



Southern-Summer School on Mathematical Biology

Alternative reproductive tactics in cichlid fish

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Sexual selection – characteristics that maximize reproductive success



- Intimidating/defeating opponents of the **same sex** (size dimorphism, secondary sex characteristics)
- Attraction of the **opposite sex** (ornaments)

cichlids

- Family of freshwater fish (Asia, Africa and South America)
- Remarkable dimorphism (size, color, ornaments)



Apistogramma cacatuoides. Amazon Basin, South America

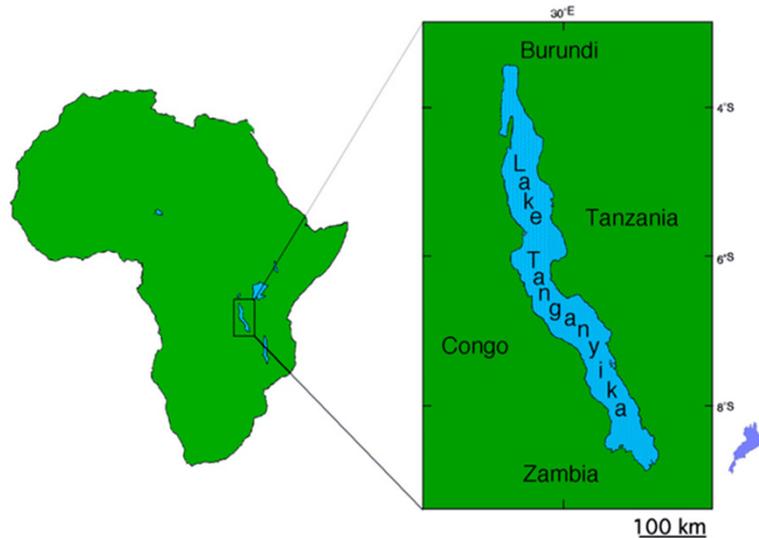


Aulonocara jacobfreibergi. Lake Malawi, Africa

- External fertilization in fish (allowing the selection of **parasitic** tactics)

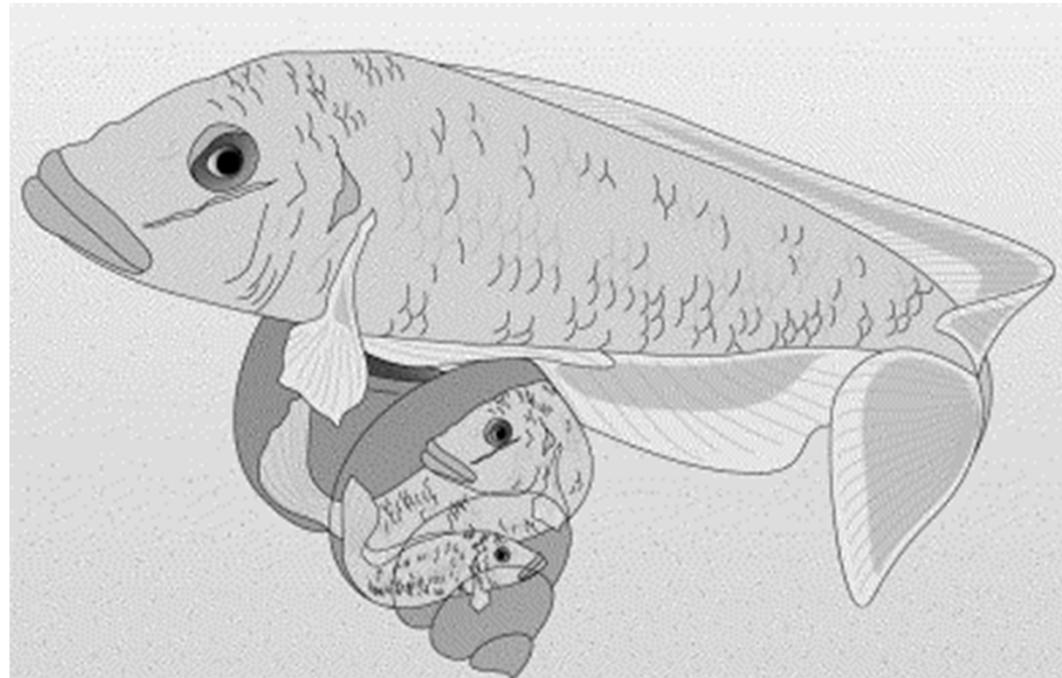
Taborsky. 2001. The Journal of heredity.

Alternative Reproductive Tactics



- *Lamprologus callipterus*
- Strong size dimorphism (competition between large males)
- Males collect and guard shells (nests)
- Females shelter and spawn in shells

- Very small males are able to enter inside guarded shells and breed with females during the reproductive period (**parasitic tactic**)
 - Small males go to innermost part of the shell
- Tactics are hereditary (size of male offspring is related to the size of the father)
 - Sizes between males tactics are disproportional (bimodal selection of male size)



Wirtz-Ocana et al. 2013. Ecology and Evolution.



Strategies

- **Bourgeois**
 - Nesting
 - Large sized
- **Dwarf**
 - Small sized
 - Cryptic (detection)

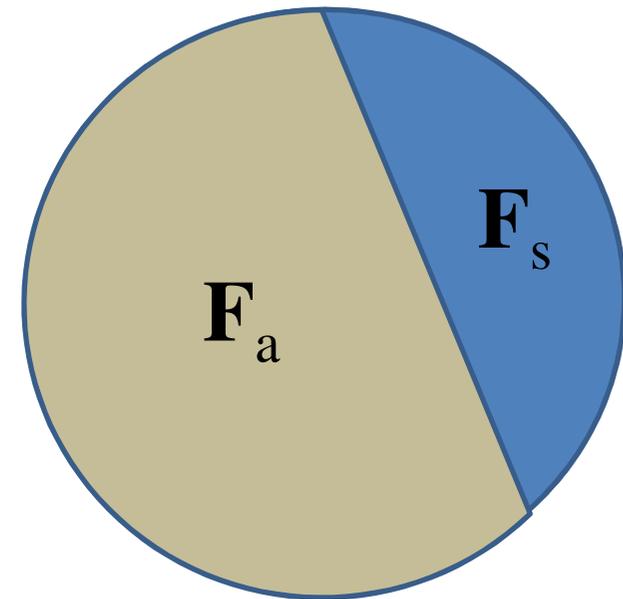
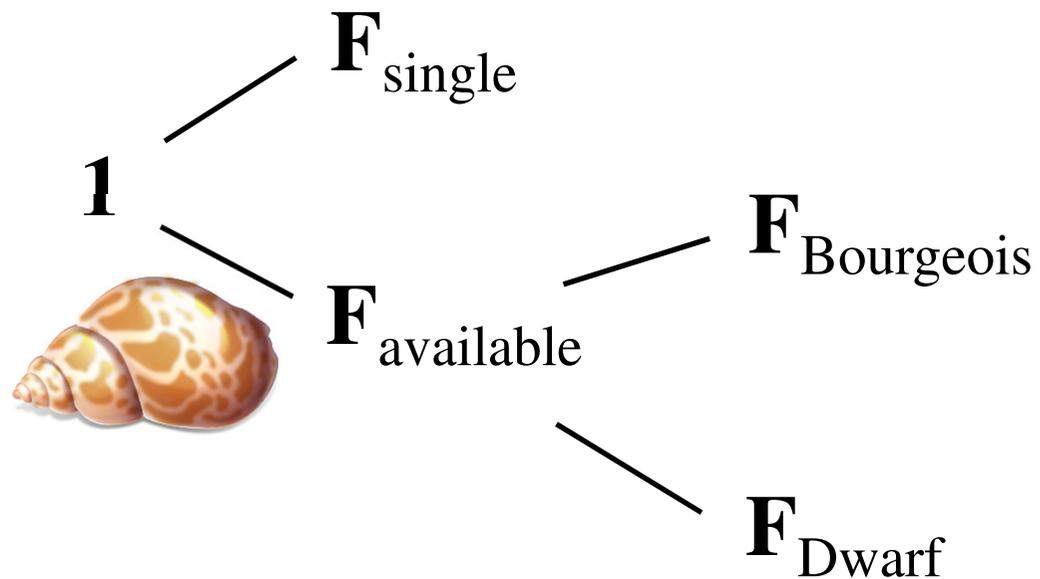


Question

- In which conditions there is long-term coexistence of both strategies in a population?

Assumptions

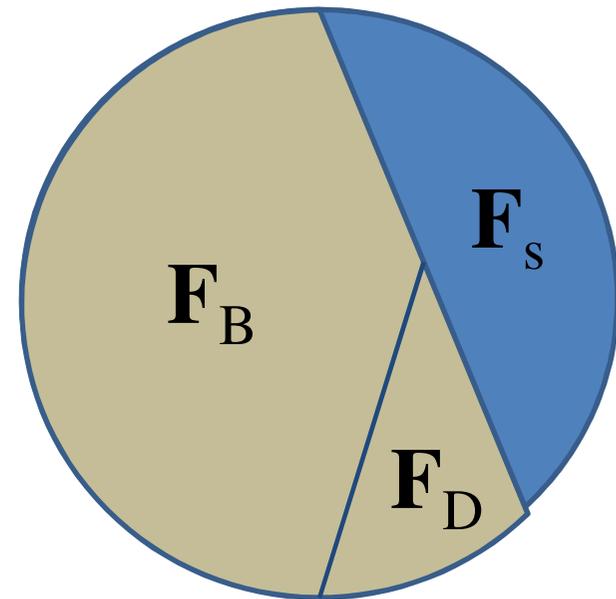
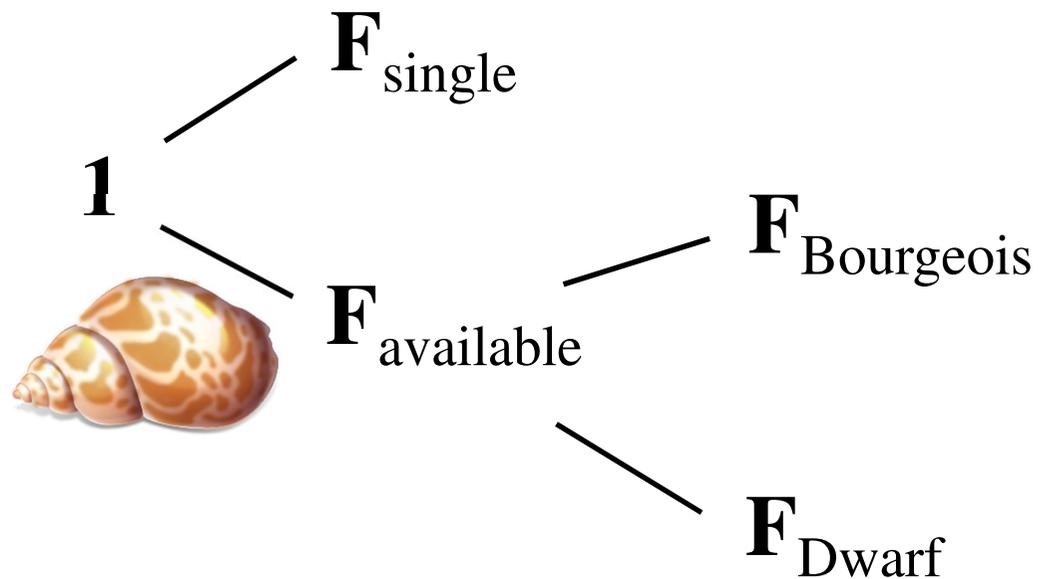
- Total females are constant in time (simplify)
- Proportion of females



$$1 = F_S + F_B + F_D$$

Assumptions

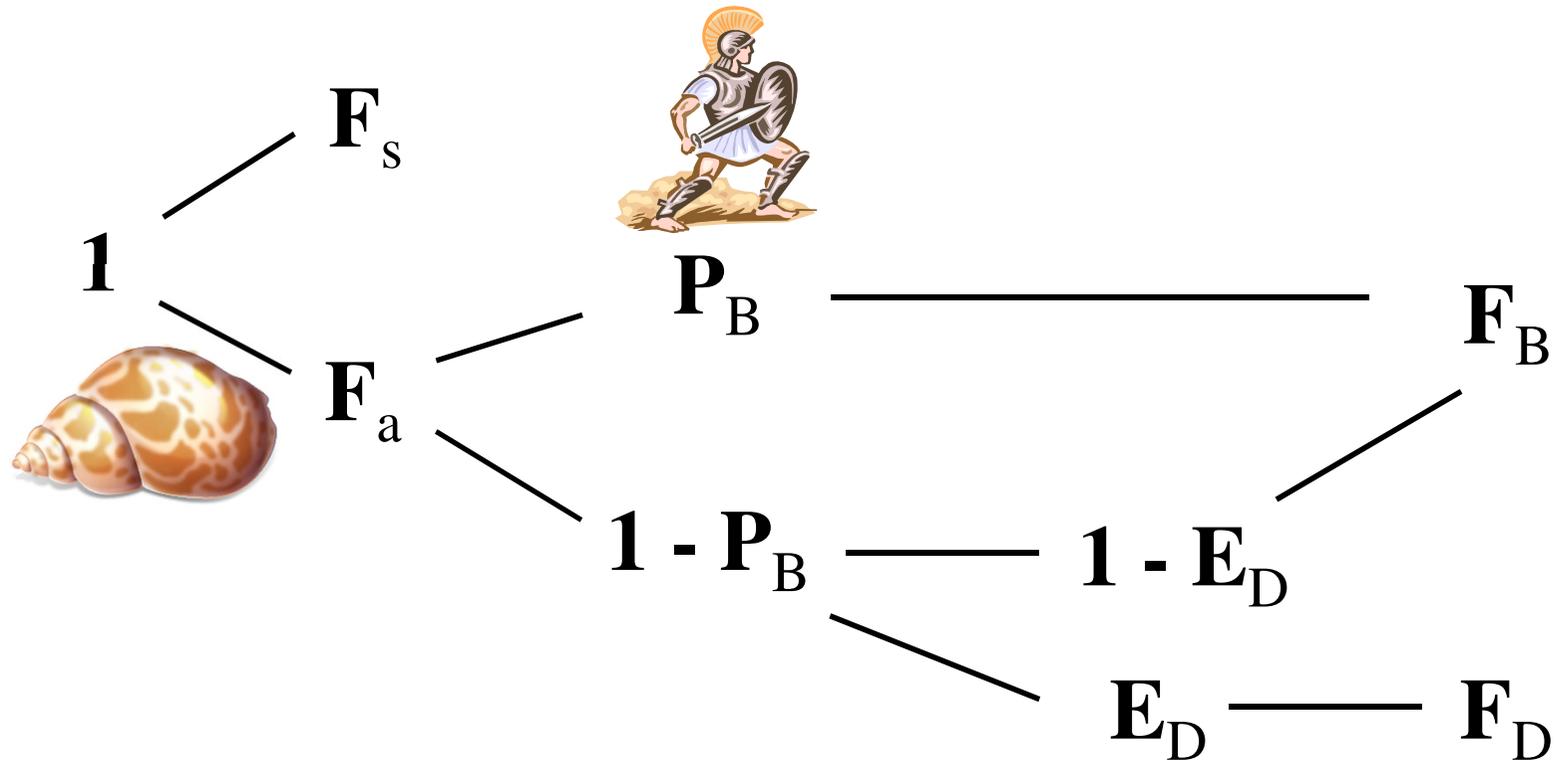
- Total females are constant in time (simplify)
- Proportion of females



$$1 = F_S + F_B + F_D$$

Assumptions

- Available females could be protected or not
- Non protected females can mate with dwarf or bourgeois



P_B = Proportion of females protected
 E_D = Proportion of females parasitized



Assumptions

- Bourgeois are essential for the reproduction of the species (nesting)



$$F_s = \frac{1}{1 + e B / F}$$

F_s = Proportion of single females

e = Efficiency of building nests

B = Bourgeois

F = Number of females (fixed)

Differential equations

$$\left\{ \begin{array}{l} \frac{dB}{dt} = aF_B F - bB \\ \frac{dD}{dt} = cF_D F - dD \end{array} \right.$$

B = Number of Bourgeois

D = Number of Dwarfs

F = Total number of females (fixed)

F_B = Proportion of females that mate with B

F_D = Proportion of females that mate with D

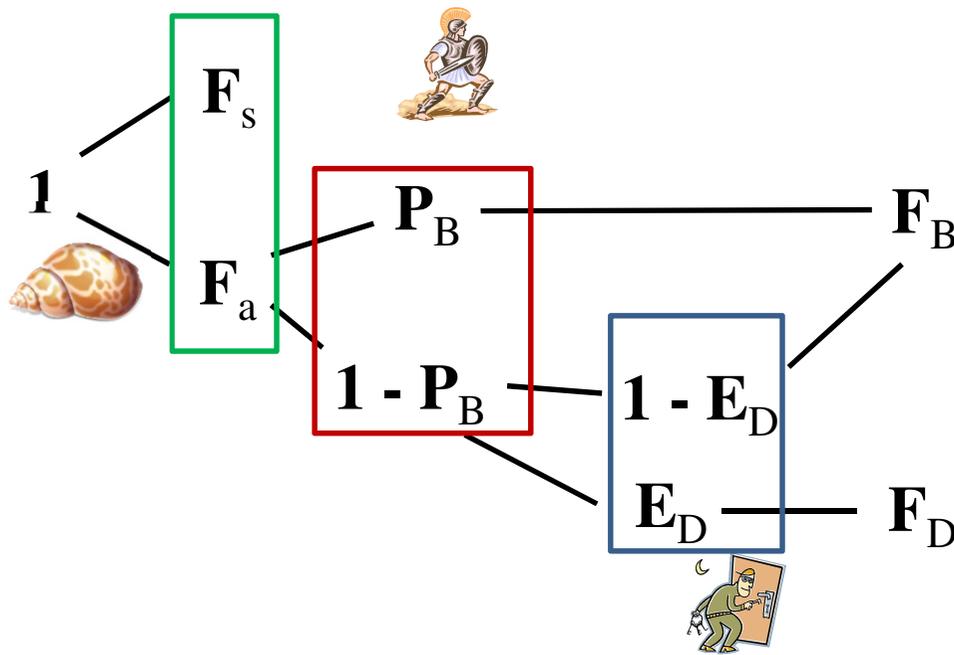
a = Intrinsic reproductive rate of B

b = Death rate of B

c = Intrinsic reproductive rate of D

d = Death rate of D

Conditions



$$F_s = \frac{1}{1 + e B/F}$$

$$P_B = \frac{g B/F(1 - F_s)}{1 + g B/F(1 - F_s)}$$

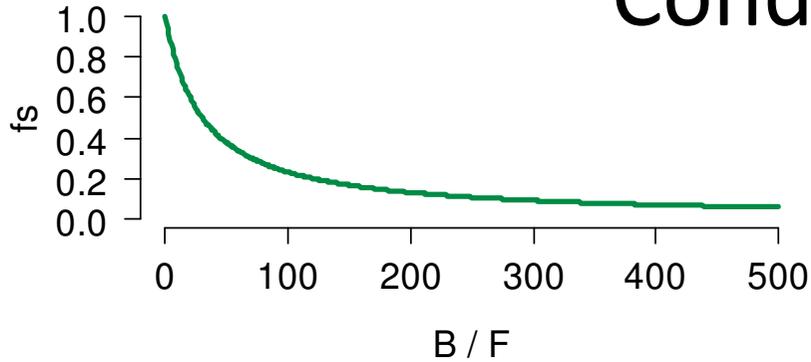
$$E_D = \frac{h D/F(1 - F_s)}{1 + h D/F(1 - F_s)}$$

e = Efficiency of nesting

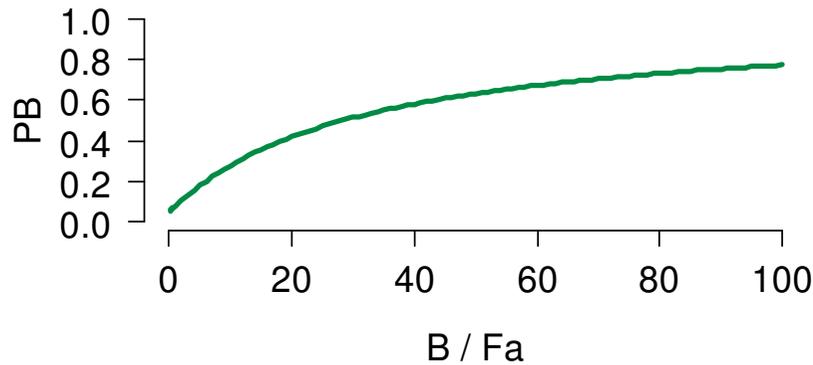
g = Intrinsic capacity to protect females

h = Intrinsic capacity of cheating

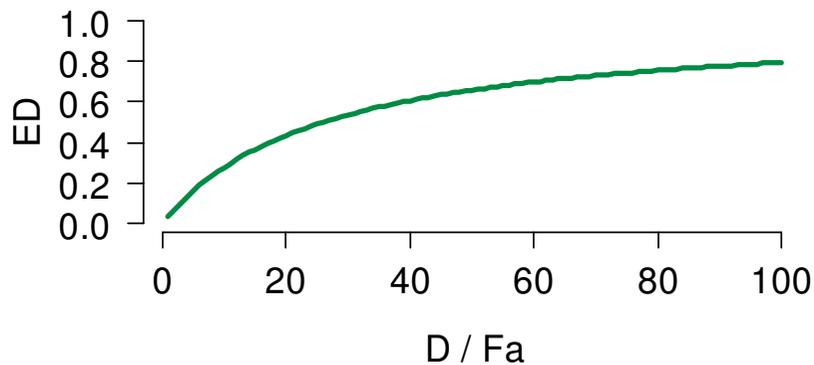
Conditions



$$F_s = \frac{1}{1 + e B/F}$$



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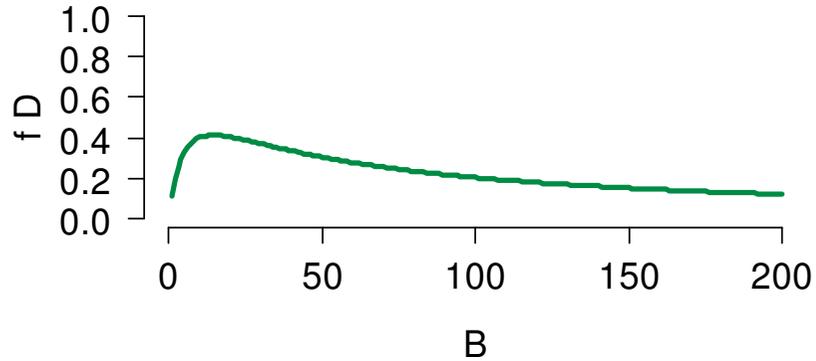
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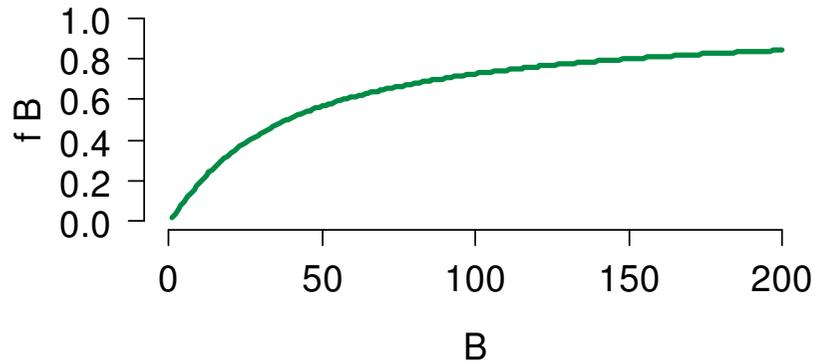
P_B = Proportion of females protected

E_D = Proportion of females parasitized

Conditions



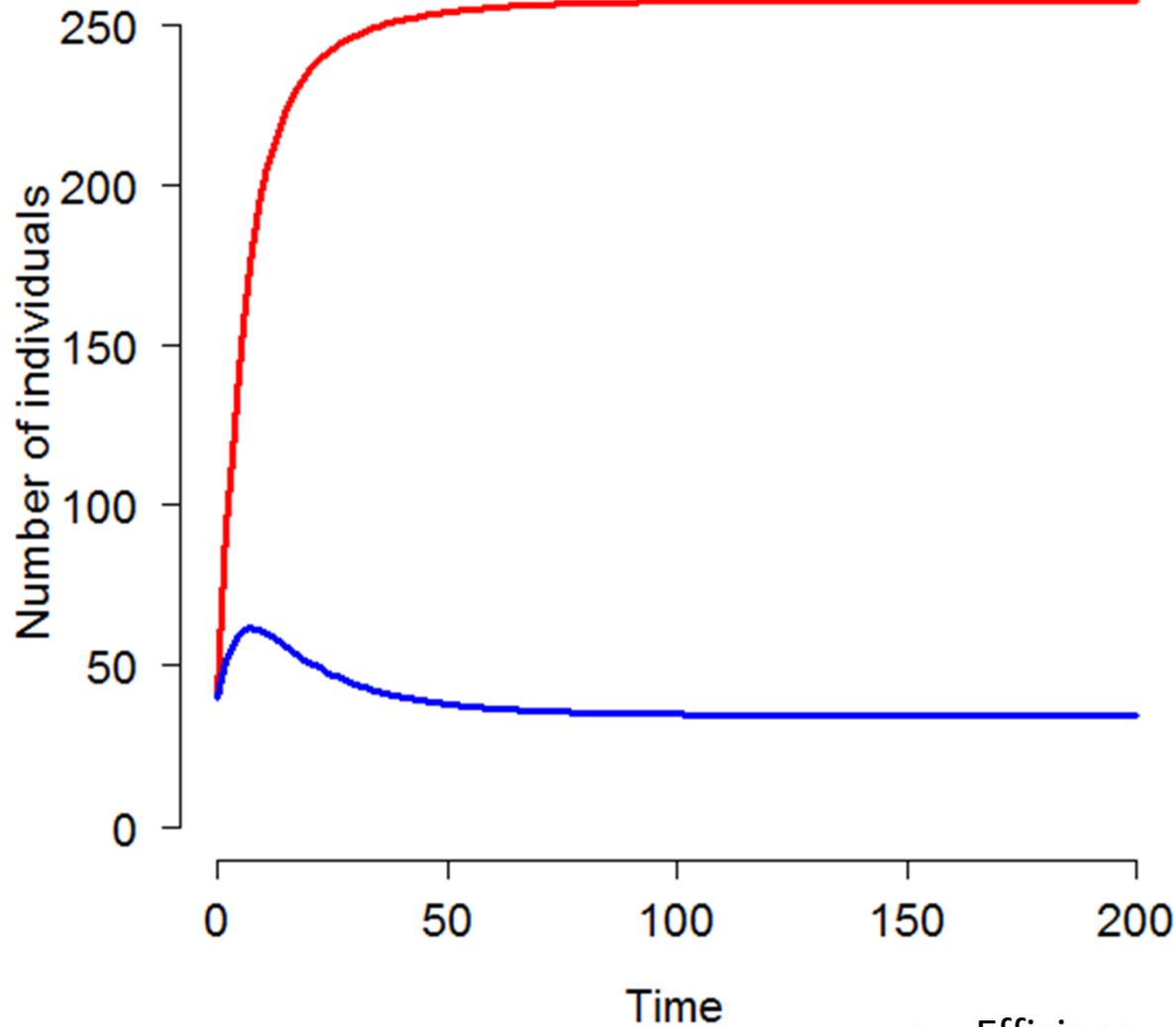
$$F_D = (1 - F_S)(1 - P_B)E_D$$



$$F_B = (1 - F_S) - F_D$$

P_B = Proportion of females protected

E_D = Proportion of females parasitized



F = 100

B = 40

D = 40

e = 10

g = 0.4

h = 0.8

a = 0.6

b = 0.2

c = 1.0

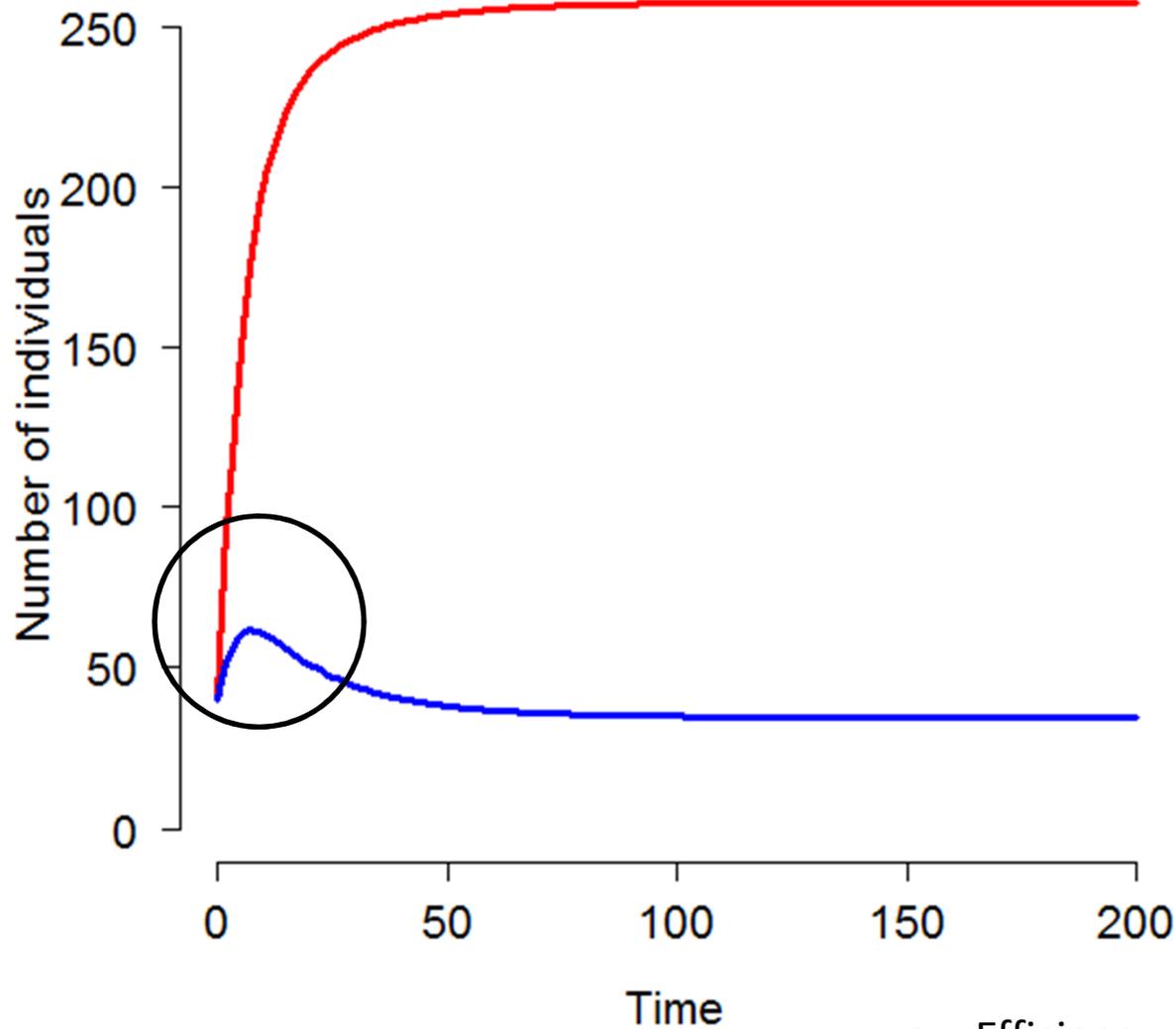
d = 0.3

— Bourgeois — Dwarf

e = Efficiency of nesting

g = Intrinsic capacity to protect females

h = Intrinsic capacity of cheating



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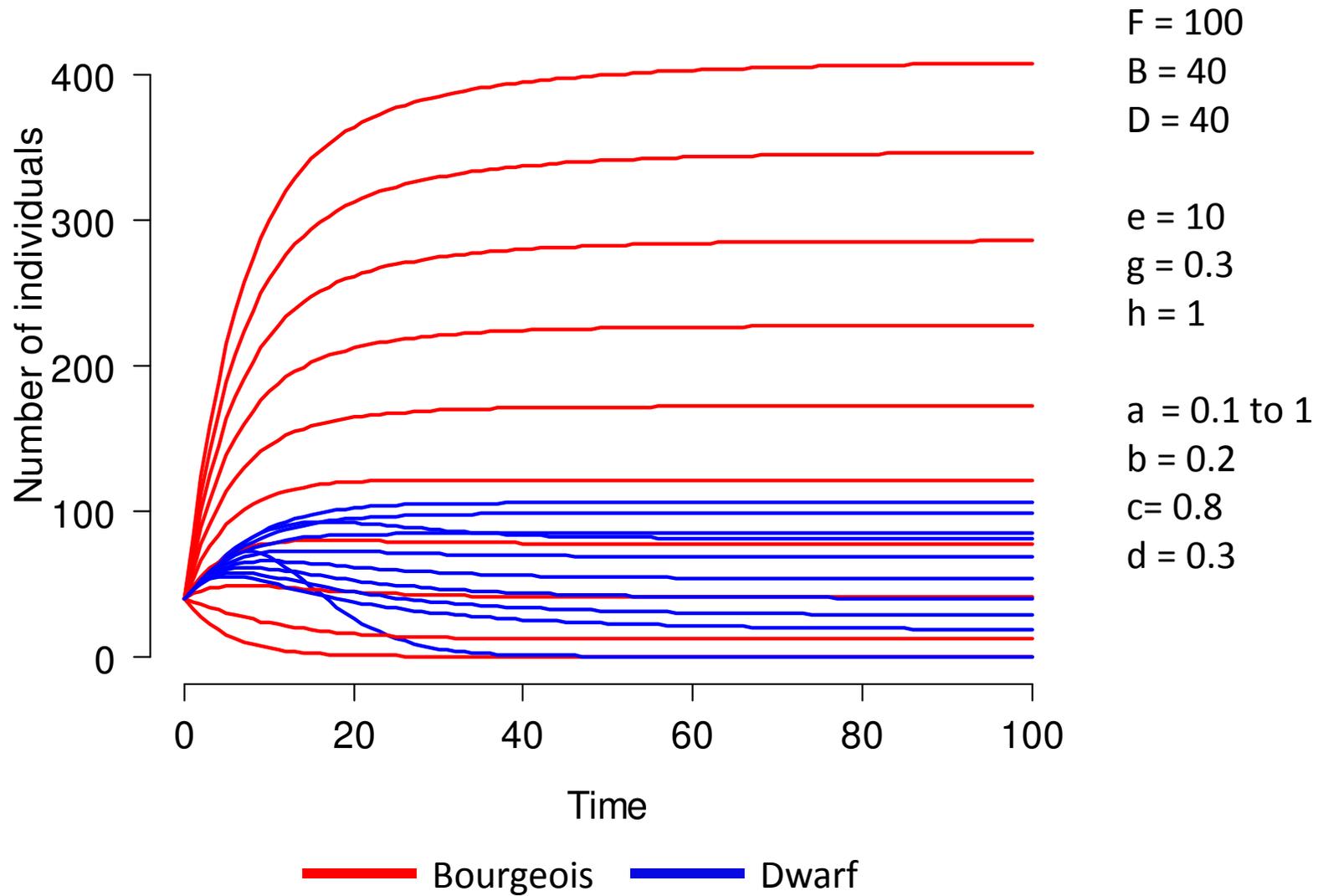
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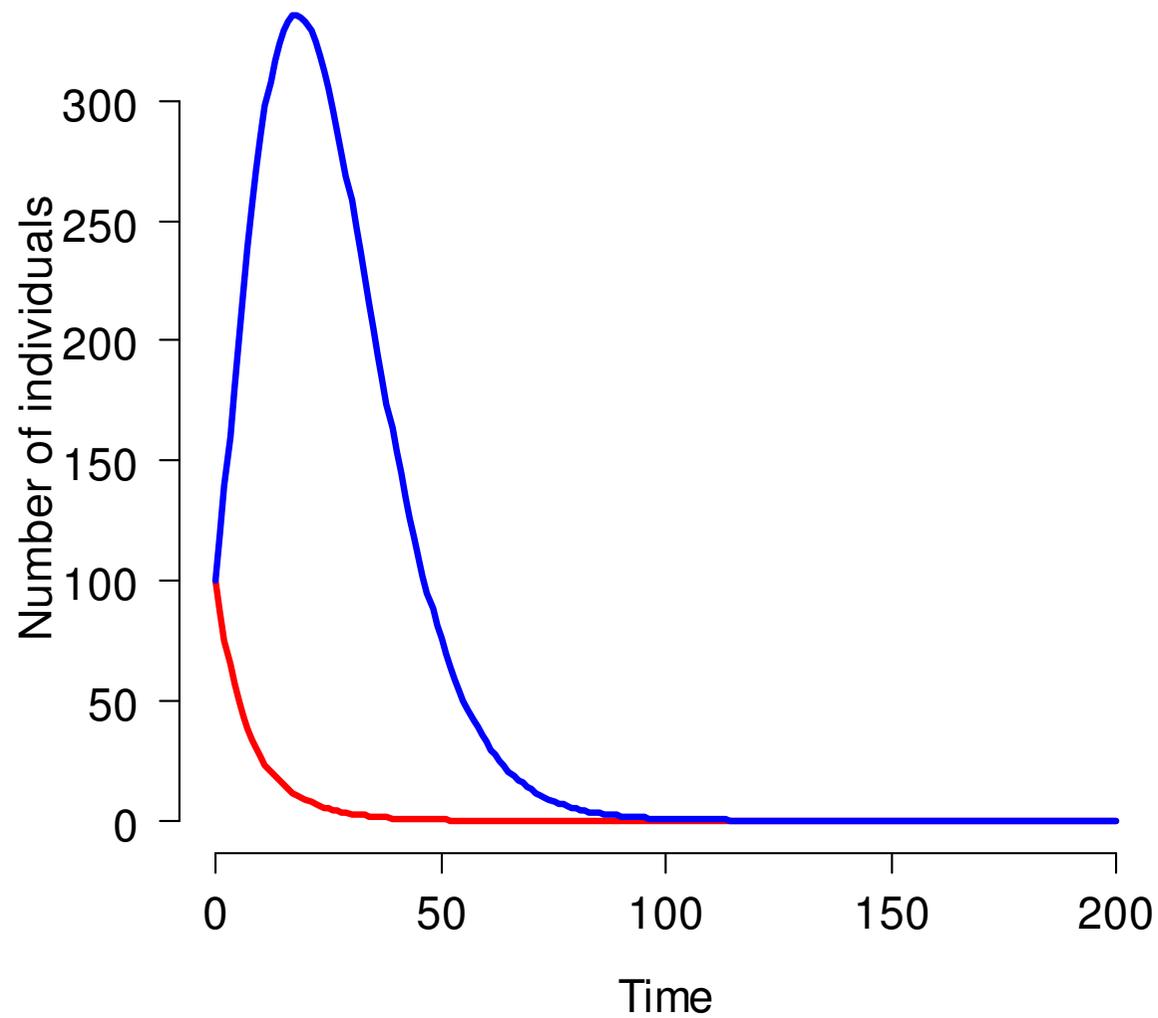
e = Efficiency of nesting

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Ranging a from 0.1 to 1





F = 100

B = 100

D = 100

e = 10

g = 0.3

h = 1

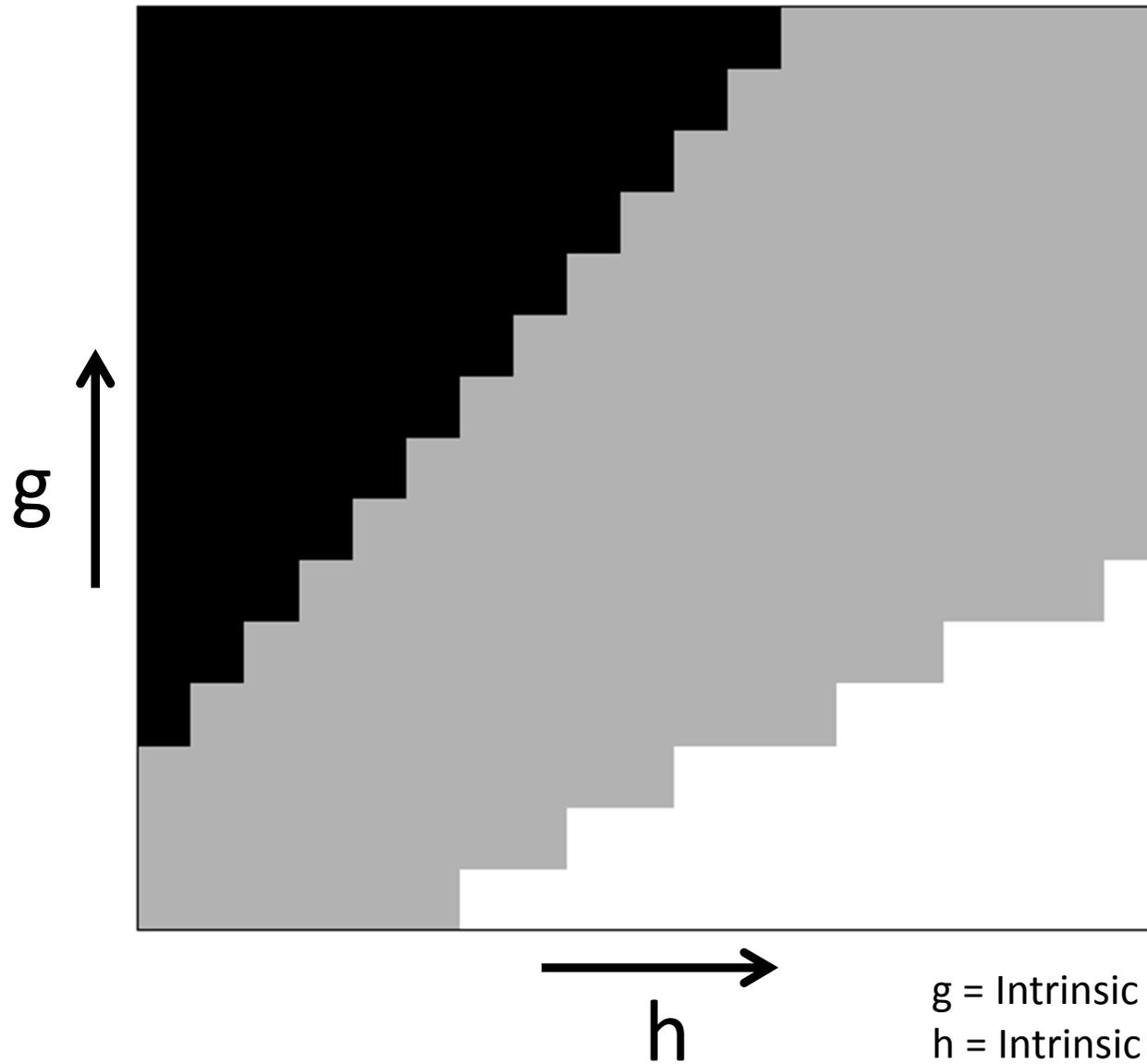
a = 0.1

b = 0.2

c = 0.8

d = 0.1

— Bourgeois — Dwarf



g = Intrinsic capacity to protect females
 h = Intrinsic capacity of cheating



Conclusion

Coexistence will depend on growth and death rates of each strategy (a, b, c and d) – D depends on B

Coexistence (relation between g and h)

- Bourgeois competition (g)
 - Bourgeois is always busy (Protection is not perfect)
- Cryptic ability of dwarf (h)
 - Camouflage, mimic females... (threshold of low values of h for coexistence)
 - High values of parasite efficiency extinct the species (threshold of high values)

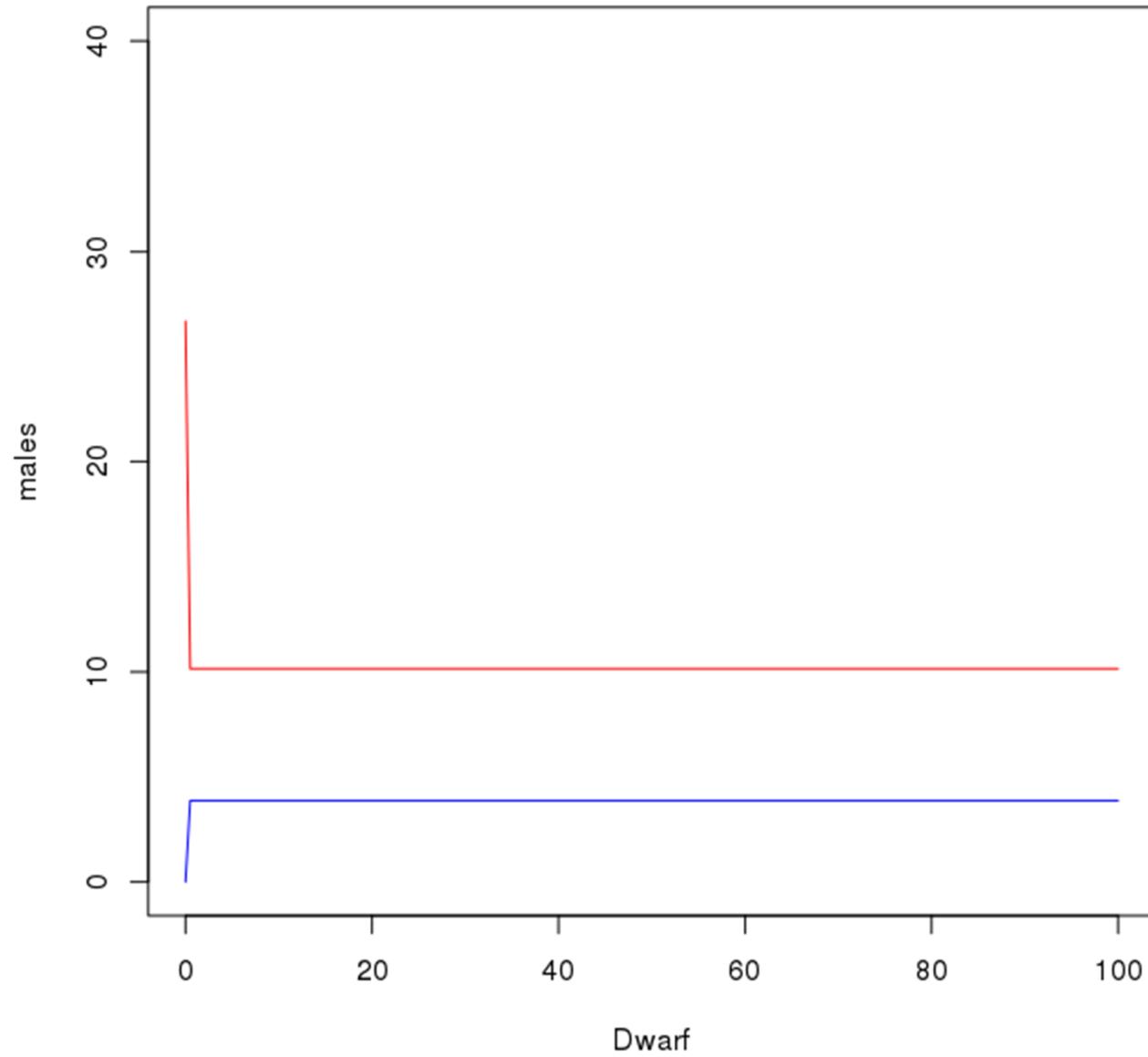
Thank you

- Assistants: Bernardo Niebuhr, Diogo Melo and Fernando Rossine, Renato Coutinho, Ayana Martins, Flávia...
- Otso Ovaskainen and François Massol

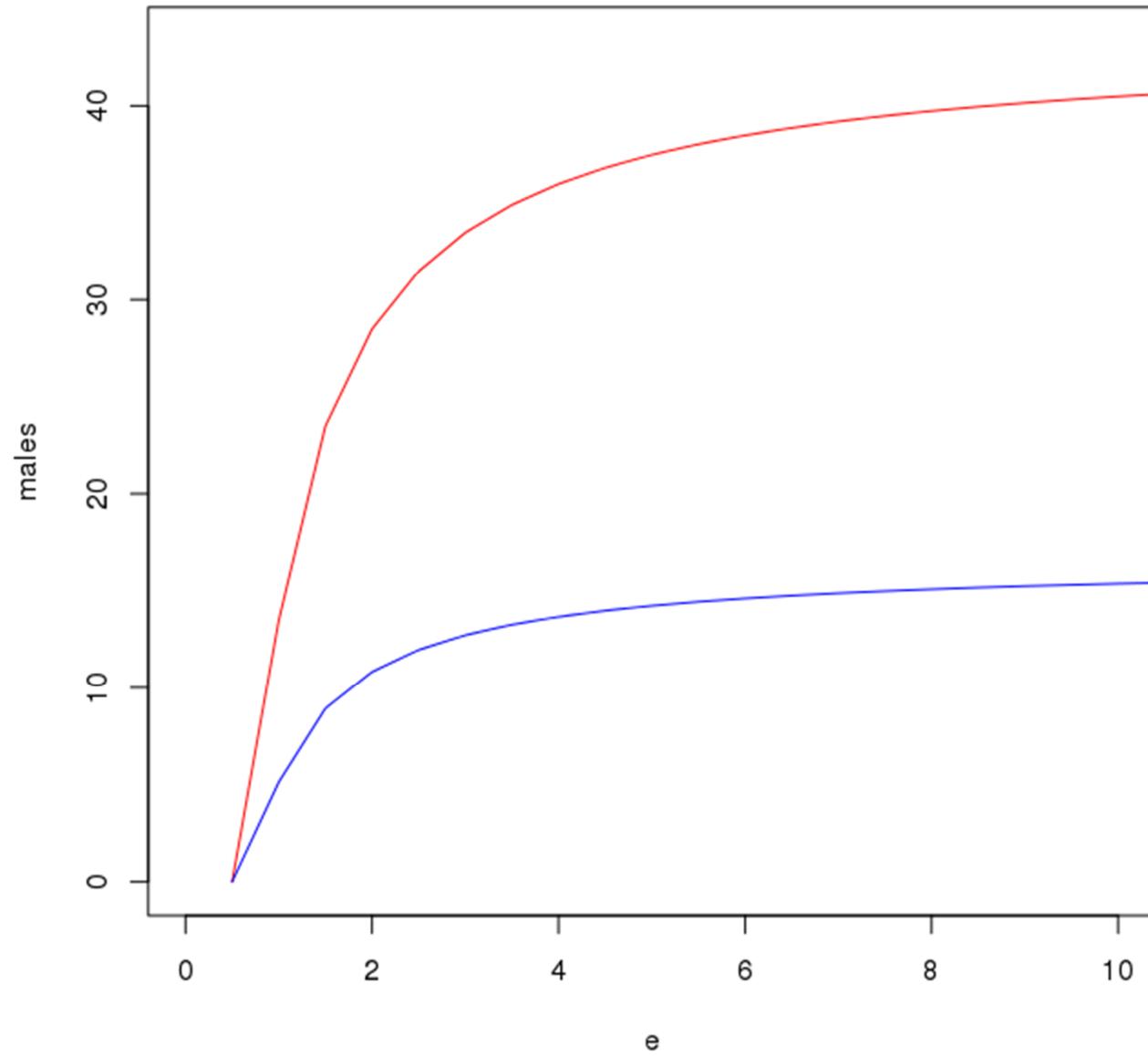


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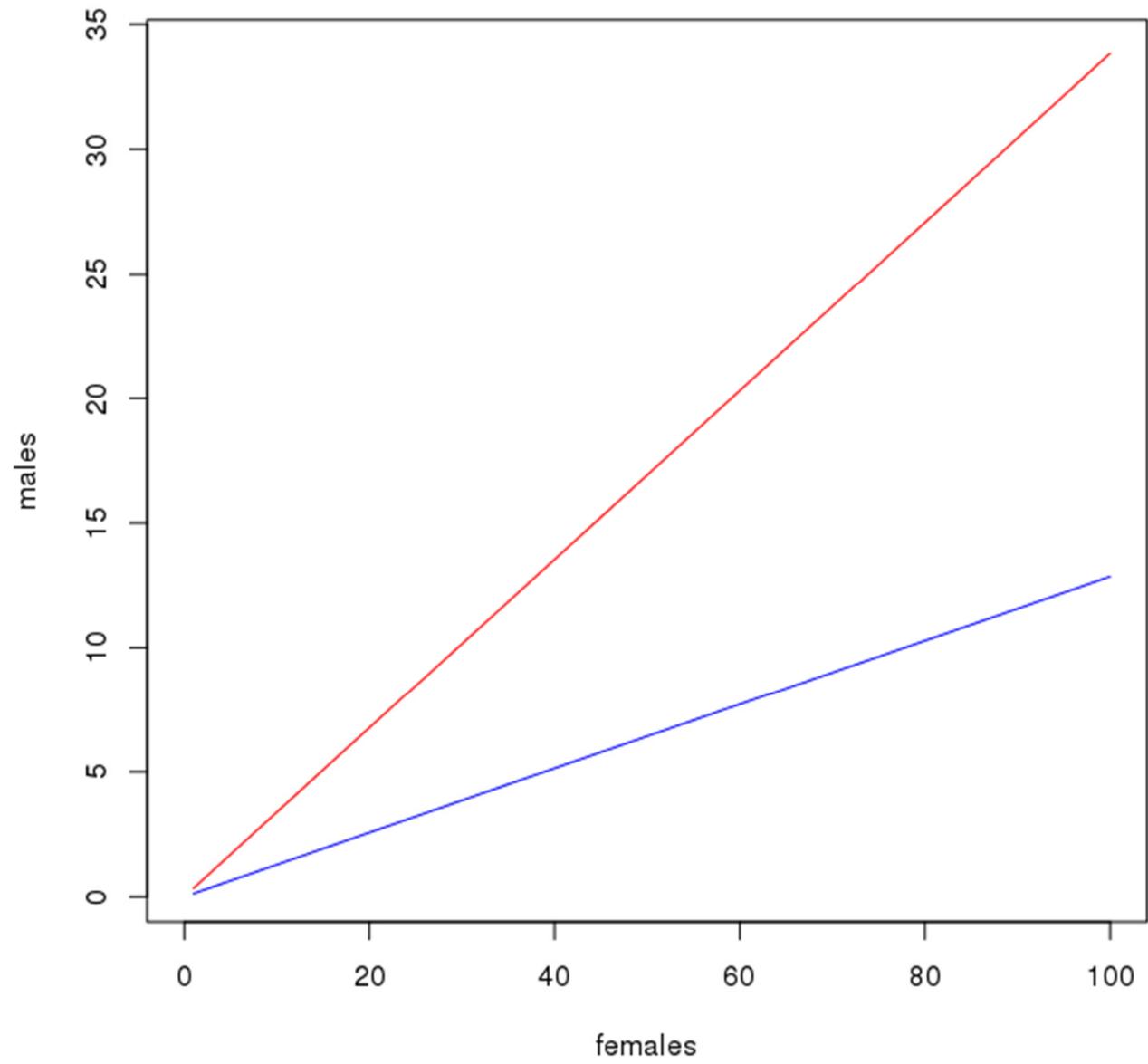
(a=1,b=0.5,ci=1,d=0.5,e=0.9,g=0.2,h=1,Fi=30)



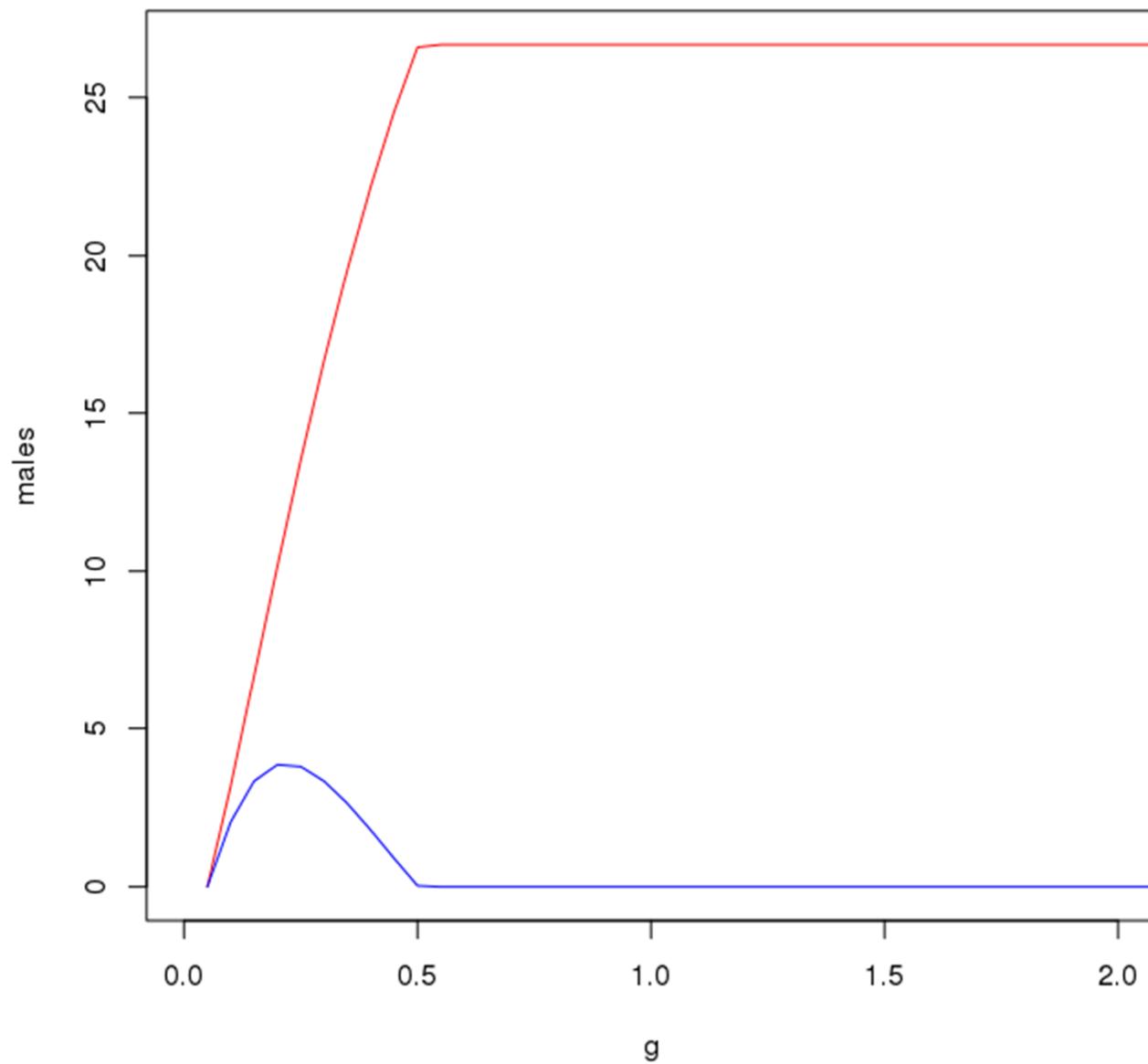
(a=1,b=0.5,ci=1,d=0.5,e=i,g=0.2,h=1,Fi=30)



(a=1,b=0.5,ci=1,d=0.5,e=0.9,g=0.2,h=1,Fi=i



(a=1,b=0.5,ci=1,d=0.5,e=0.9,g=0.2,h=i,Fi=30)



(a=1,b=0.5,ci=1,d=0.5,e=0.9,g=0.2,h=i,Fi=30)

