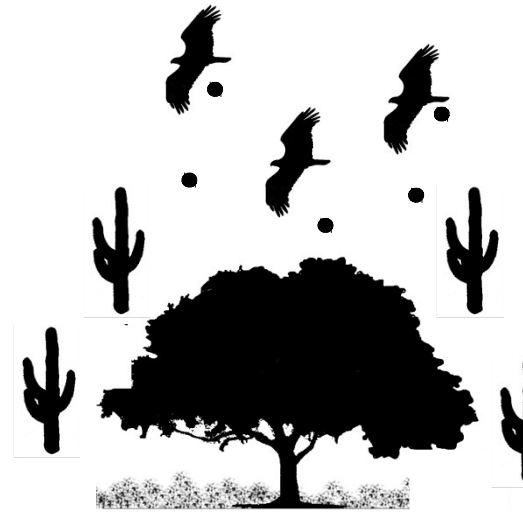
As the killer cacti can survive for very long!!

But not just any parasite...

As the killer cacti can survive for very long!!

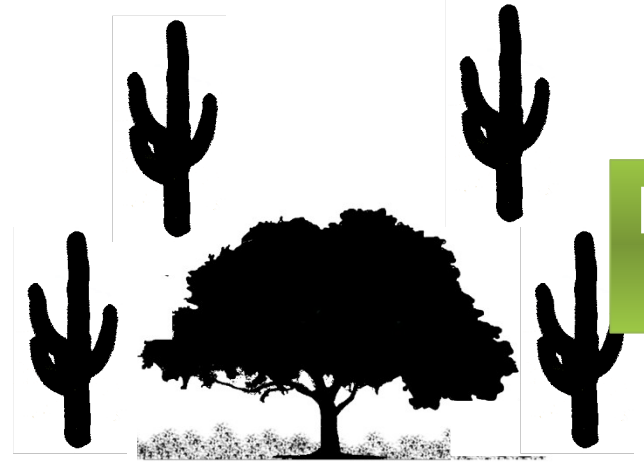
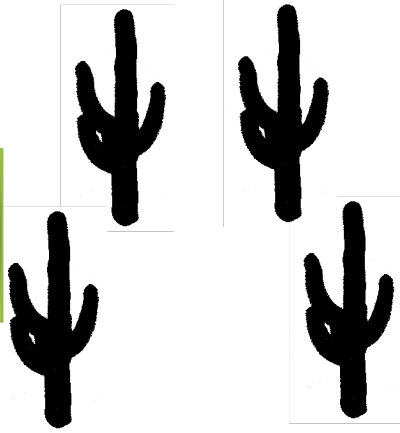


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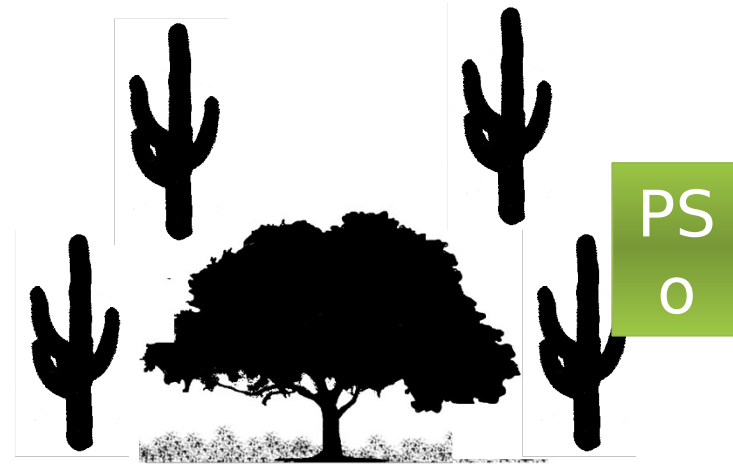
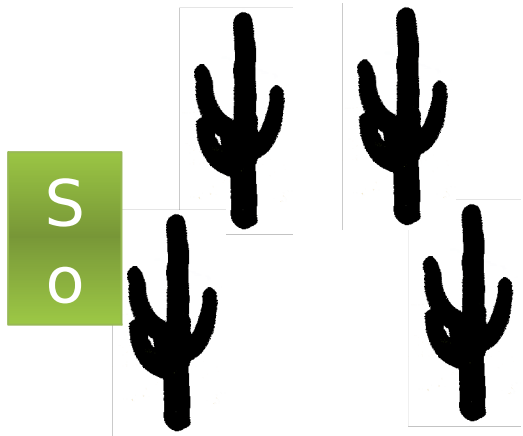
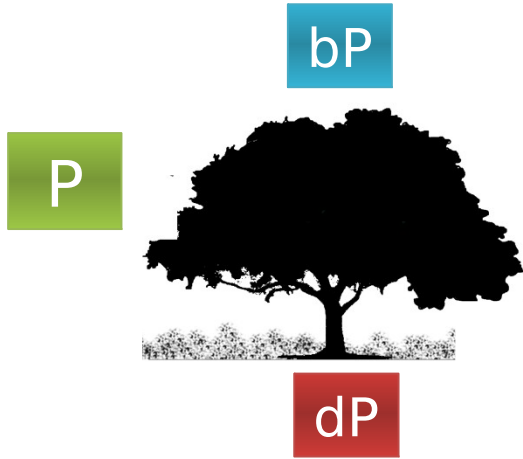


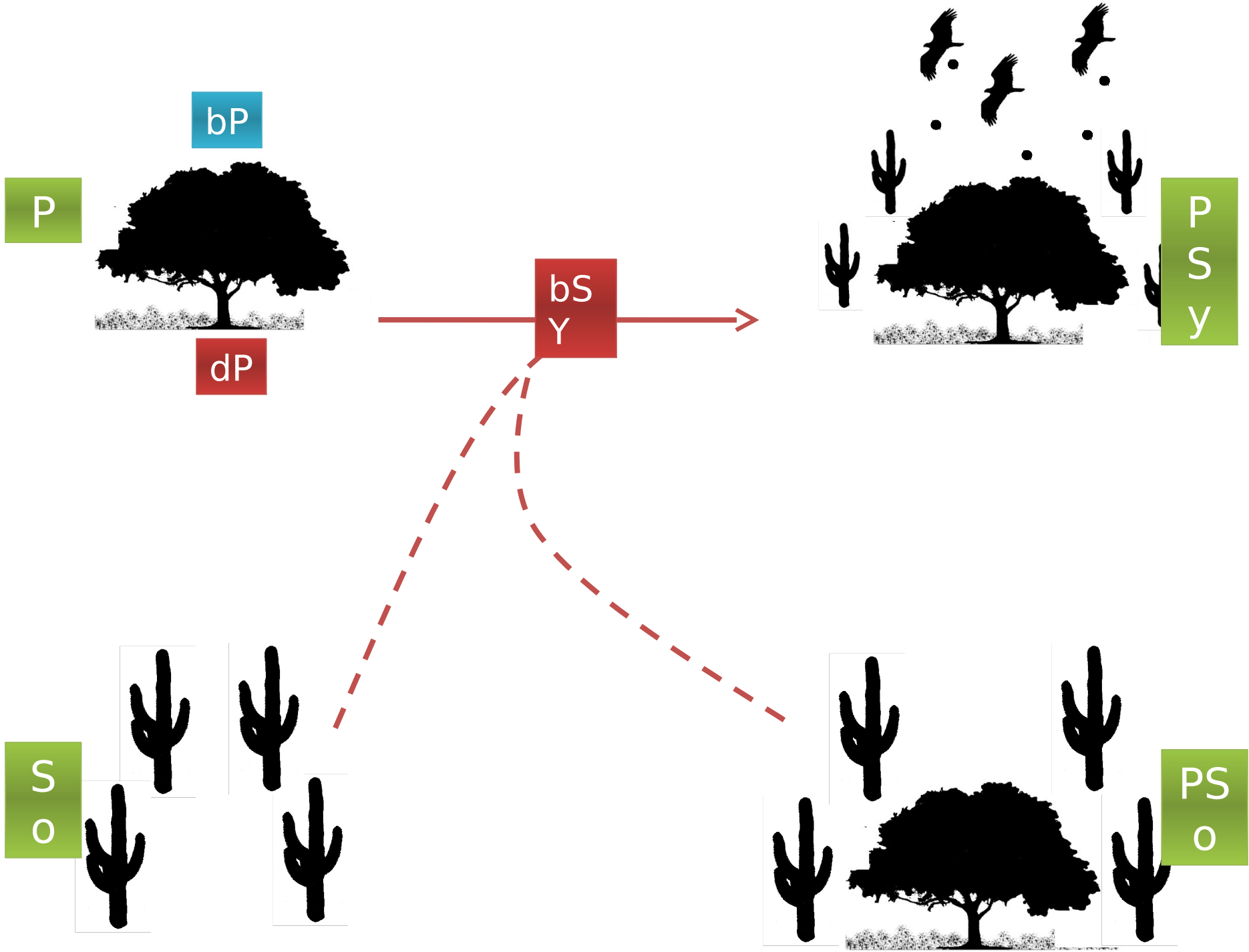
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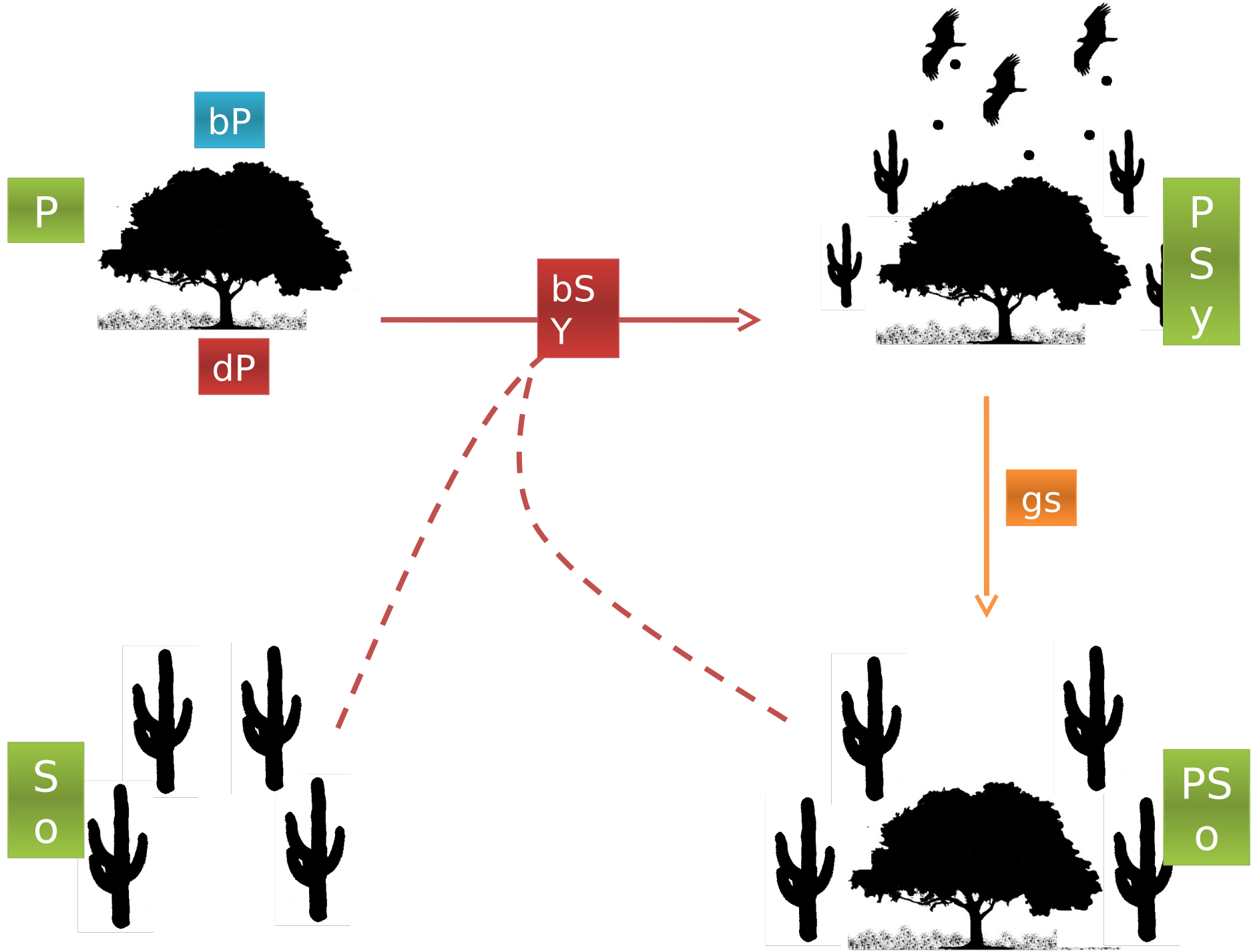
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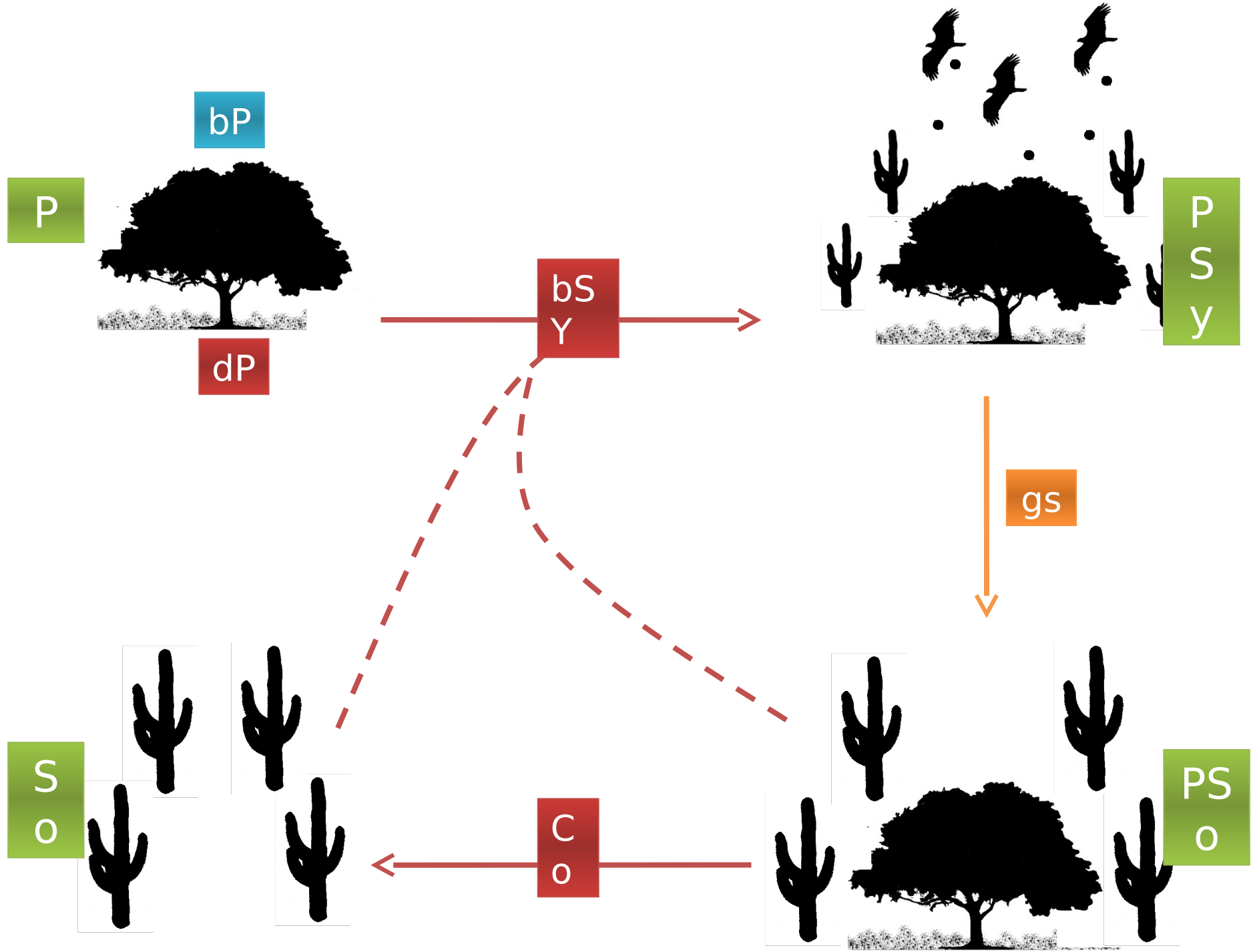


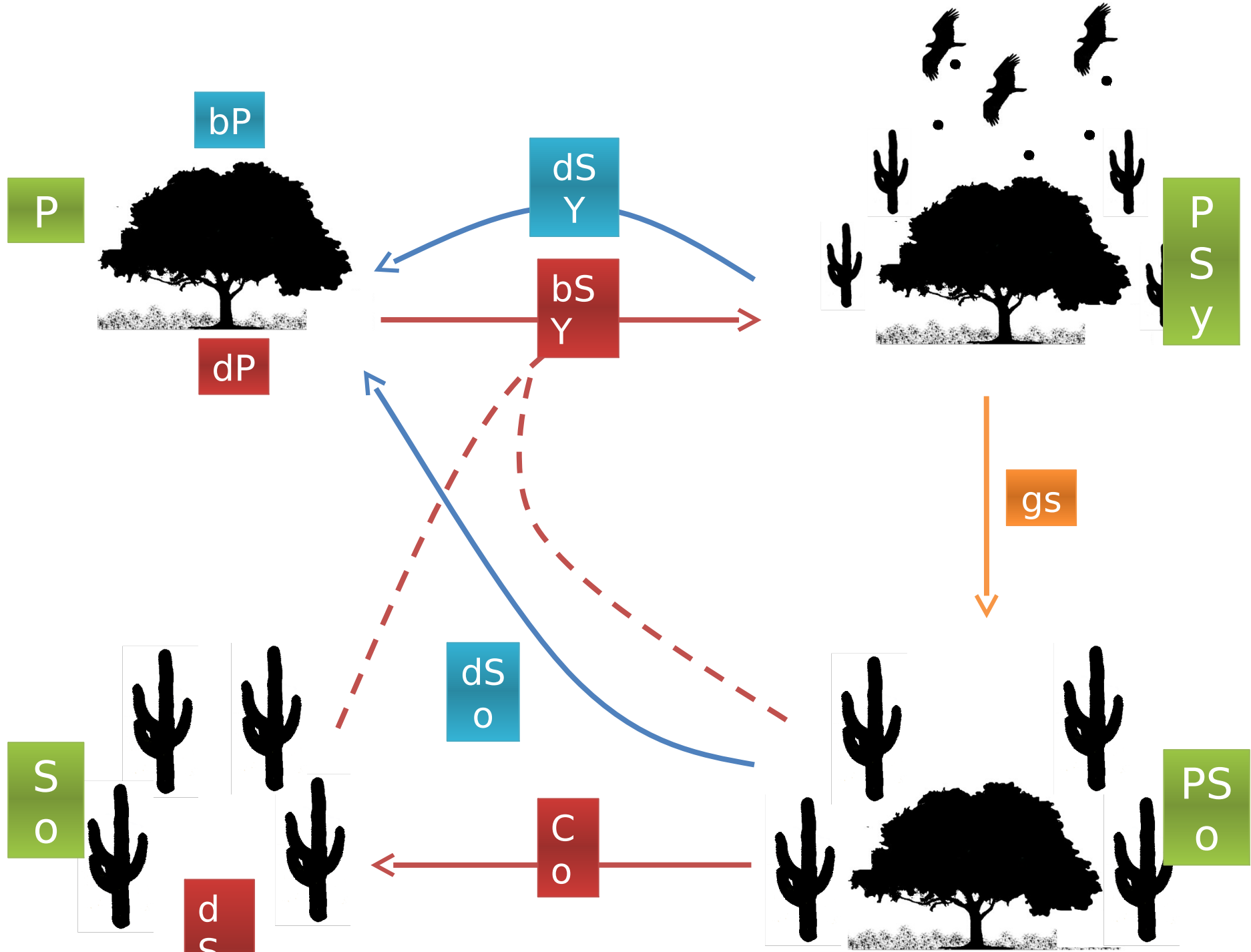
PS
O











“Alien Cactus” Mode



$$\frac{dP}{dt} = b_p P_T - d_p \left(1 + \frac{P_T}{K_P}\right) P - b_{S_y} (P_{S_o} + S_o) P + d_{S_y} P_{S_y} + d_{S_o} P_{S_o}$$

P_T : total number of Palo Verde trees ($P_T = P + P_{S_y} + P_{S_o}$)

“Alien Cactus” Mode



$$\frac{dP_{S_y}}{dt} = b_{S_y}(P_{S_o} + S_o)P - g_S P_{S_y} - d_{S_y} P_{S_y} - d_p P_{S_y}$$

“*Alien Cactus*” Mode



$$\frac{dP_{S_o}}{dt} = g_S P_{S_y} - d_{S_o} P_{S_o} - d_p \left(1 + \frac{P_T}{K_P} + C_{S_o} \right) P_{S_o}$$

“Alien Cactus” Mode



$$\frac{S_o}{dt} = d_p \left(1 + \frac{P_T}{K_P} + C_{S_o} \right) P_{S_o} - d_{S_o} S_o$$

“Alien Cactus” Mode



$$\frac{dP}{dt} = b_p P_T - d_p \left(1 + \frac{P_T}{K_P}\right) P - b_{S_y} (P_{S_o} + S_o) P + d_{S_y} P_{S_y} + d_{S_o} P_{S_o}$$

$$\frac{dP_{S_y}}{dt} = b_{S_y} (P_{S_o} + S_o) P - g_S P_{S_y} - d_{S_y} P_{S_y} - d_p P_{S_y}$$

$$\frac{dP_{S_o}}{dt} = g_S P_{S_y} - d_{S_o} P_{S_o} - d_p \left(1 + \frac{P_T}{K_P} + C_{S_o}\right) P_{S_o}$$

$$\frac{dS_o}{dt} = d_p \left(1 + \frac{P_T}{K_P} + C_{S_o}\right) P_{S_o} - d_{S_o} S_o$$

Possible Outcomes

- **Endemy/Coexistence: Both species survives**
- **Recovery: Cacti extinction**
- **Extinction: Both species extinct**

Exploring the model

- Differential equations solved by numerical integration.

Exploring the model

- Differential equations solved by numerical integration.
- Initial conditions:
 - P: high population
 - Psy: low population
 - Pso: absent
 - So: absent

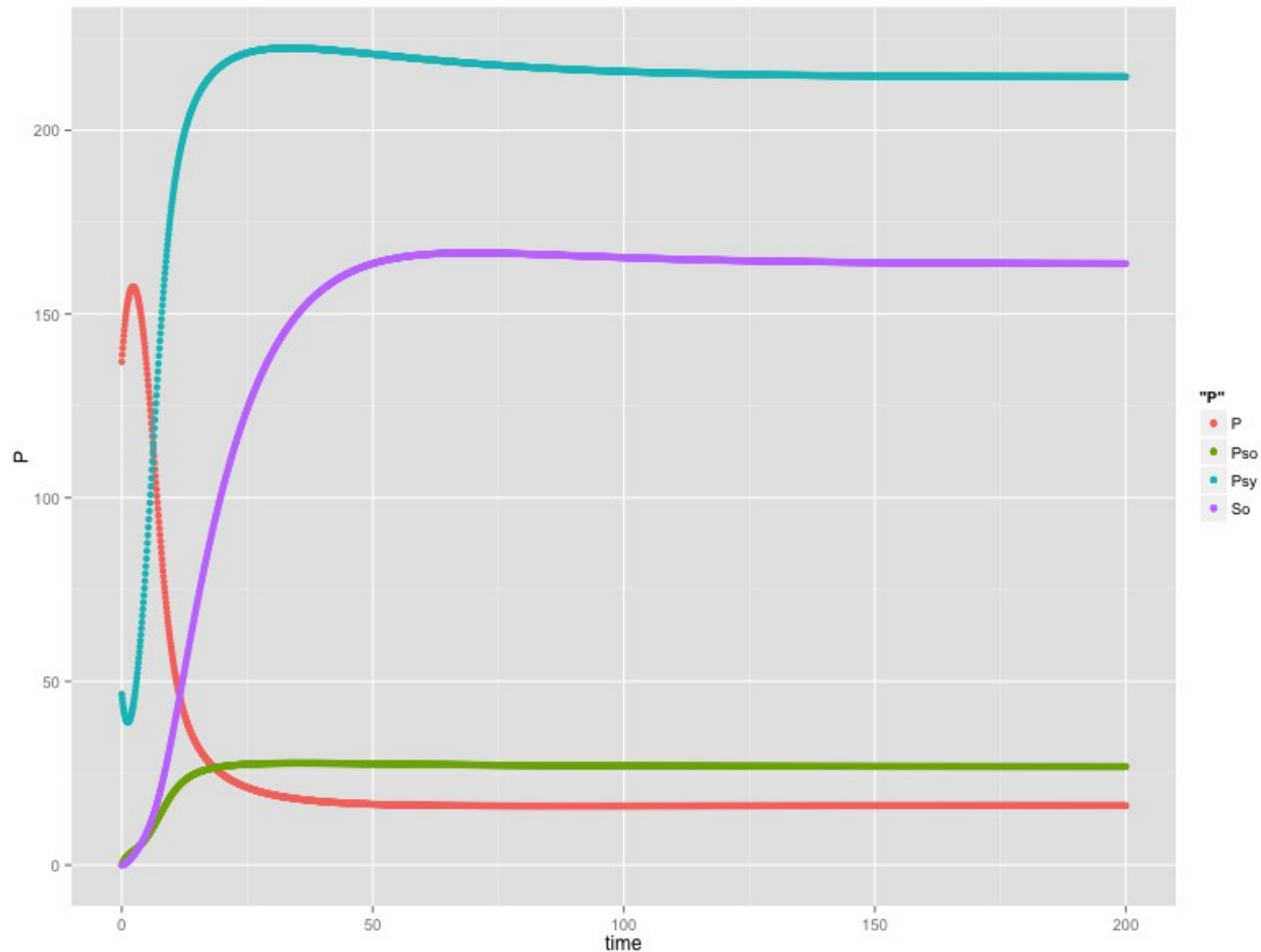
Exploring the model

- Differential equations solved by numerical integration.
- Initial conditions:
 - P: high population
 - Psy: low population
 - Pso: absent
 - So: absent
- Parameter space explored with the Latin Hypercube

Model Outcomes

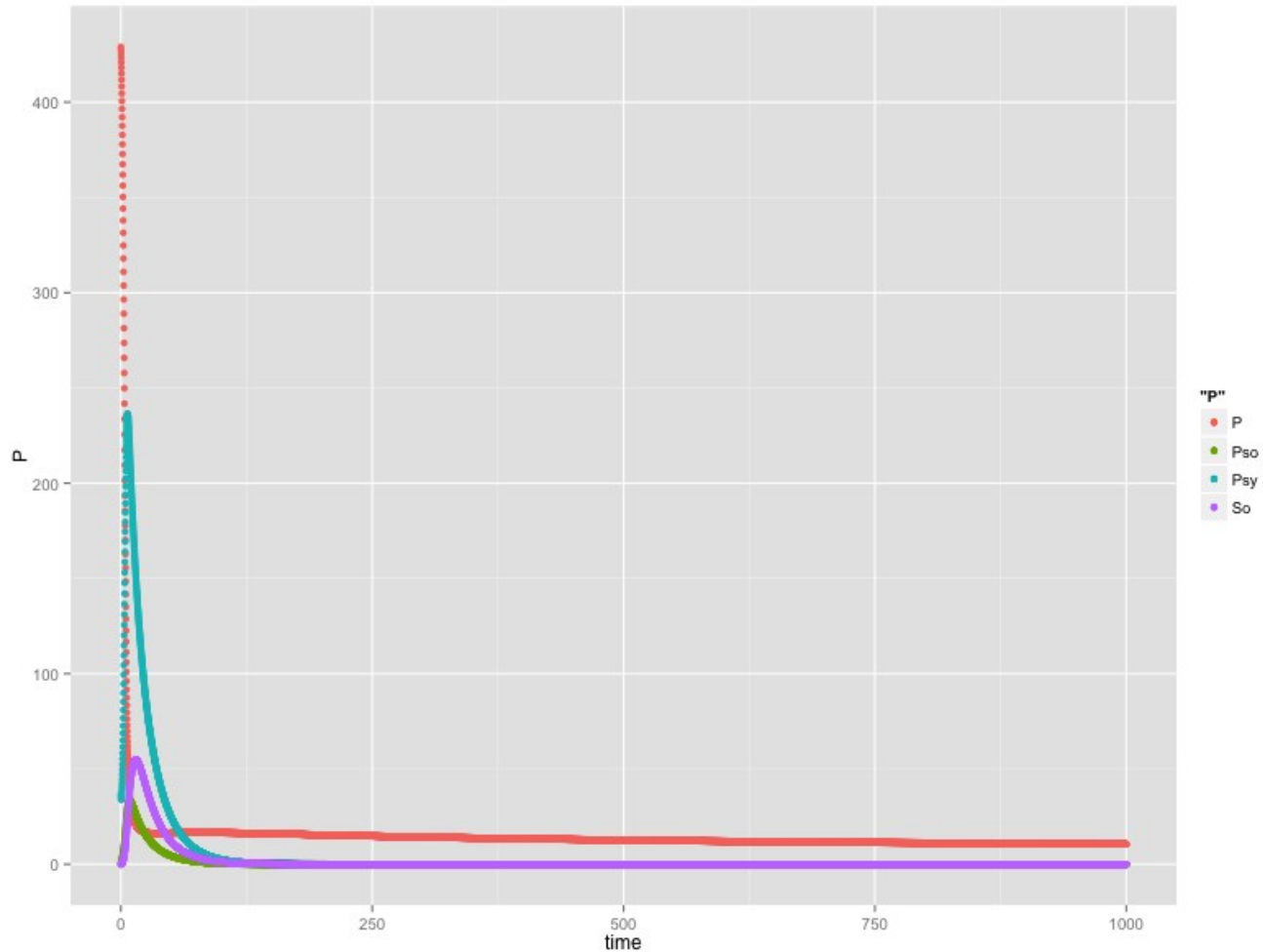
Endemism/Coexistence: Both species

SU



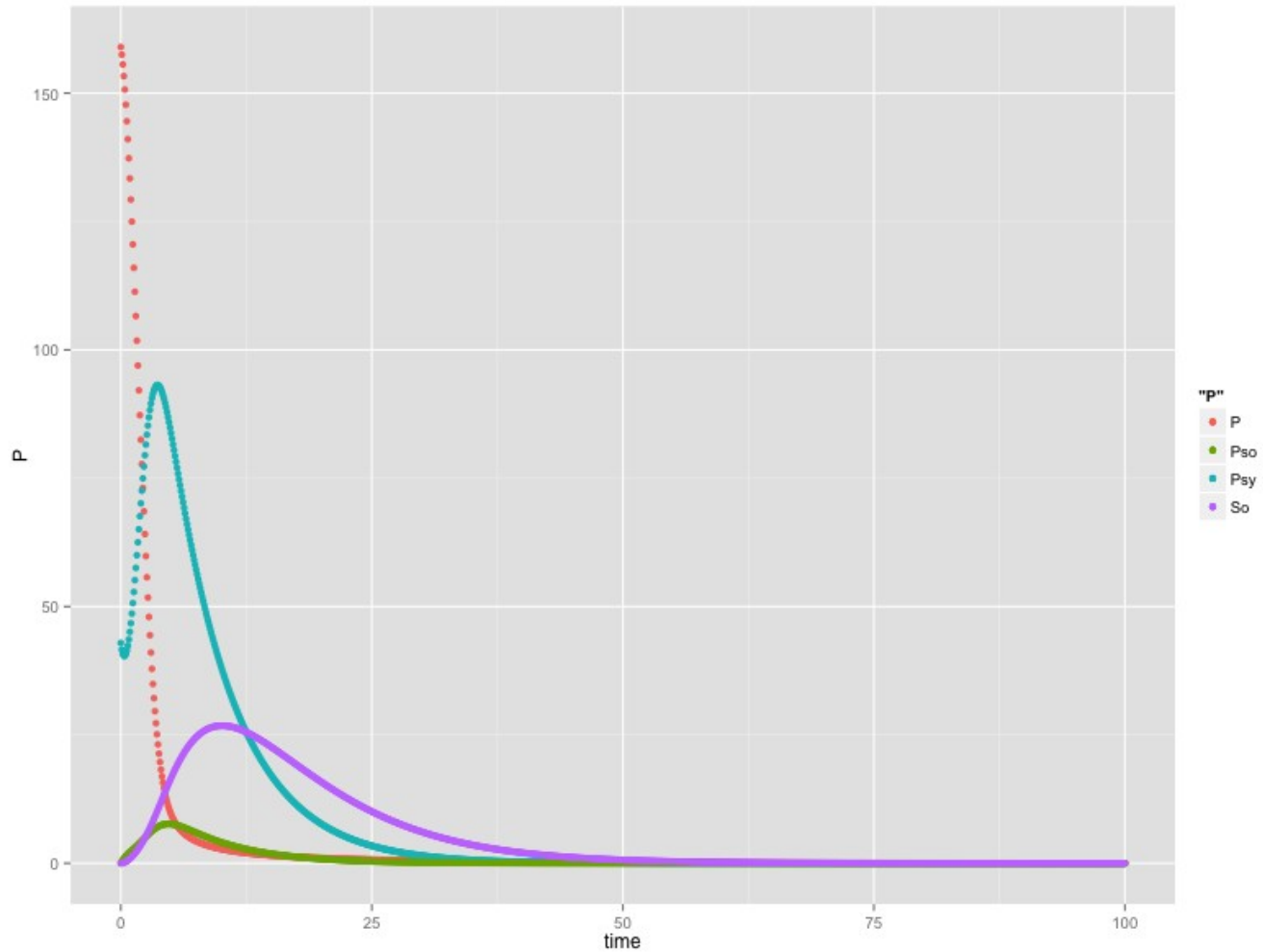
Model Outcomes

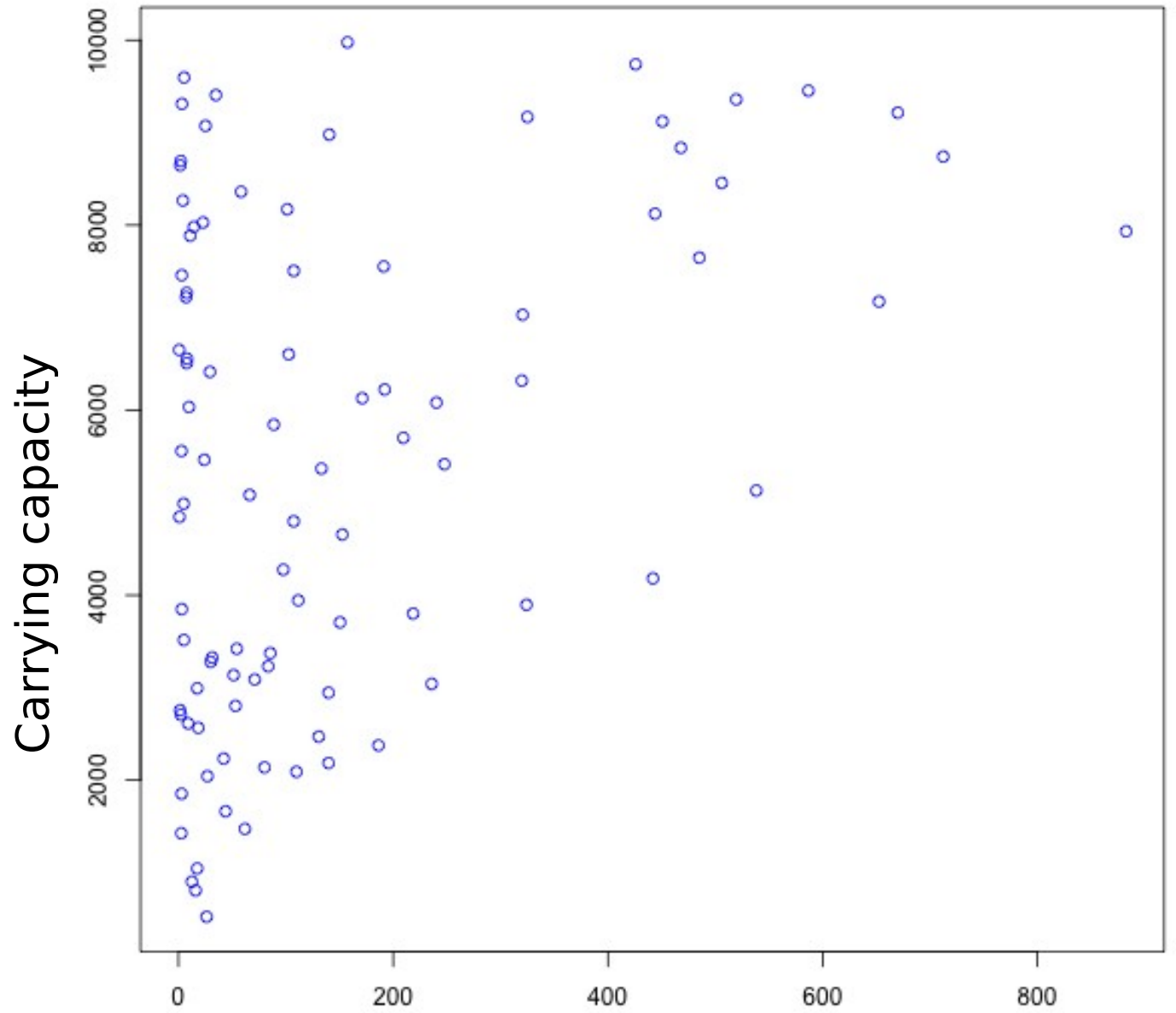
Recovery: Cacti



Model Outcomes

Extinction: Both



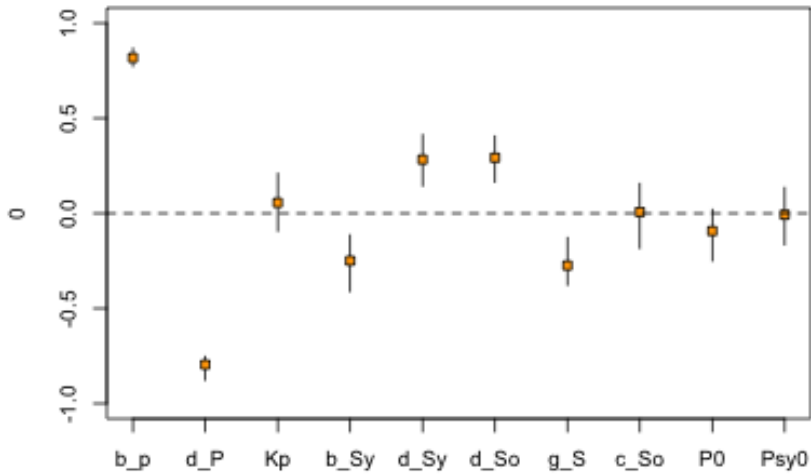


All the Palo Verde

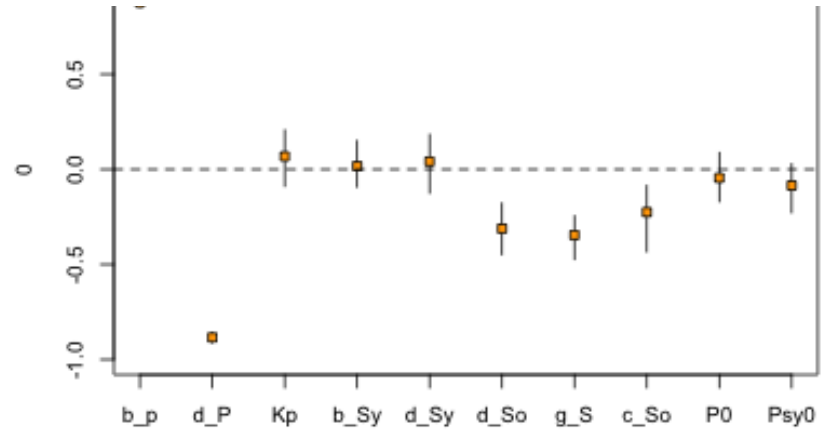
loti

Partial Rank Correlation Coefficients

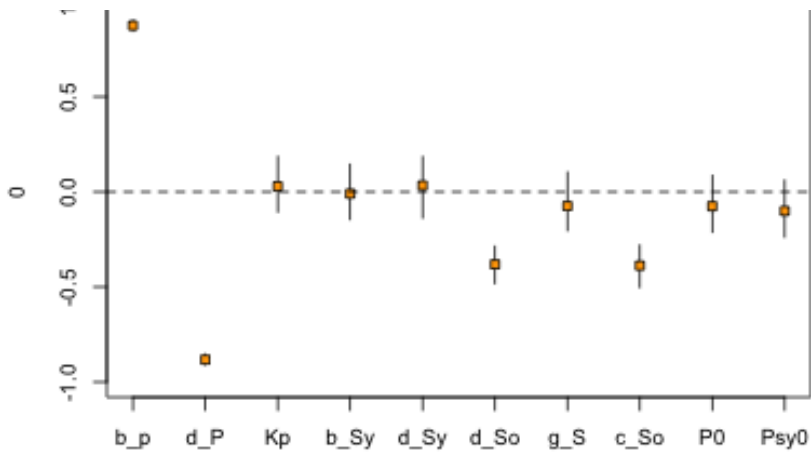
All the Palo Verde populations



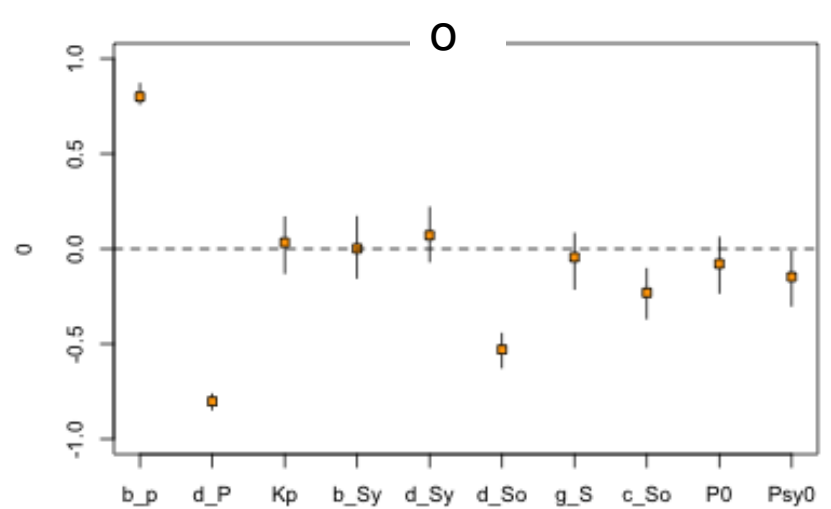
Palo Verde infected by young Saguars



Palo Verde infected by adult Saguars

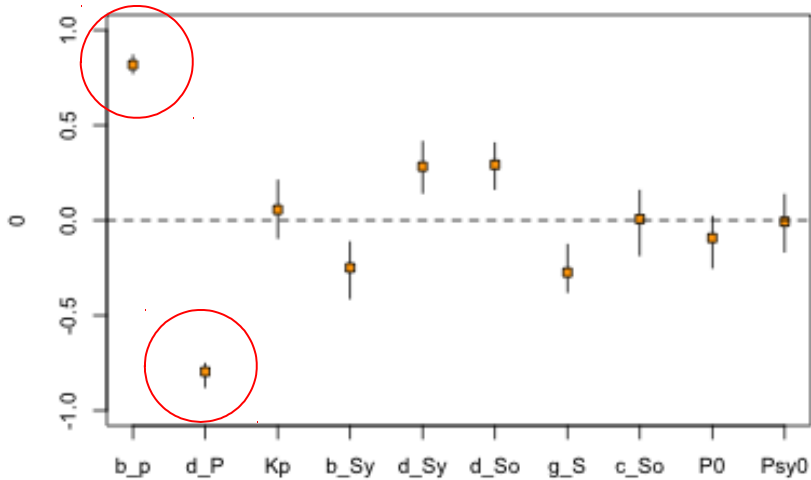


Adult Saguars

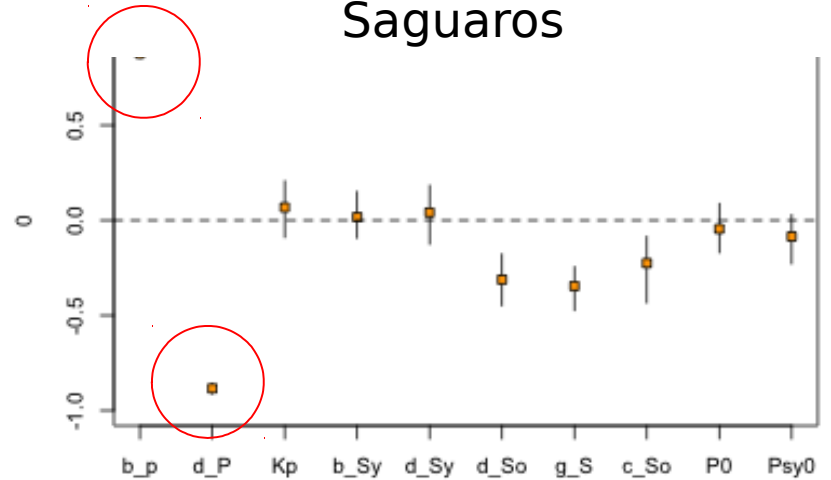


Partial Rank Correlation Coefficients

All the Palo Verde populations



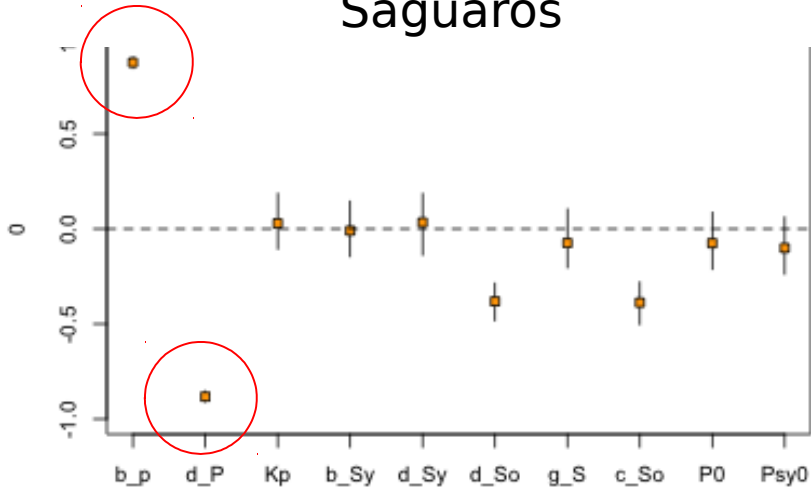
Palo Verde infected by young Saguars



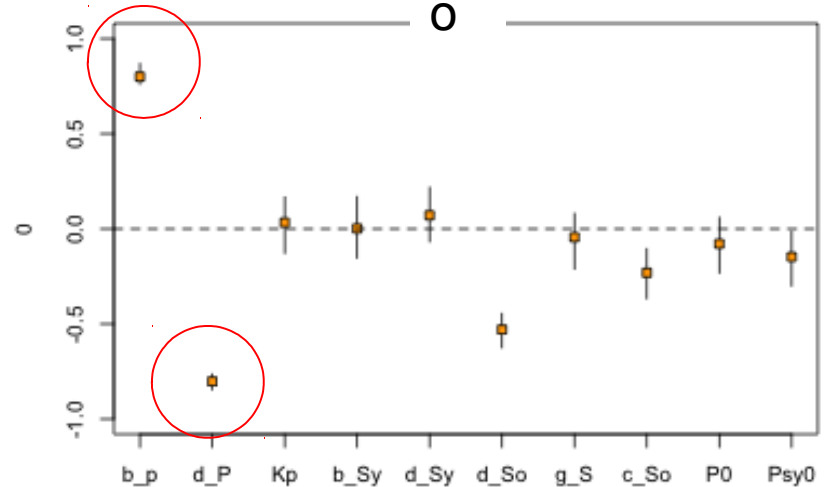
Large correlation coefficients for

b_p and d_p

Palo Verde infected by adult Saguars

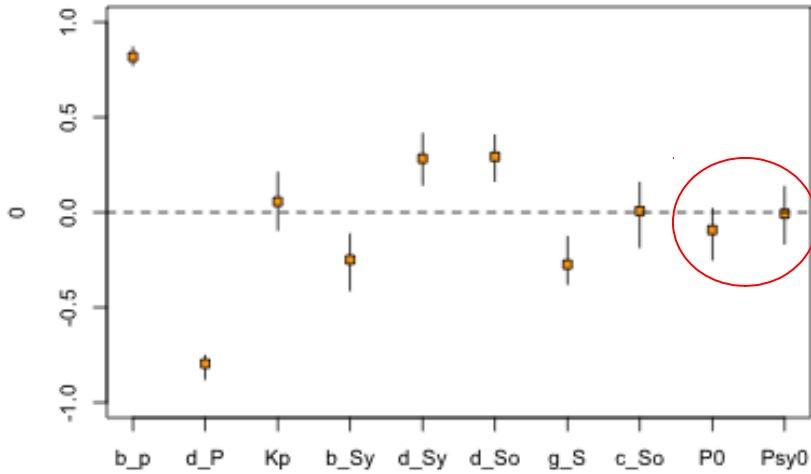


Adult Saguars

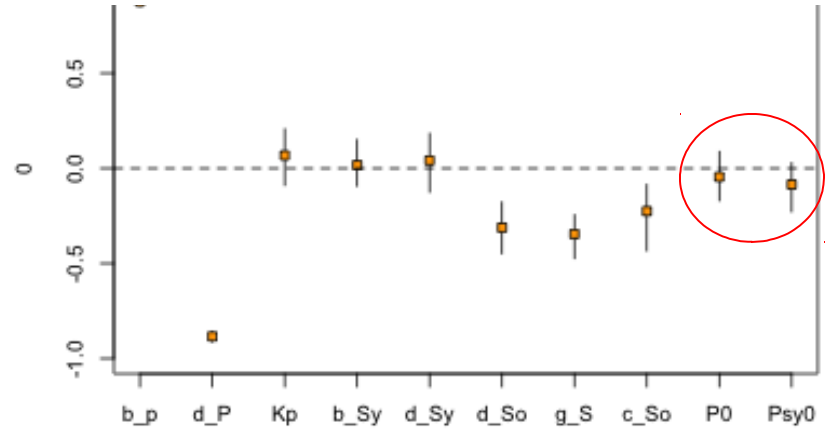


Partial Rank Correlation Coefficients

All the Palo Verde populations

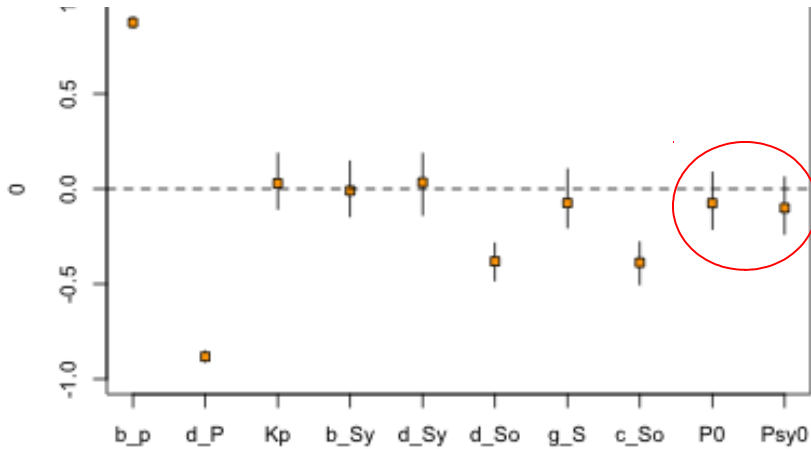


Palo Verde infected by young Saguars

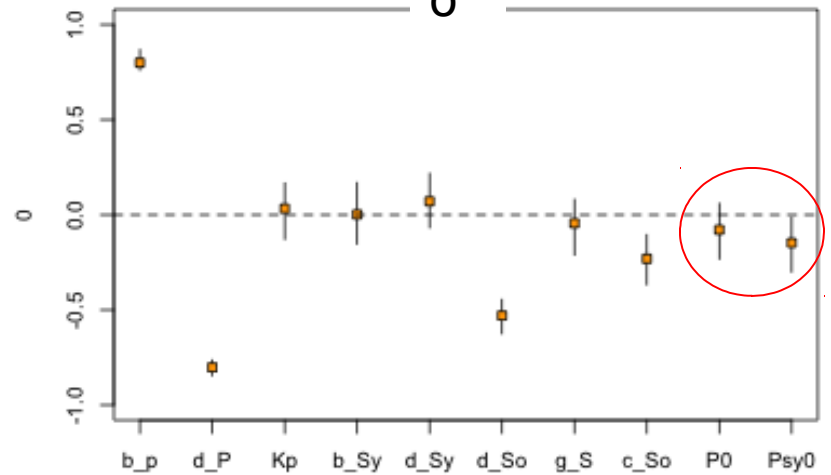


No effect of the initial conditions

Palo Verde infected by adult Saguars

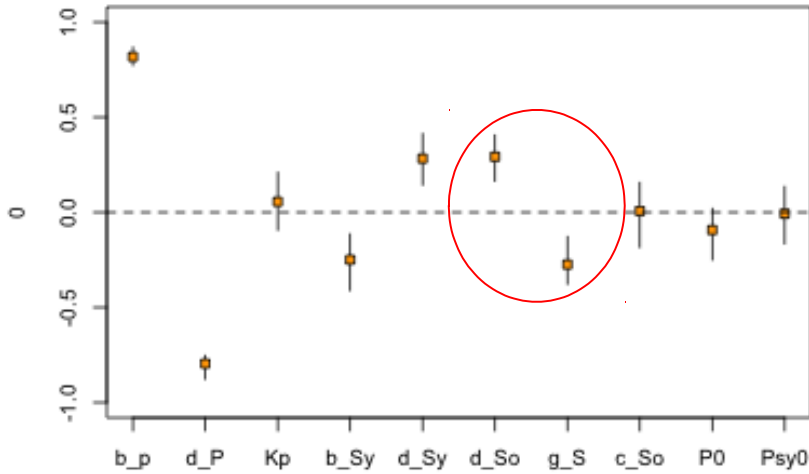


Adult Saguars

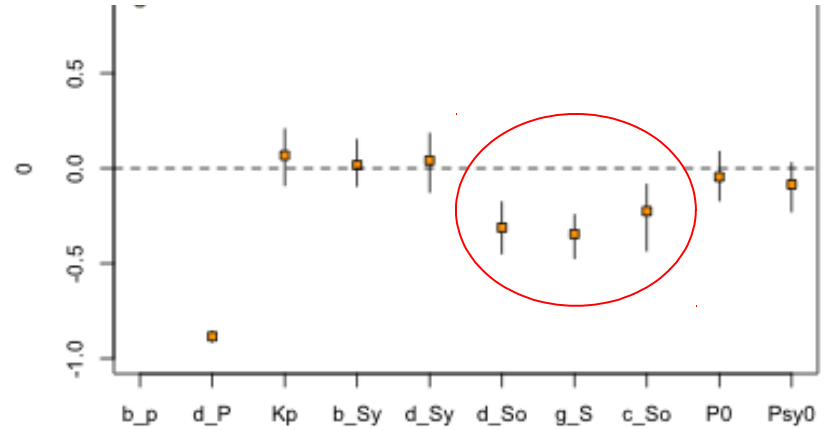


Partial Rank Correlation Coefficients

All the Palo Verde populations

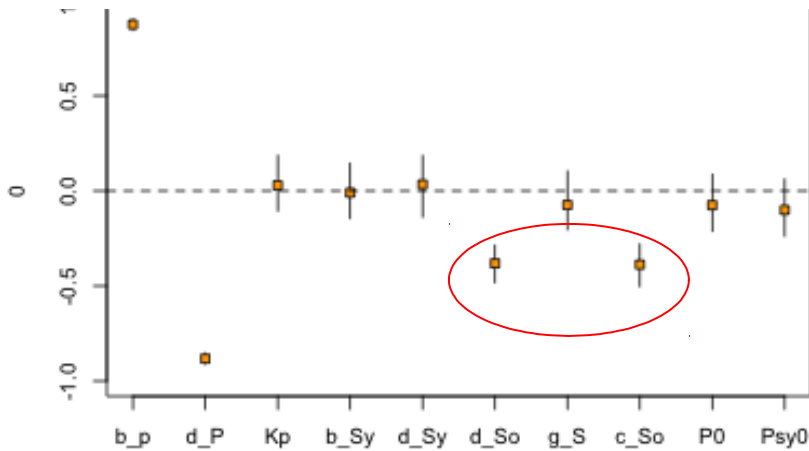


Palo Verde infected by young Saguars

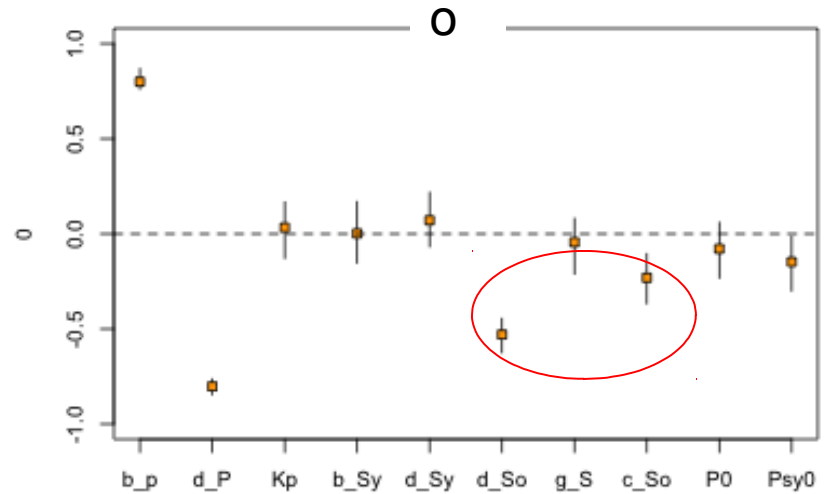


Significant effects of dSo,

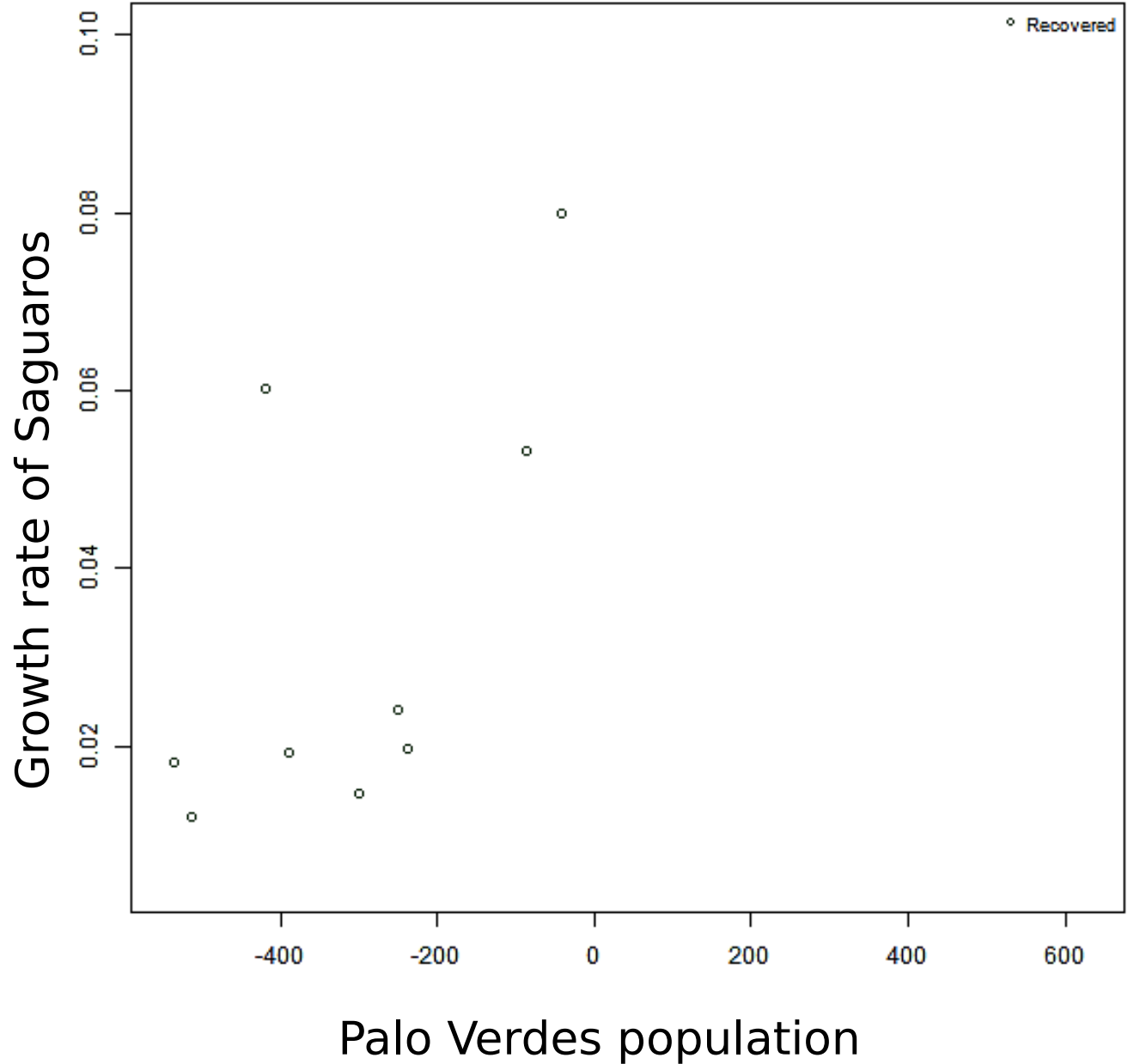
gS and cSo
Palo Verde infected by adult Saguars



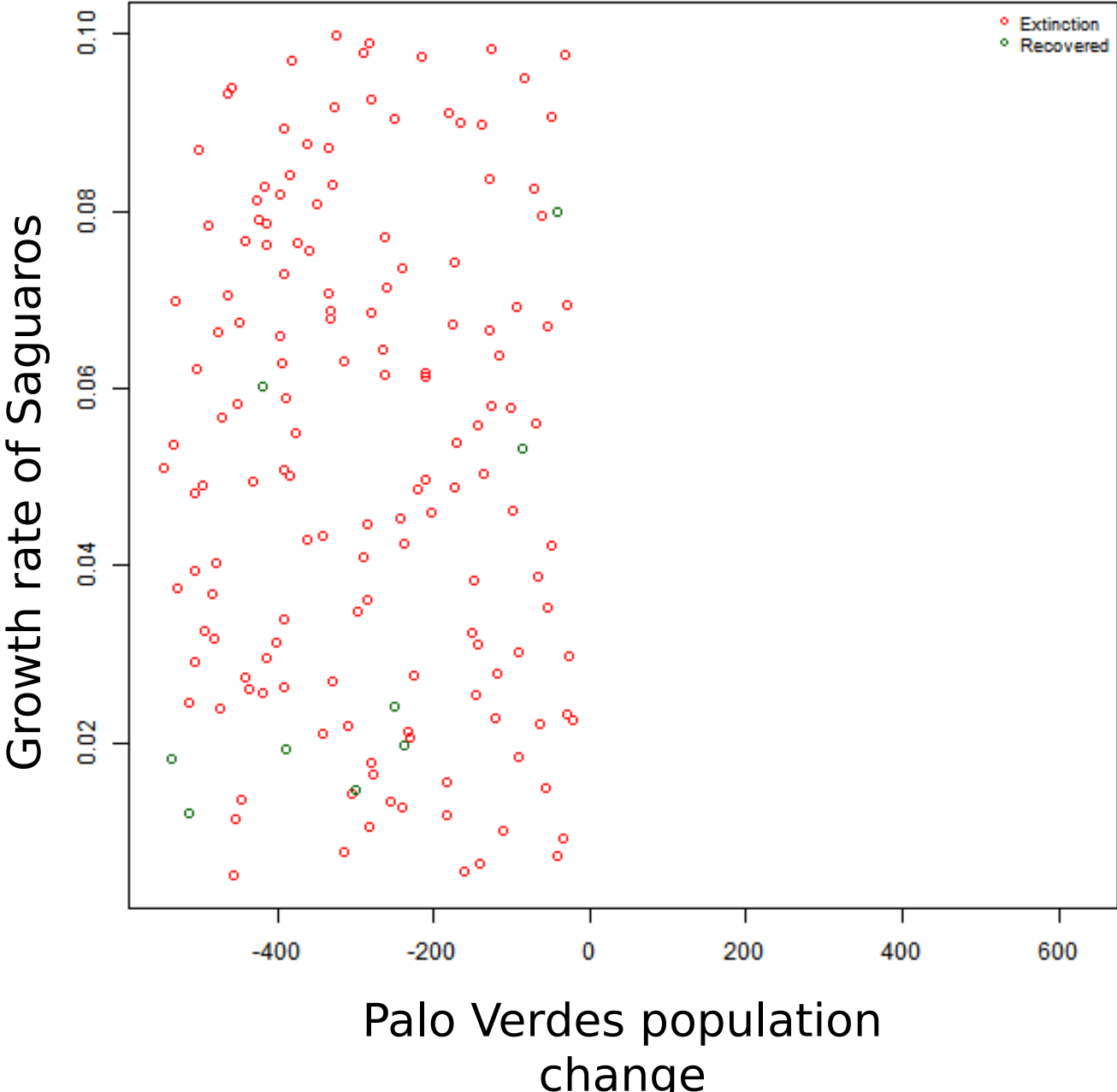
Adult Saguars



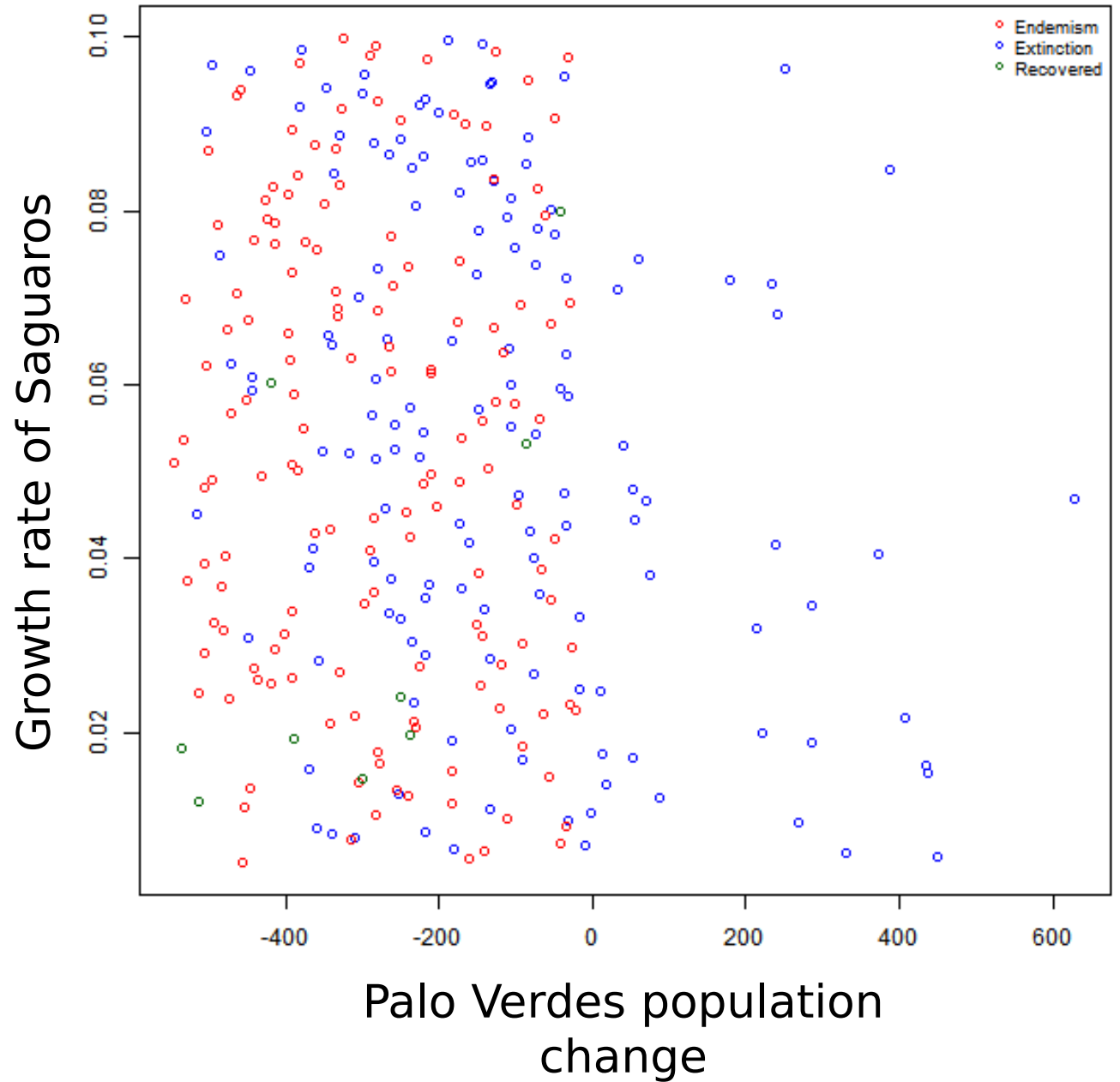
Change in Initial Population of Palo Verdes



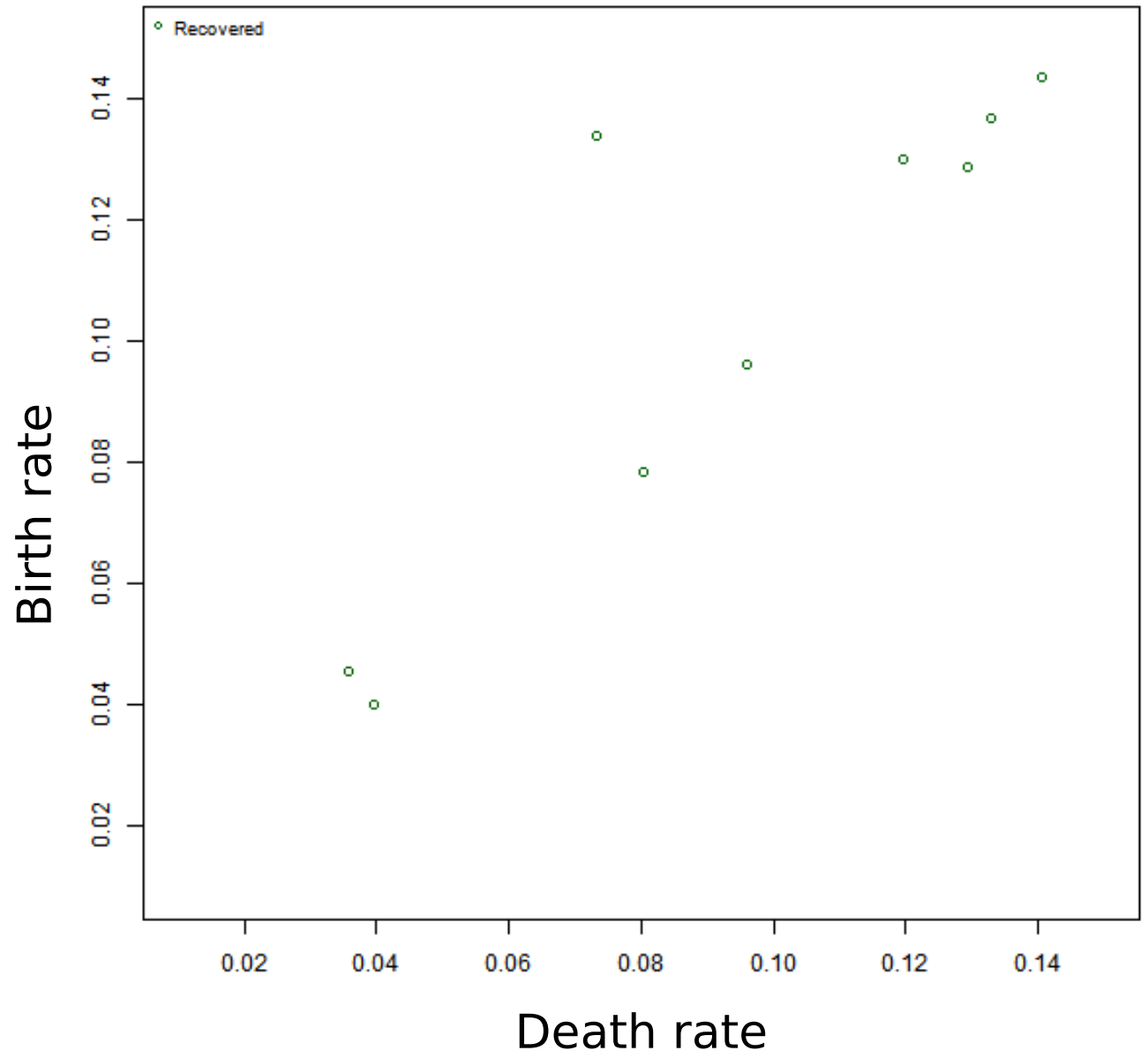
Change in Initial Population of Palo Verdes



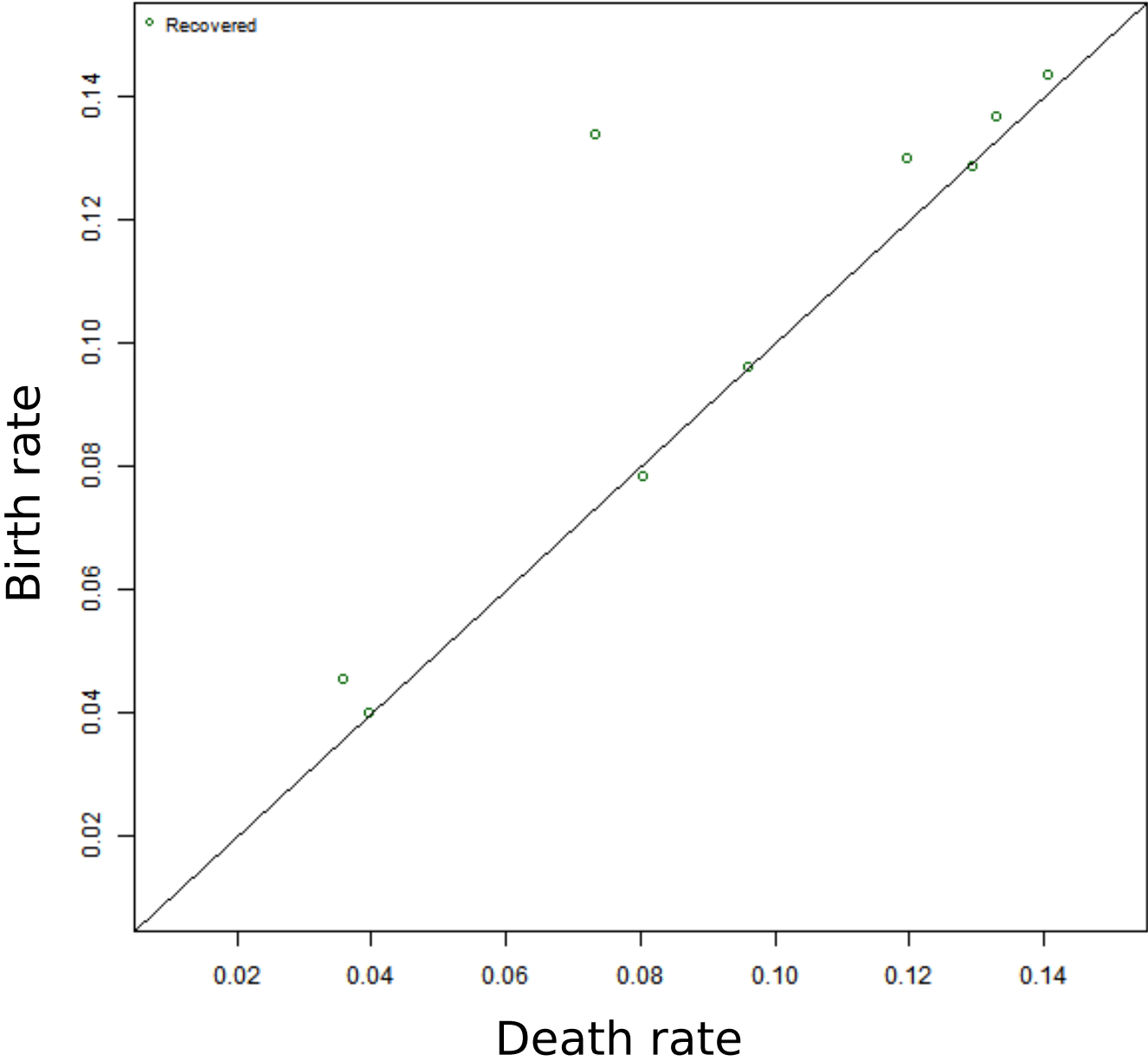
Change in Initial Population of Palo Verdes



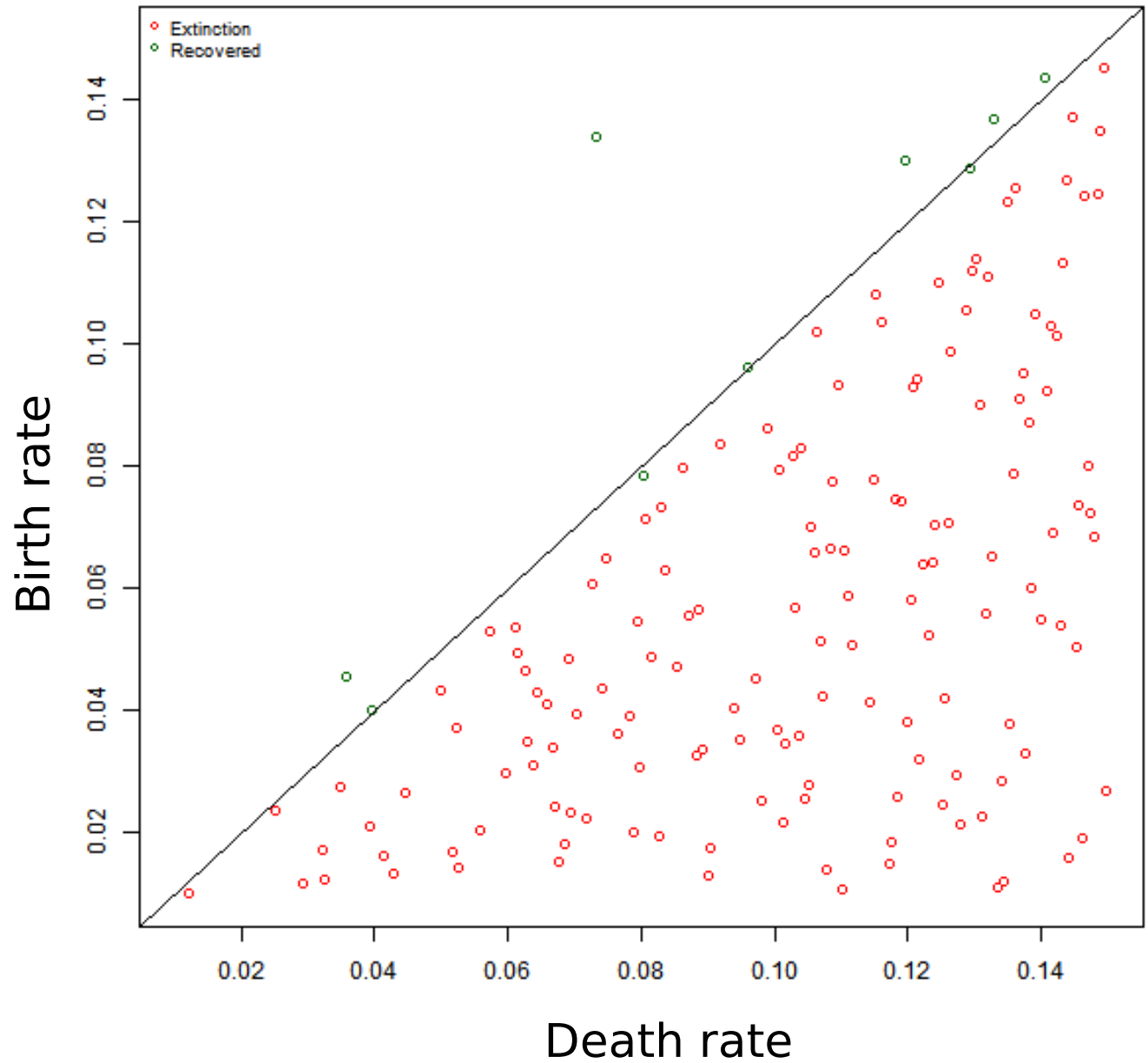
Palo Verde Birth Rate vs. Mortality



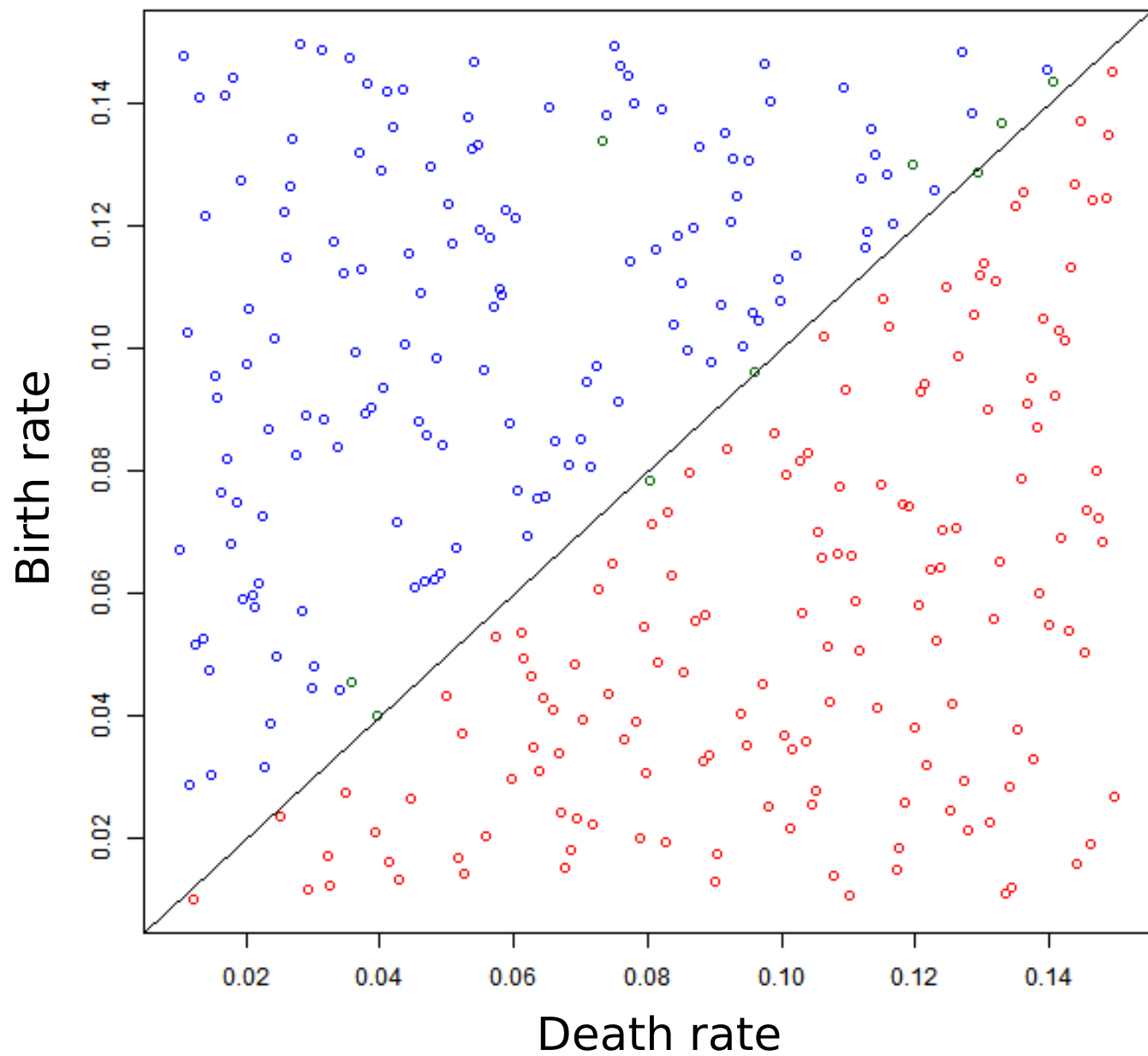
Palo Verde Birth Rate vs. Mortality



Palo Verde Birth Rate vs. Mortality



Palo Verde Birth Rate vs. Mortality



Conclusions

- **Endemism/Coexistence: Both species survives**

$$\begin{array}{cc} \text{bP} & \text{dP} \\ > \end{array}$$

- **Recovery: Cacti extinction**

$$\begin{array}{cc} \text{bP} & \text{dP} \\ = \end{array}$$

- **Extinction: Both species extinct**

$$\begin{array}{cc} \text{bP} & \text{dP} \\ < \end{array}$$

Conclusions

Competition rate (c_{So}), death rate of old cacti (d_{So}) and maturation rate of cacti (g_S) seem to play an important role in the dynamics

Next steps:

- Explore other parameters while controlling the effects of b_p and d_p
- Explicitly include abiotic stress (water availability, temperature conditions, etc)