

# III Southern-Summer School on Mathematical Biology

## Miley Cyrus vs. Darth Vader



**The manipulative  
parasite and the  
gliding ant**



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Luciano Peres  
Thiago Zahn  
Willian Silva**

# INTRODUCTION

**Manipulative parasites: parasite inducing phenotypic changes in their hosts that increase the probability of their transmission from one host to another.**

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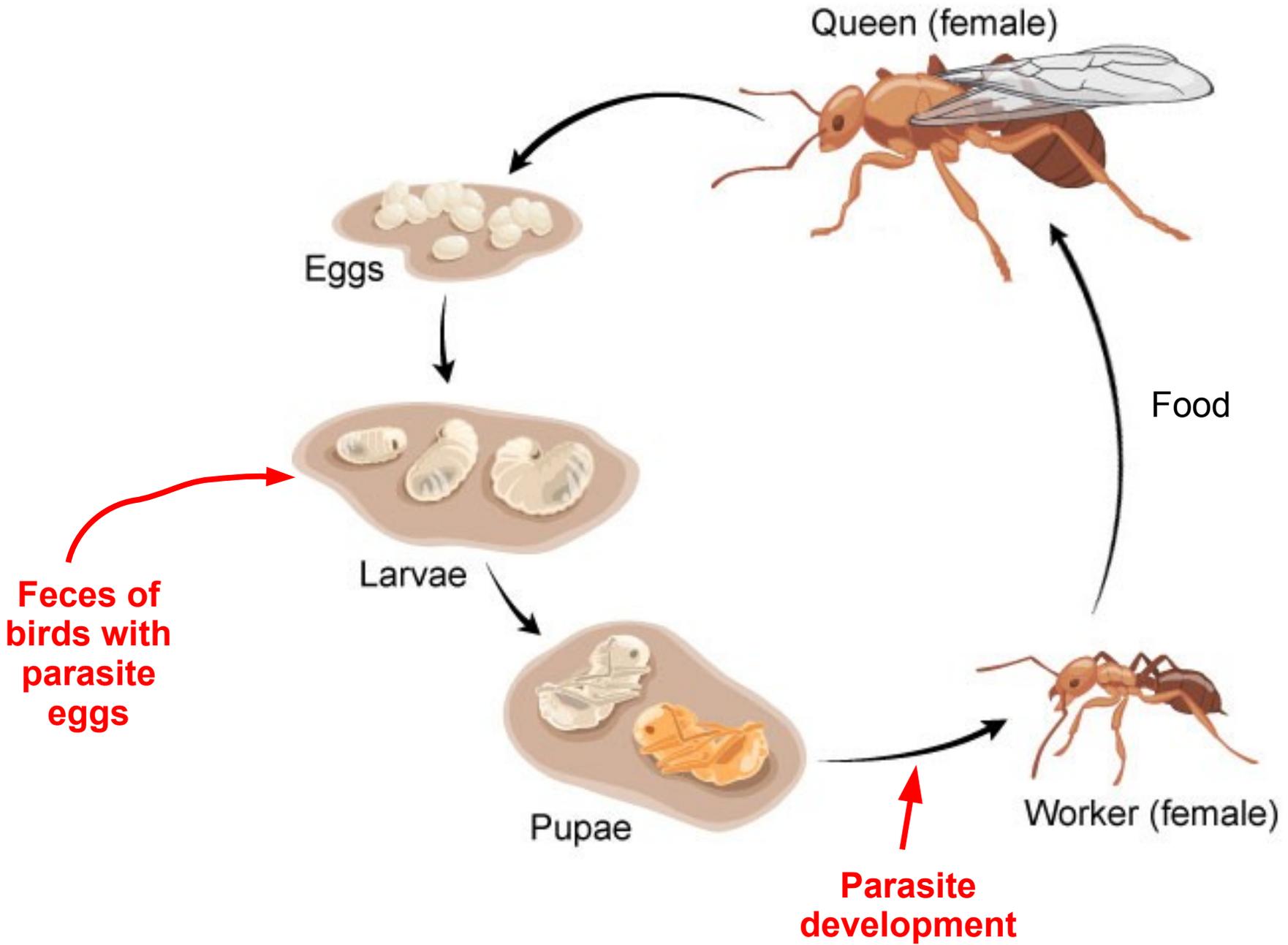
**Host: *Cephalotes atratus* (Darth Vader ant)**  
**Parasite: *Myrmeconema neotropicum***

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# QUESTIONS

**1. What initial infection rate can promote the establishment of the parasite in the colony?**



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- 2. What predation rate can maintain the parasite in the colony?**



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1. What initial infection rate can promote the establishment of the parasite in the colony?
2. What predation rate can maintain the parasite in the colony?
3. What infection rate makes the colony collapse?



# THEORETICAL DESIGN

**Li**



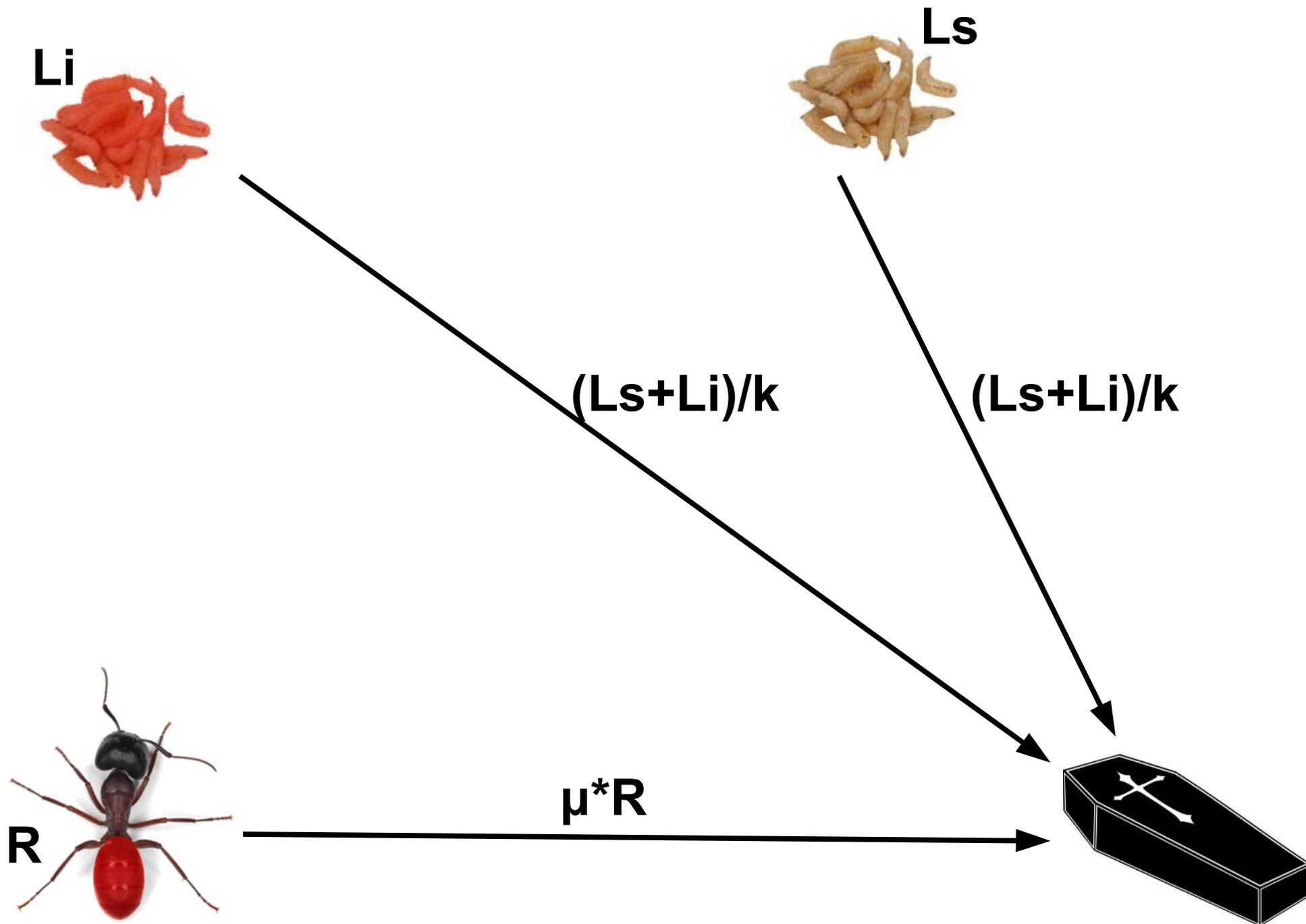
**Li<sub>s</sub>**



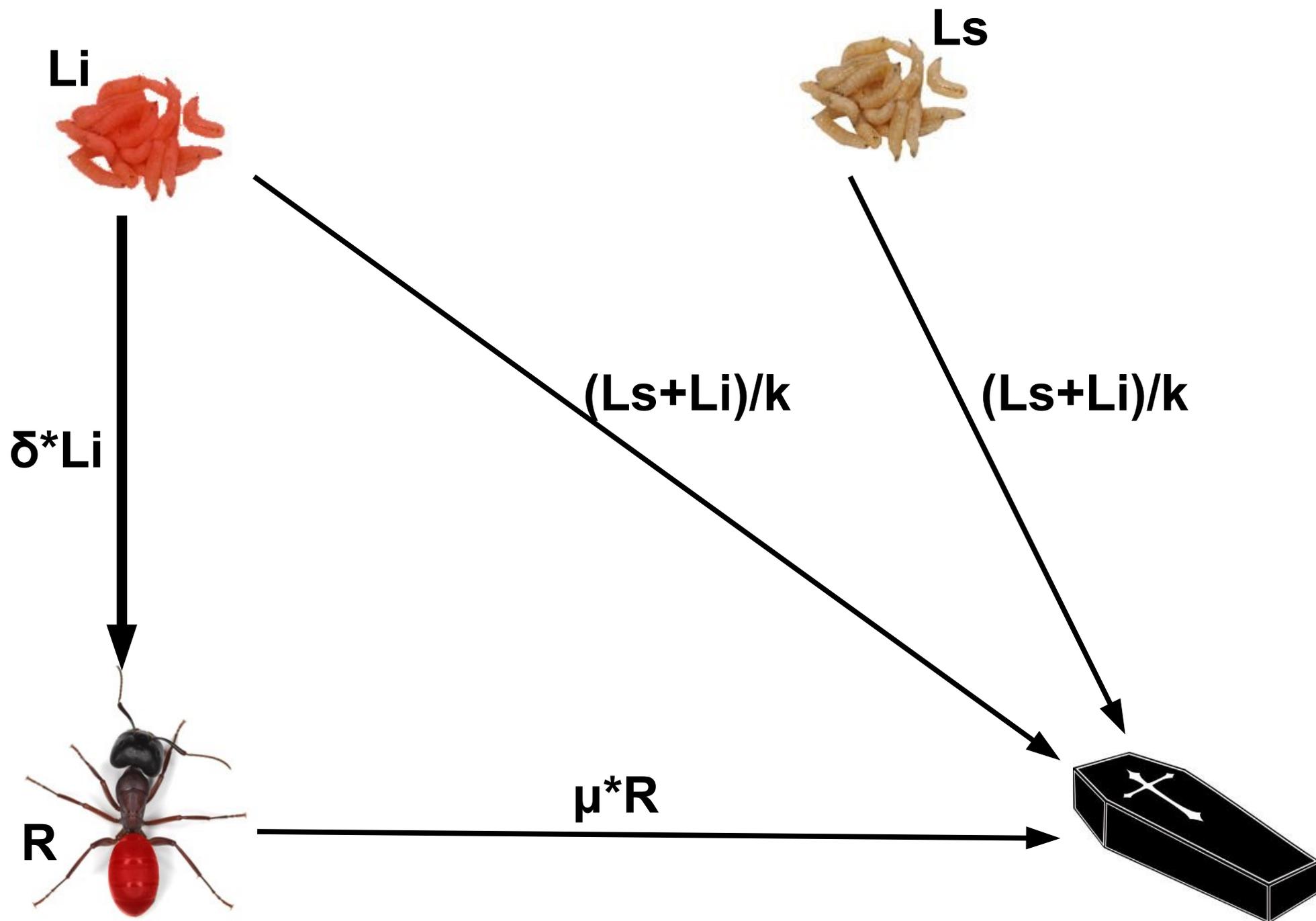
**R**



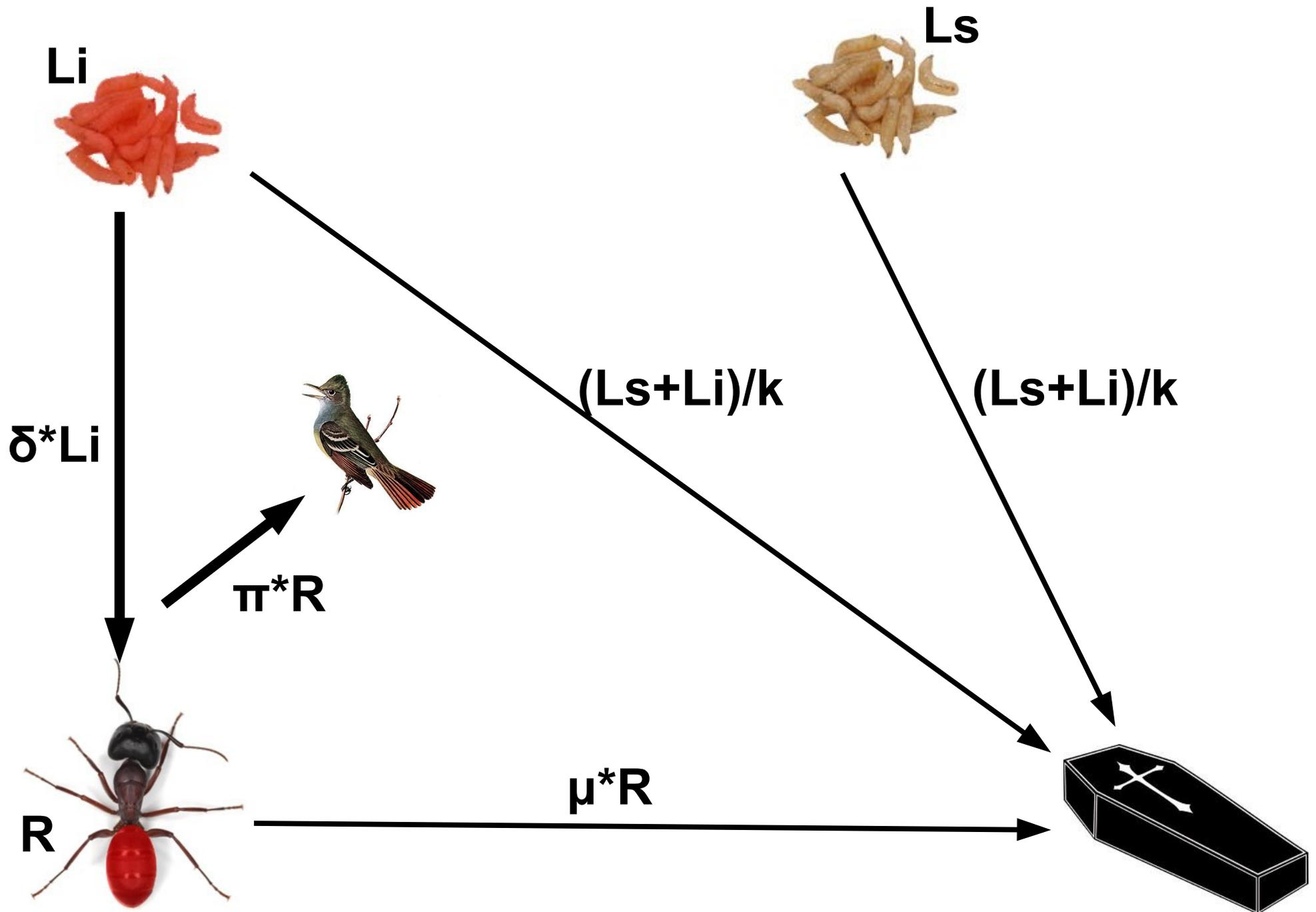
# THEORETICAL DESIGN



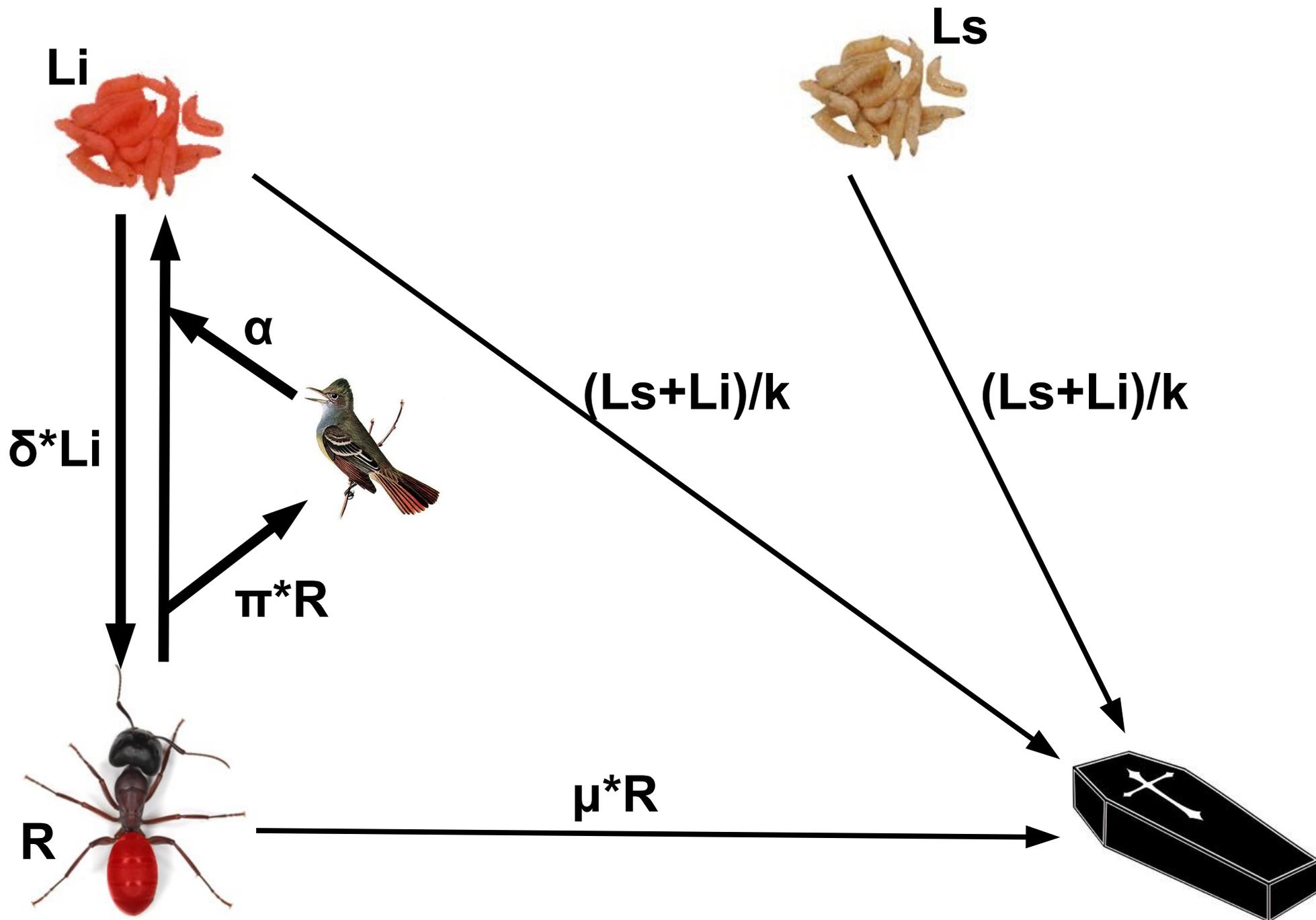
# THEORETICAL DESIGN



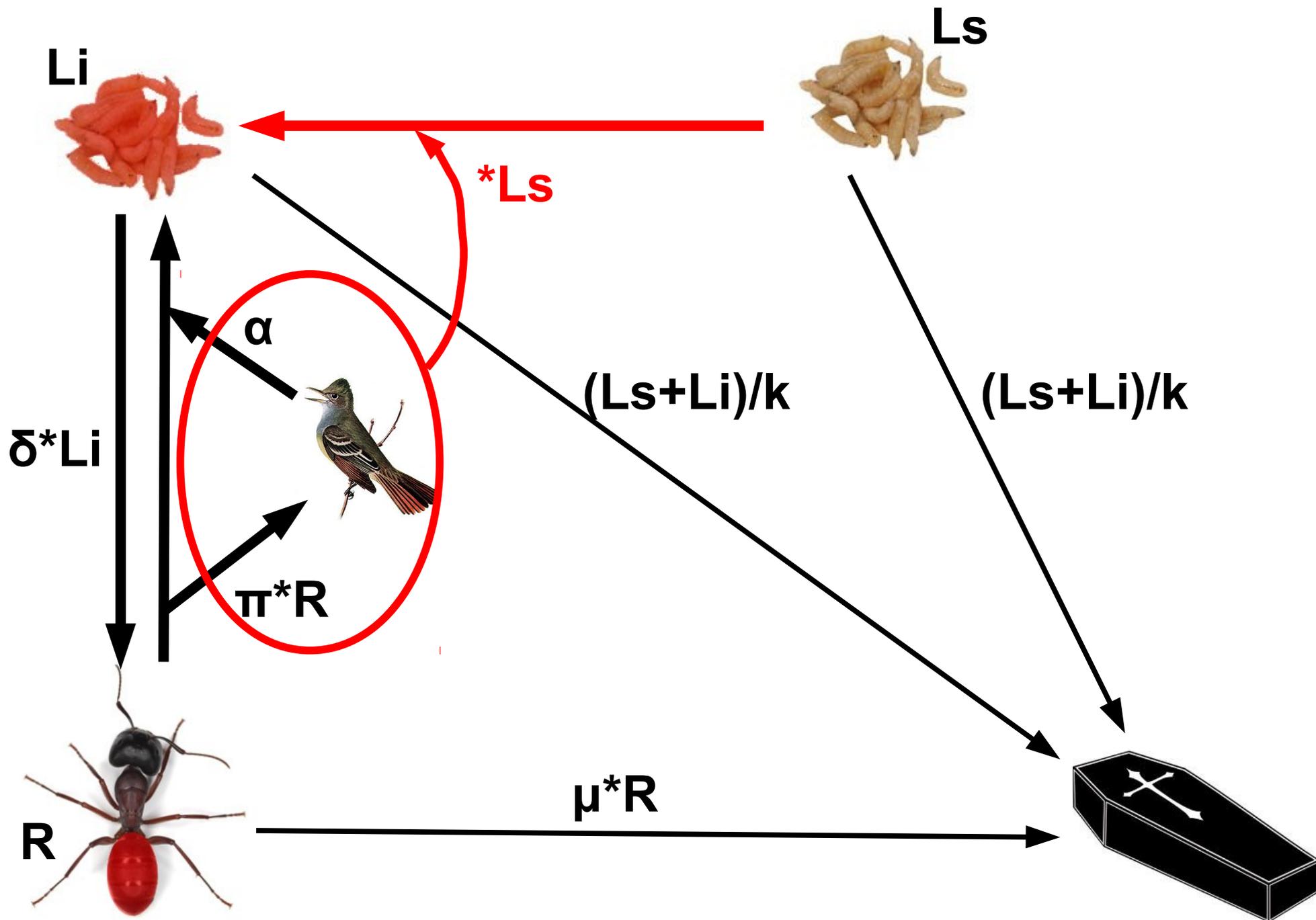
# THEORETICAL DESIGN



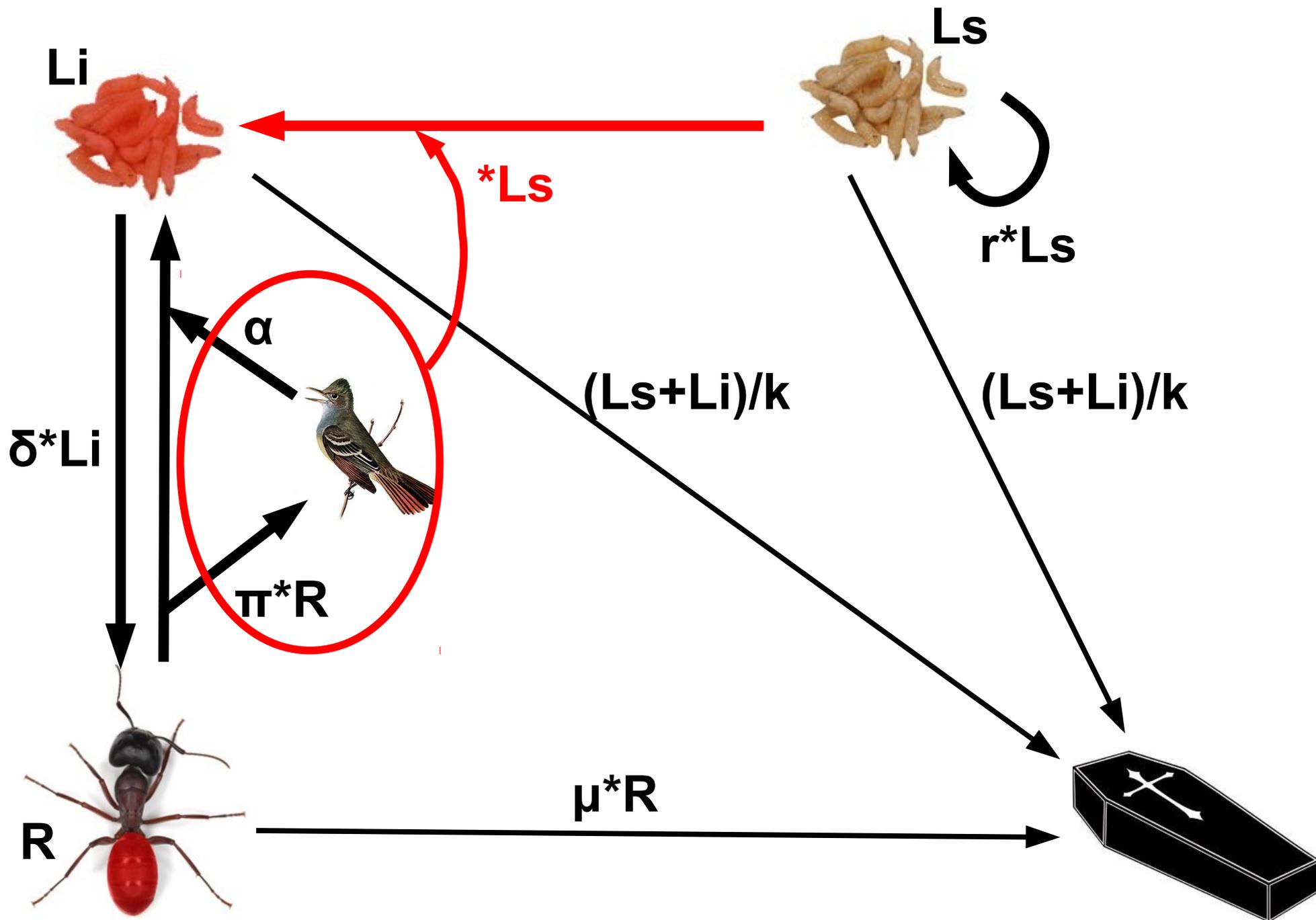
# THEORETICAL DESIGN



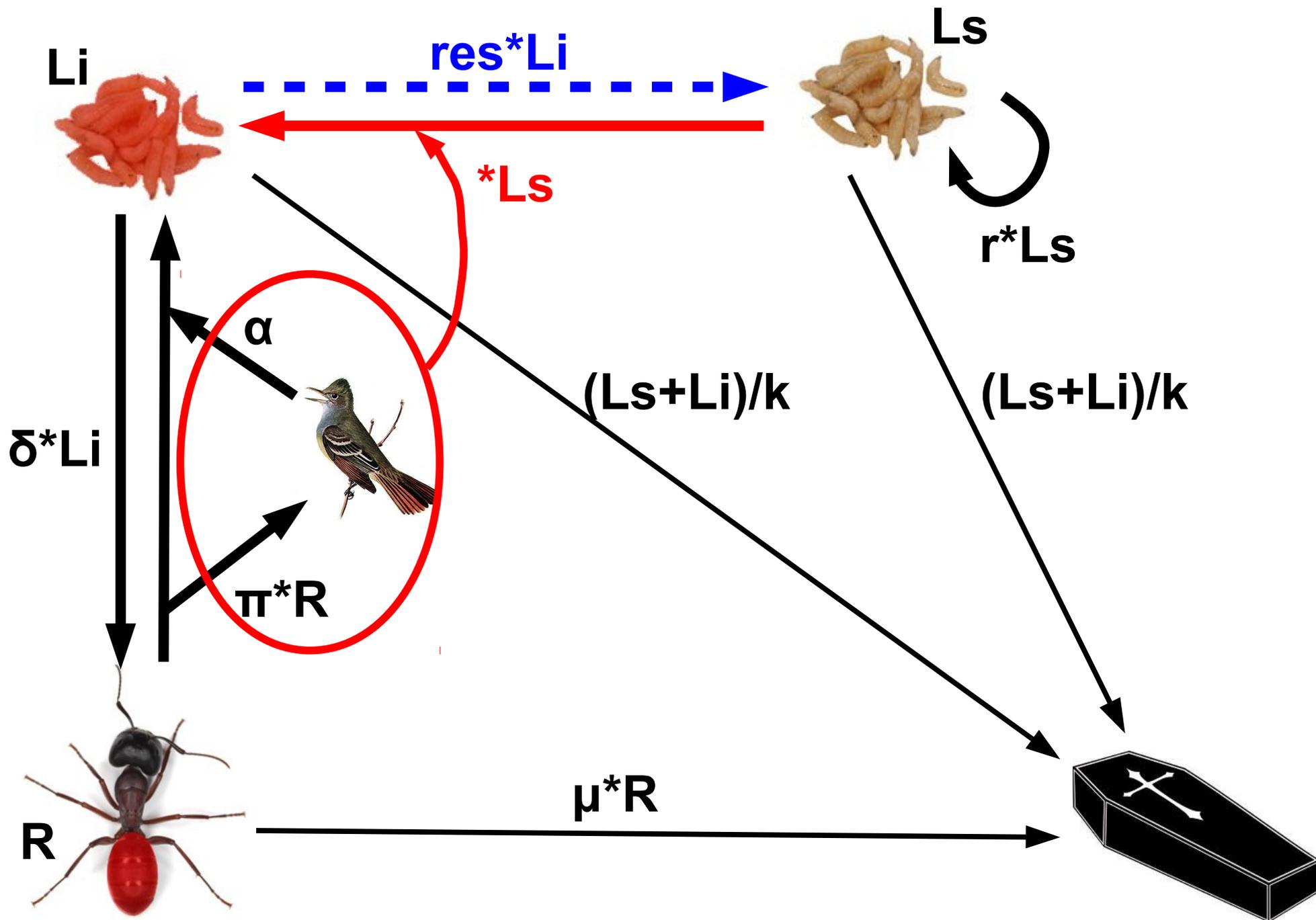
# THEORETICAL DESIGN



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## MATHEMATICAL MODELS



$$\frac{dL_s}{dt} = rL_s \left( 1 - \frac{L_s + L_i}{k} \right) - \alpha\pi L_s R$$

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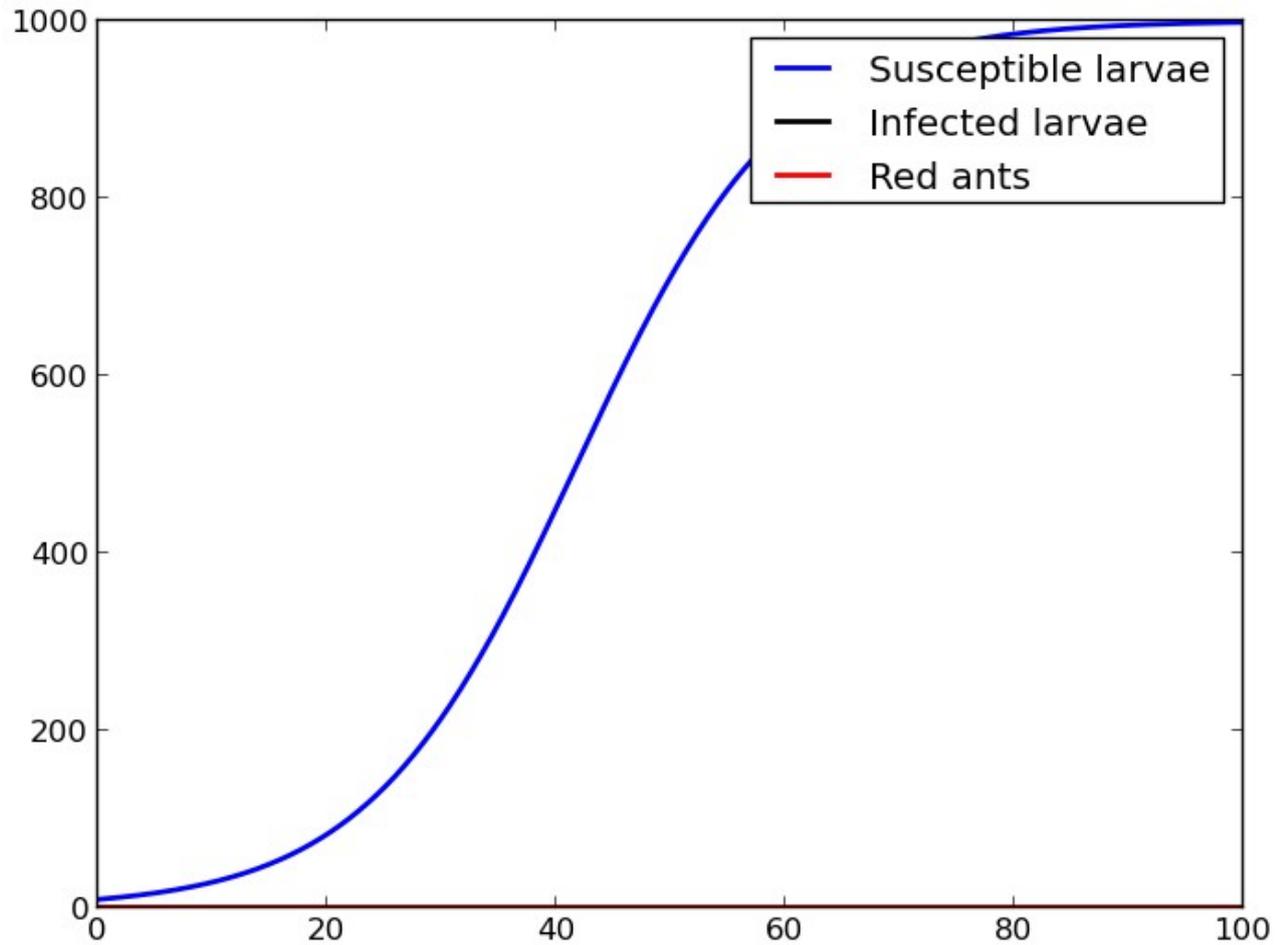
$$\frac{dL_i}{dt} = \alpha\pi L_s R \left(1 - \frac{L_s + L_i}{k}\right) - \delta L_i$$



$$\frac{dR}{dt} = L_i \delta - (\pi + \mu)R$$

# RESULTS

# Control Simulations



**$L_s = 10$**



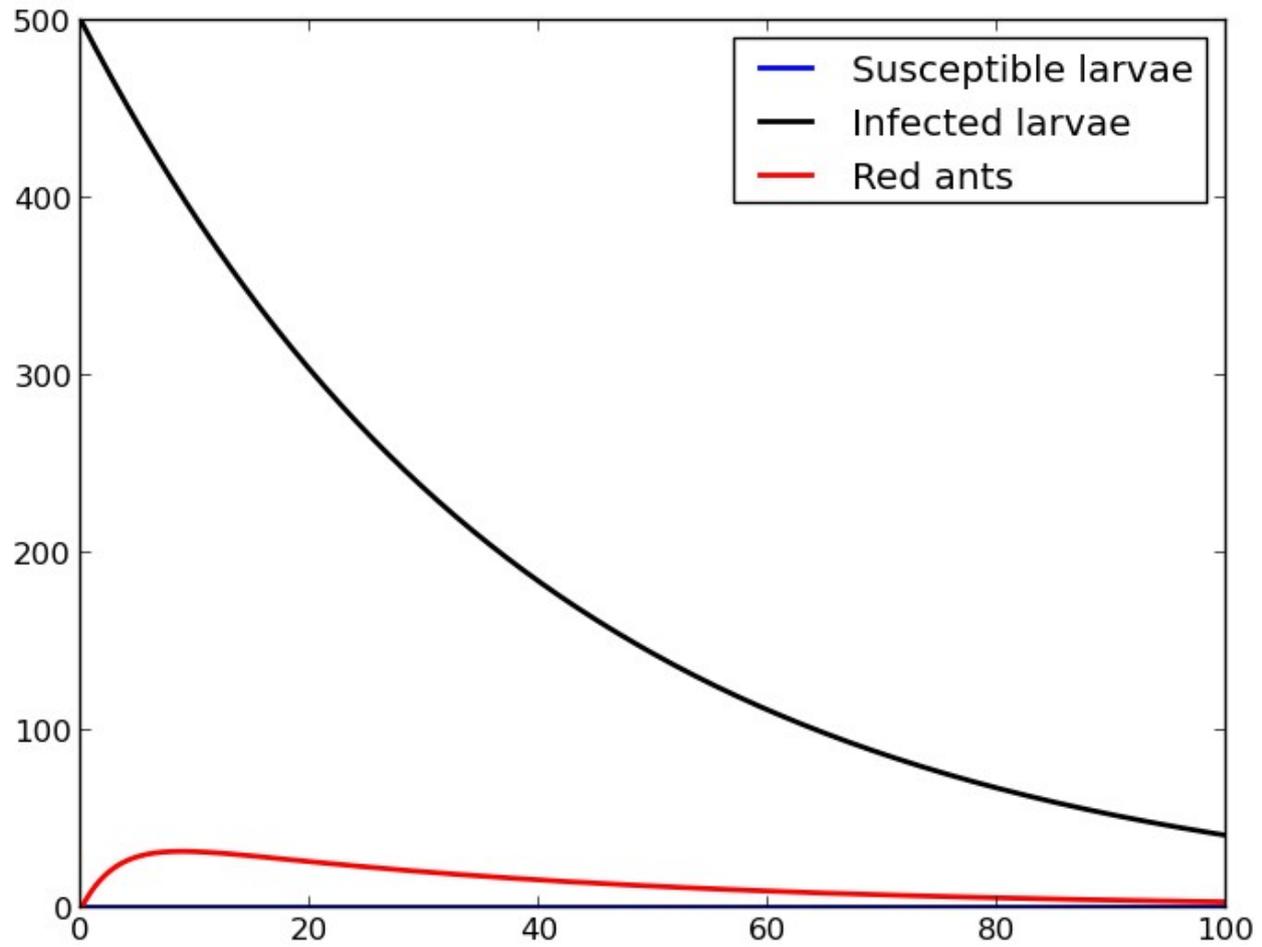
**$L_i = 0$**

**$R = 0$**

**$K = 1000$**



# Control Simulations



**$L_s = 0$**

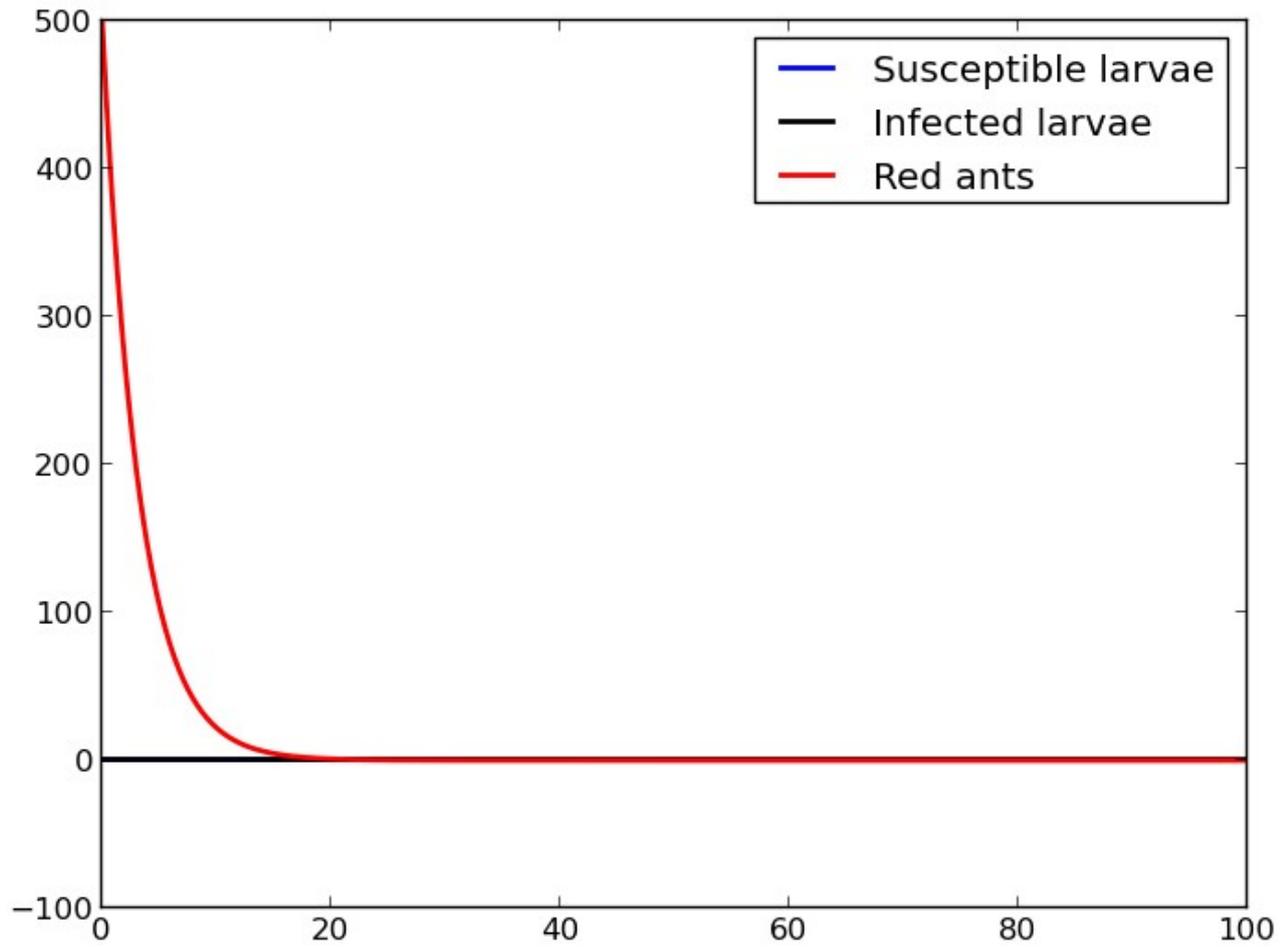
**$L_i = 500$**

**$R = 0$**

**$K = 1000$**



# Control Simulations



**$L_s = 0$**

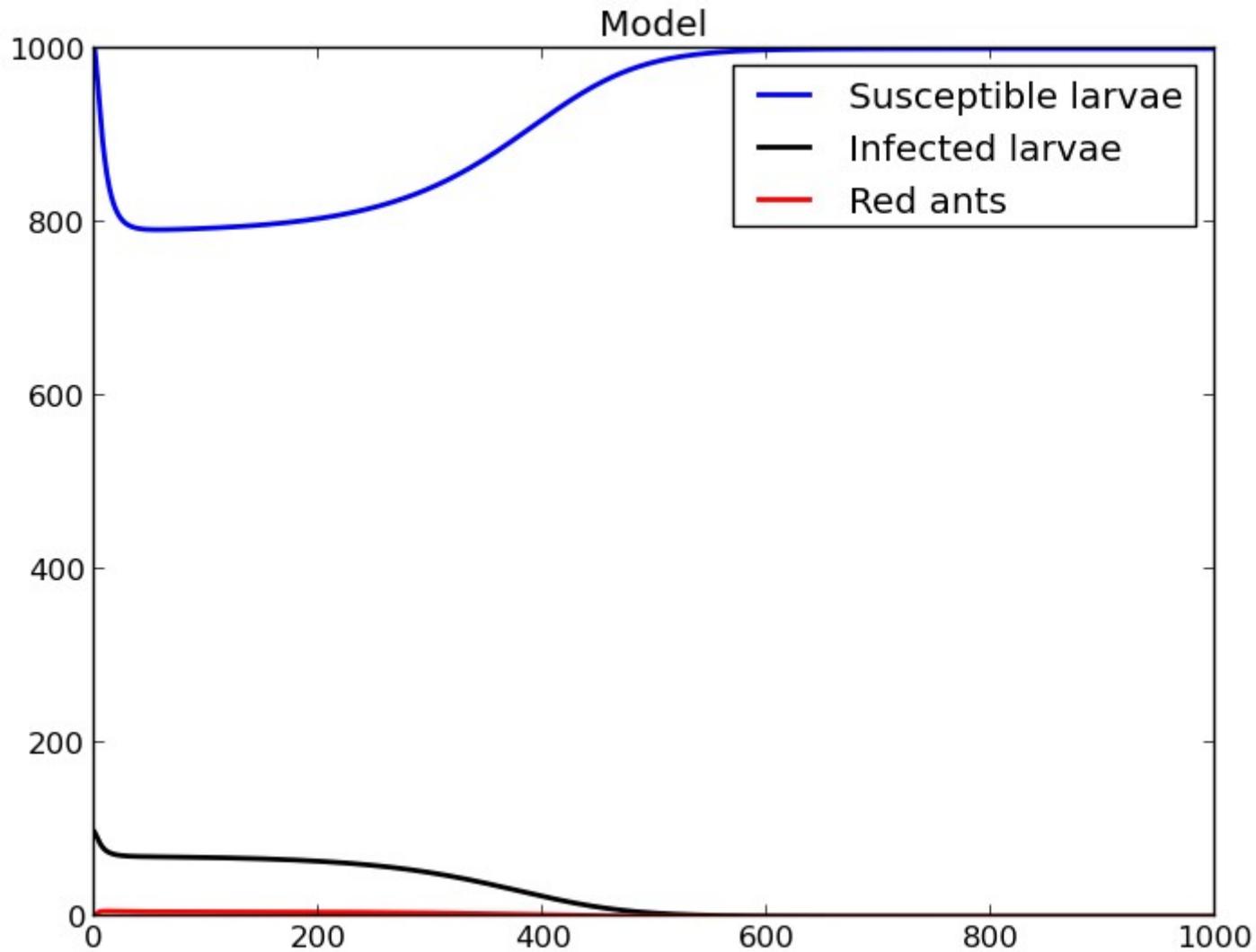
**$L_i = 0$**

**$R = 500$**

**$K = 1000$**



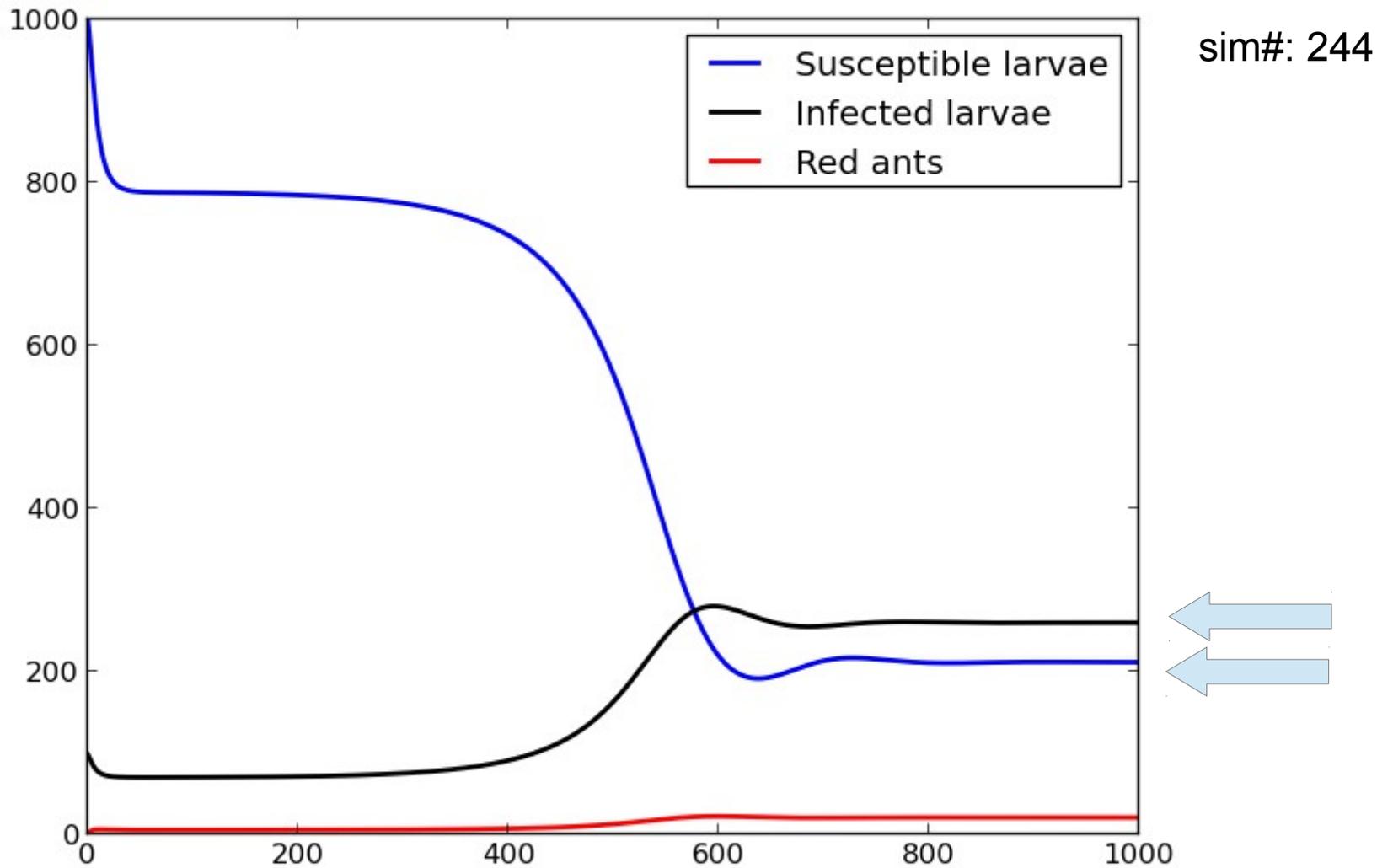
**What initial infection rate can promote the establishment of the parasite in the colony?**



$\alpha = 0.01$   
 $\Pi = 0.28$   
 $\delta = 0.025$

$\mu: 0.025$   
 $K = 1000$   
 $r = 0.11$

$L_s = 1000$   
 $L_i = 97$  ←  
 $R = 0$



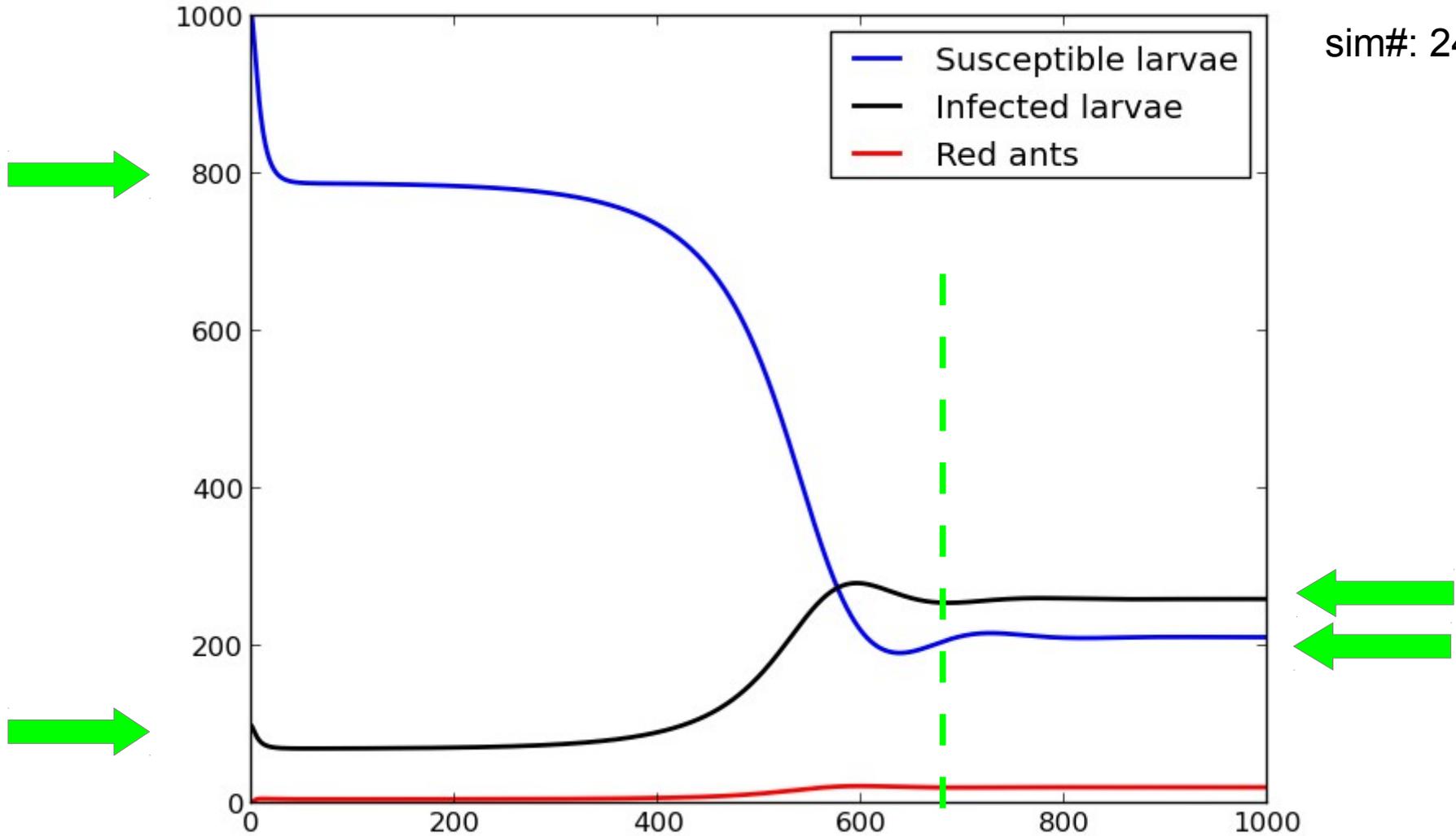
$\alpha = 0.01$   
 $\Pi = 0.28$   
 $\delta = 0.025$

$\mu: 0.025$   
 $K = 1000$   
 $r = 0.11$

$L_s = 1000$   
 $L_i = 98$   
 $R = 0$



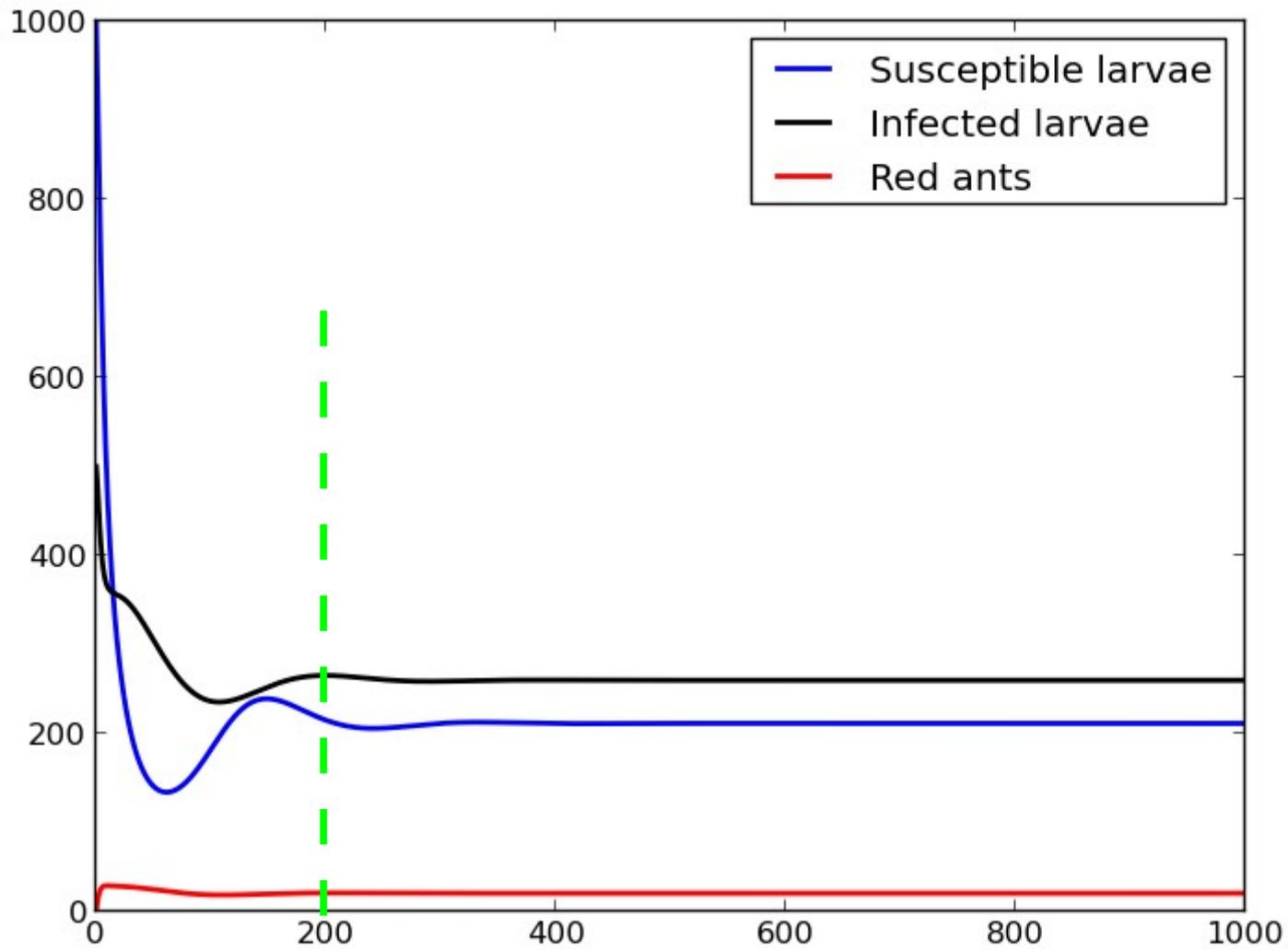
sim#: 244



$\alpha = 0.01$   
 $\Pi = 0.28$   
 $\delta = 0.025$

$\mu = 0.025$   
 $K = 1000$   
 $r = 0.11$

$L_s = 1000$   
 $L_i = 98$   
 $R = 0$

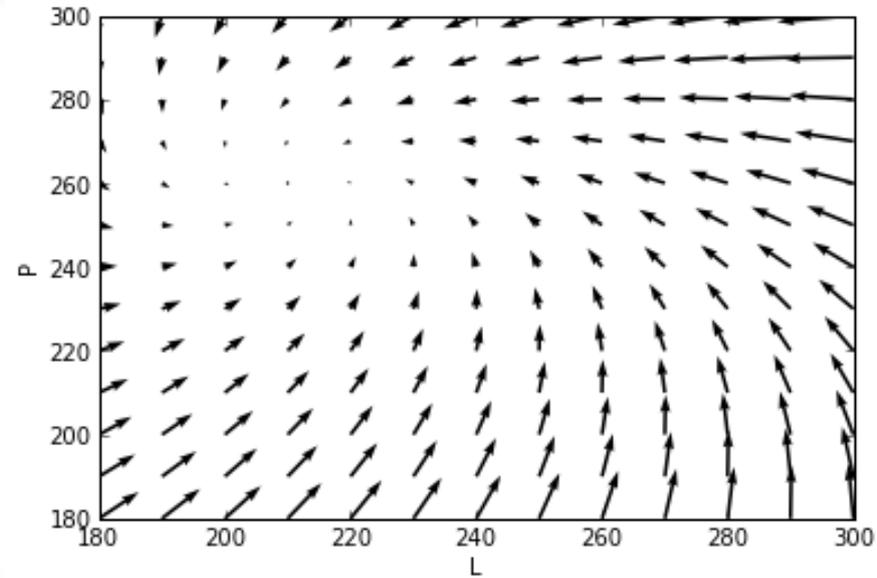
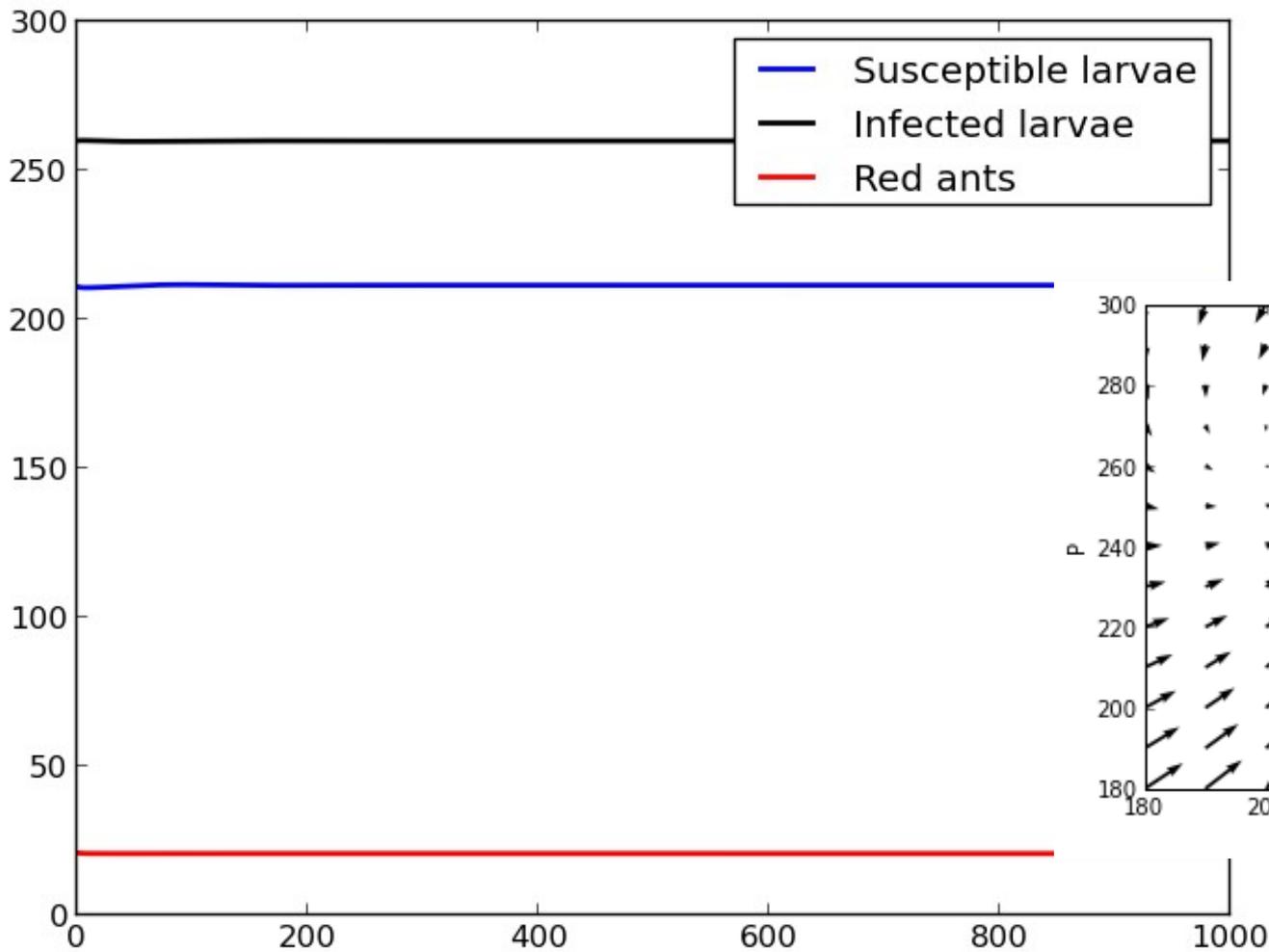


sim#: 256

$\alpha = 0.01$   
 $\Pi = 0.28$   
 $\delta = 0.025$

$\mu: 0.025$   
 $K = 1000$   
 $r = 0.11$

$L_s = 1000$   
 $L_i = 500$  ←  
 $R = 0$

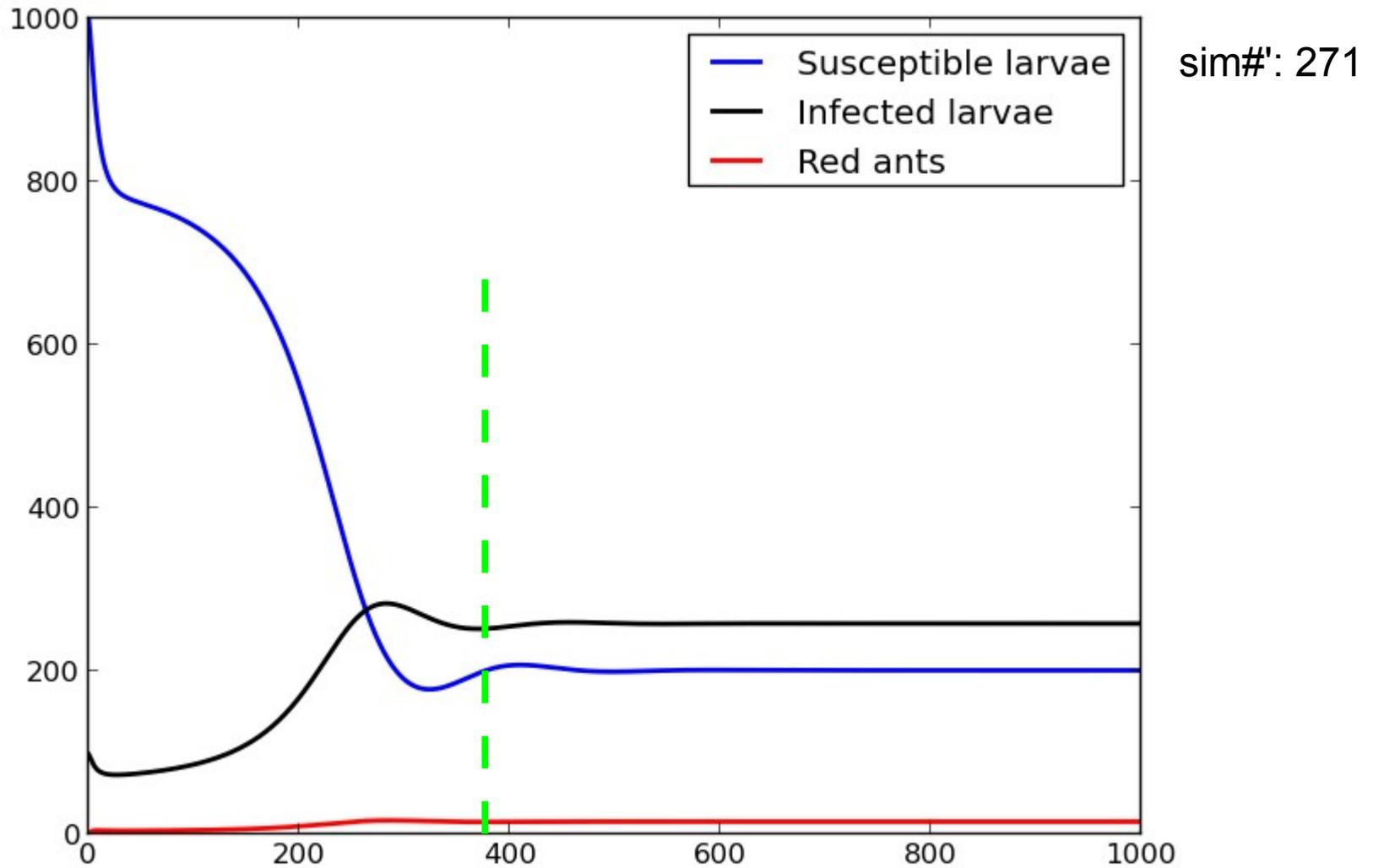


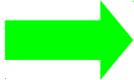
$\alpha = 0.01$   
 $\Pi = 0.28$   
 $\delta = 0.025$

$\mu: 0.025$   
 $K = 1000$   
 $r = 0.11$

$L_s = 211$   
 $L_i = 260$   
 $R = 21$

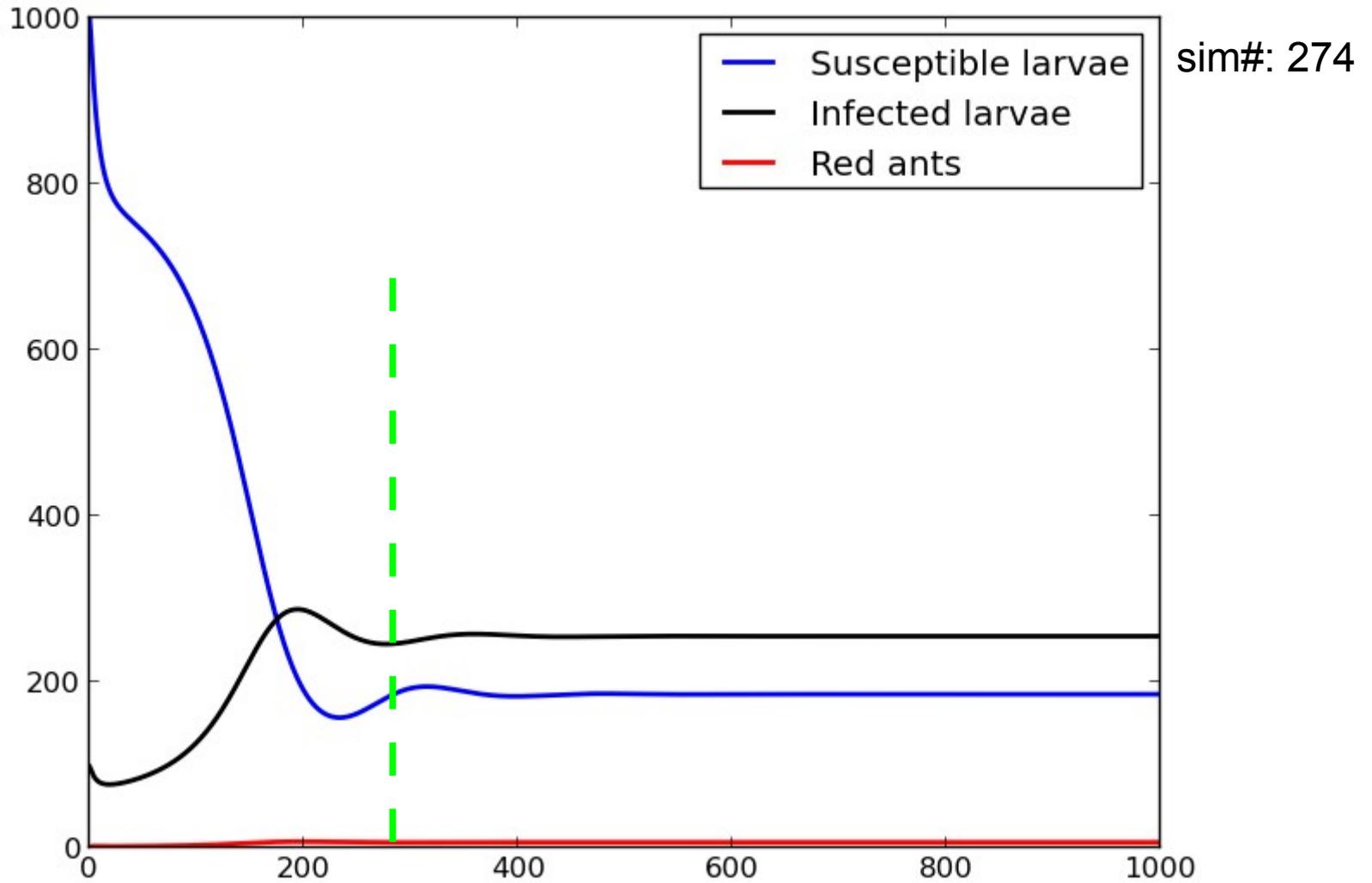





 $\alpha = 0.01$   
 $\Pi = 0.38$   
 $\delta = 0.025$

$\mu: 0.025$   
 $K = 1000$   
 $r = 0.11$

$L_s = 1000$   
 $L_i = 98$    
 $R = 0$

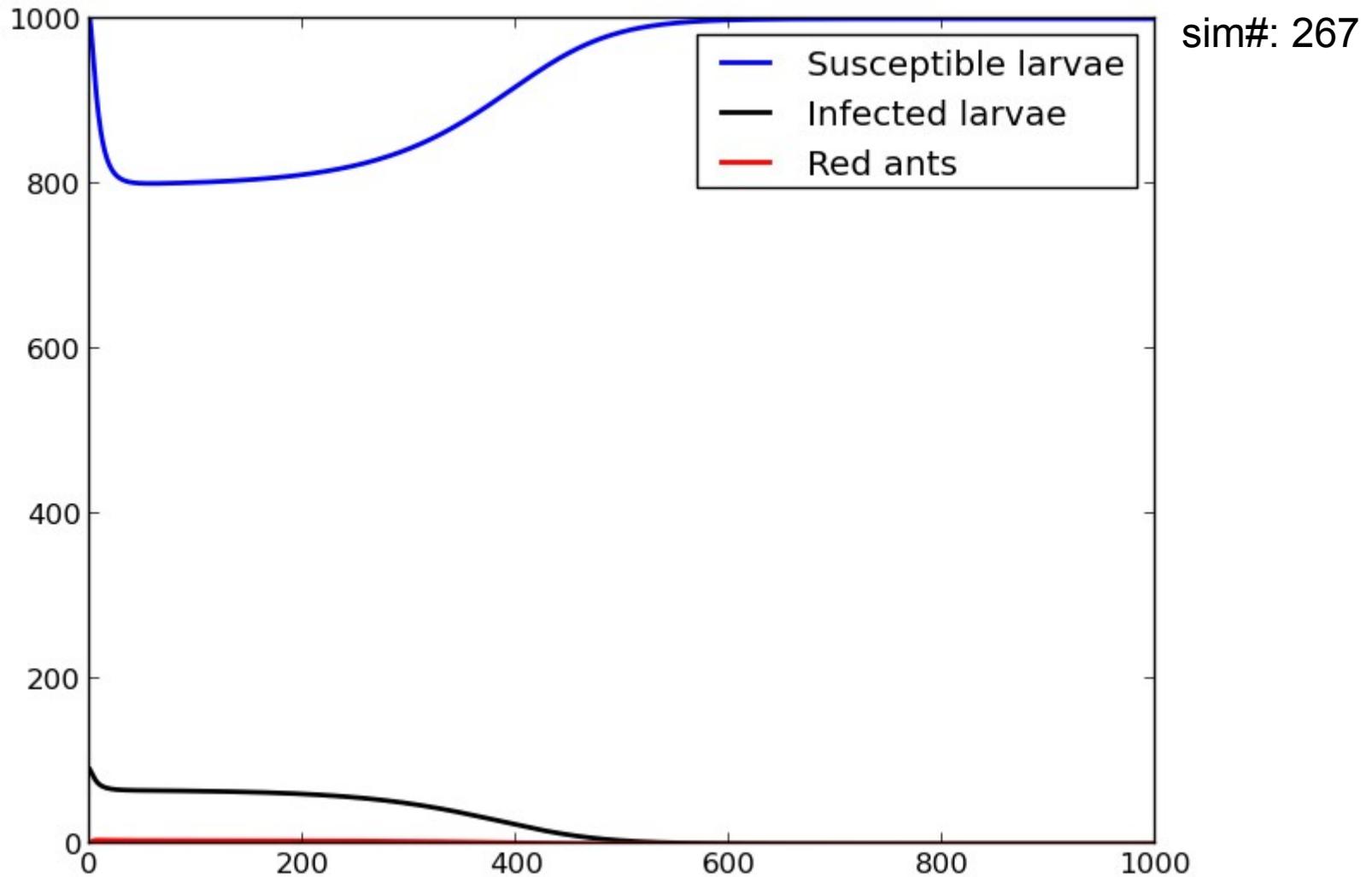


➔  $\alpha = 0.01$   
 $\Pi = 0.9$   
 $\delta = 0.025$

$\mu = 0.025$   
 $K = 1000$   
 $r = 0.11$

$L_s = 1000$   
 $L_i = 98$   
 $R = 0$

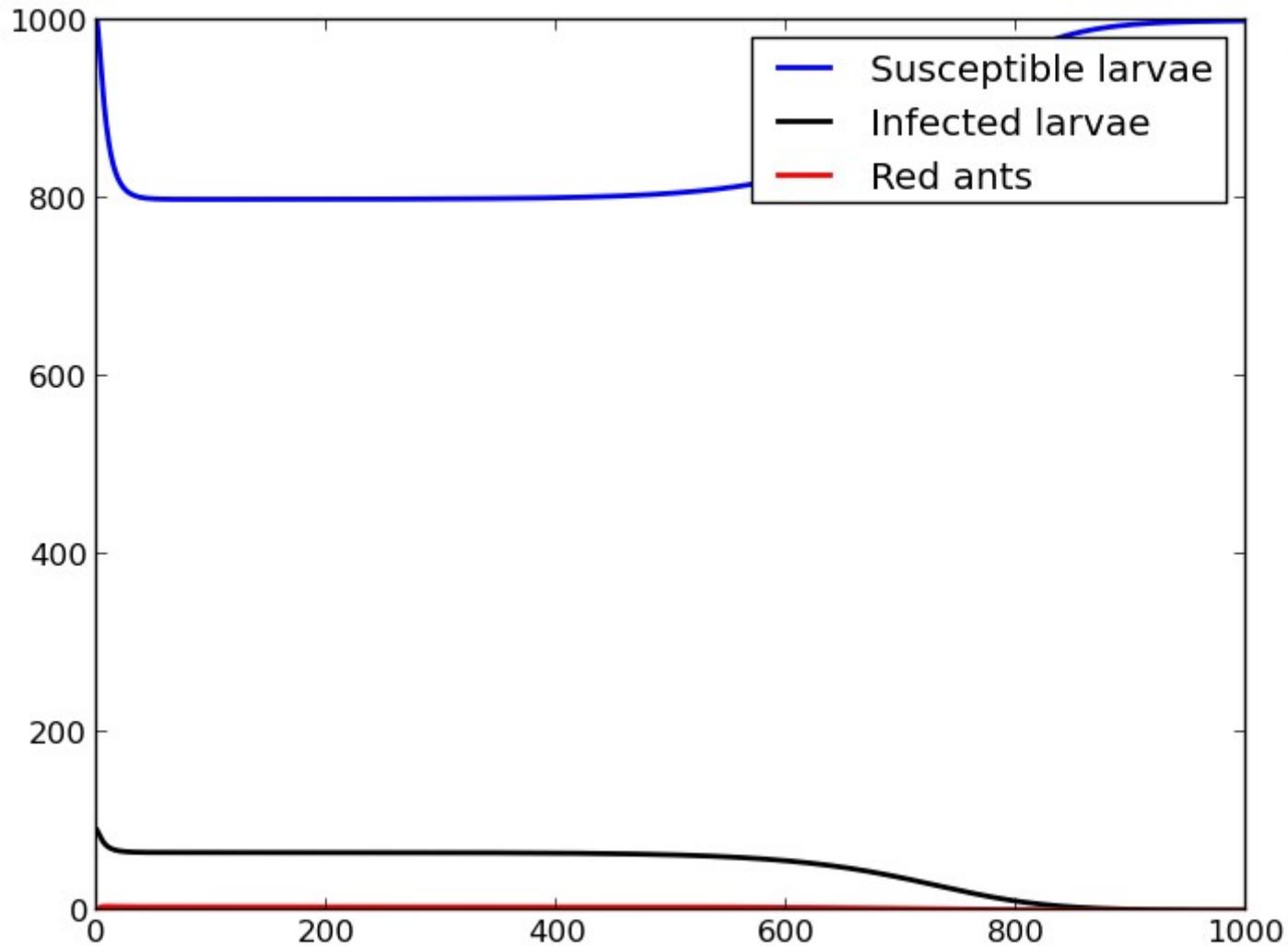
**What predation rate can maintain the parasite in the colony?**



**→**  $\alpha = 0.01$   
 $\Pi = 0.37$   
 $\delta = 0.025$

$\mu = 0.025$   
 $K = 1000$   
 $r = 0.11$

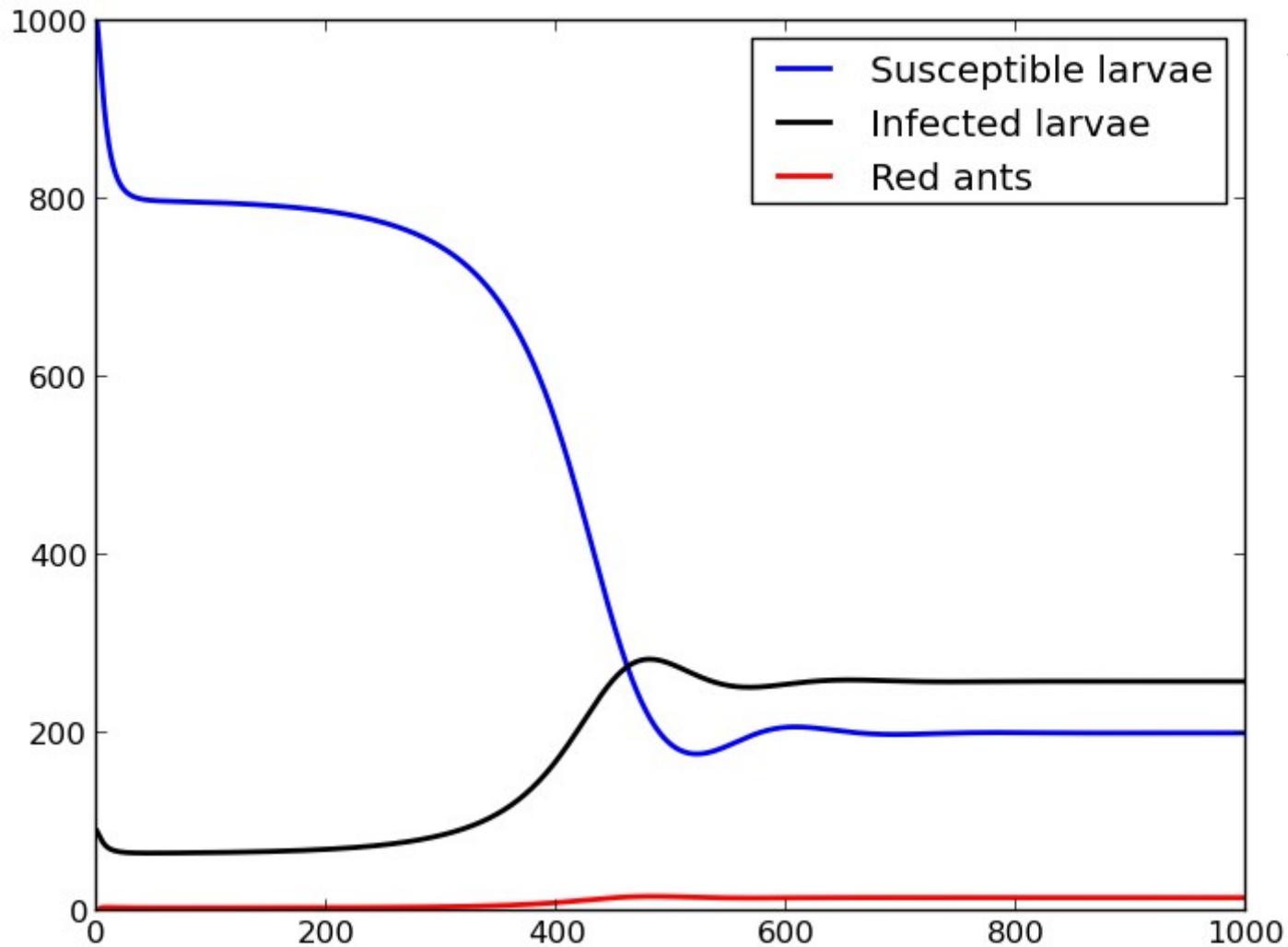
$L_s = 1000$   
 $L_i = 90$  **←**  
 $R = 0$



**→  $\alpha = 0.01$**   
 **$\Pi = 0.38$**   
 **$\delta = 0.025$**

**$\mu: 0.025$**   
 **$K = 1000$**   
 **$r = 0.11$**

**$L_s = 1000$**   
 **$L_i = 90$**   
 **$R = 0$**

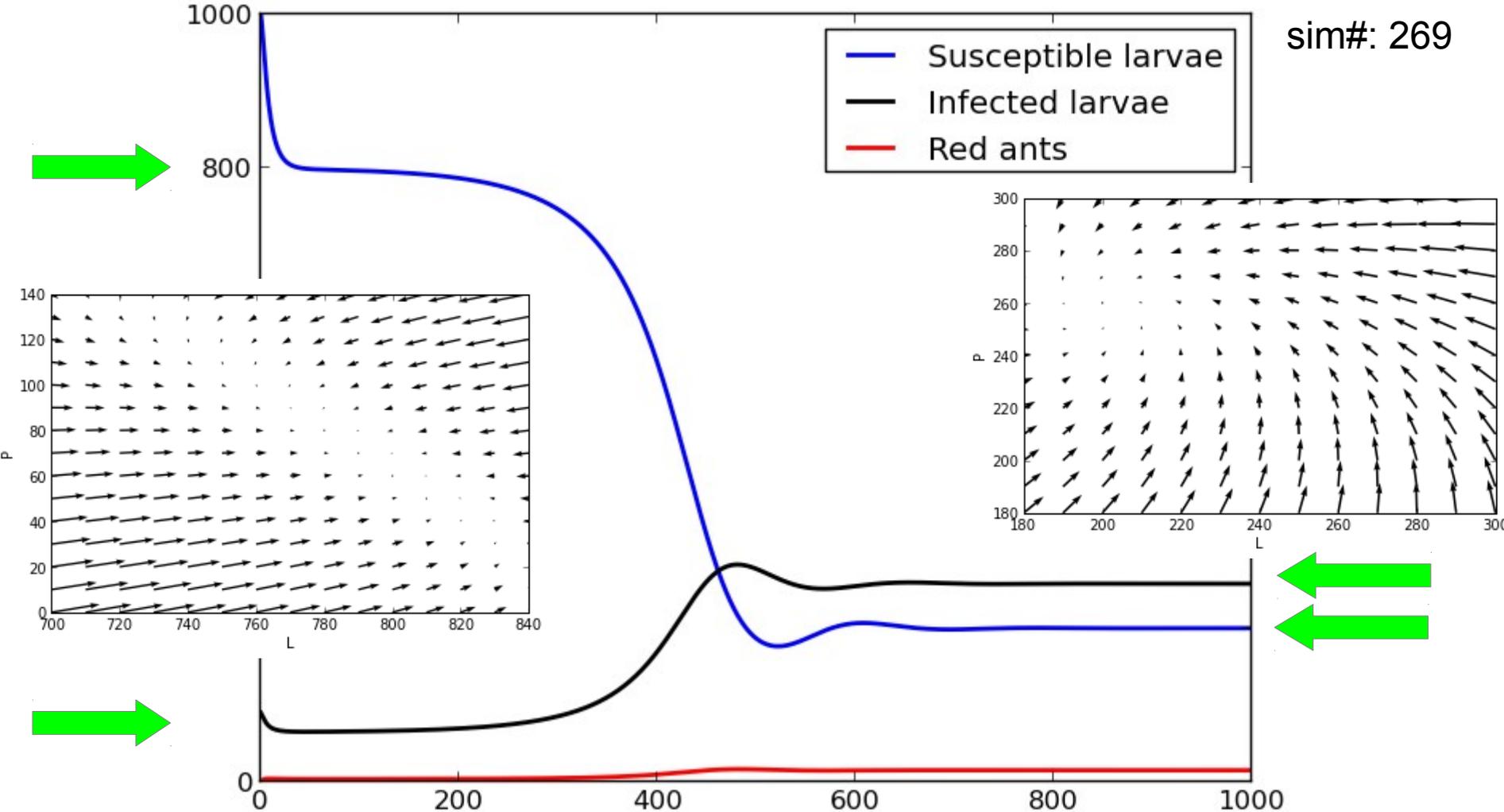
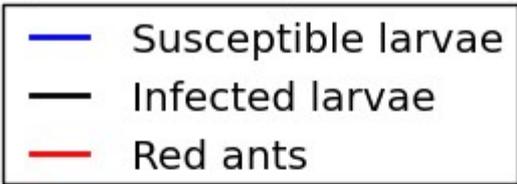


→  $\alpha = 0.01$   
 $\Pi = 0.39$   
 $\delta = 0.025$

$\mu: 0.025$   
 $K = 1000$   
 $r = 0.11$

$L_s = 1000$   
 $L_i = 90$   
 $R = 0$

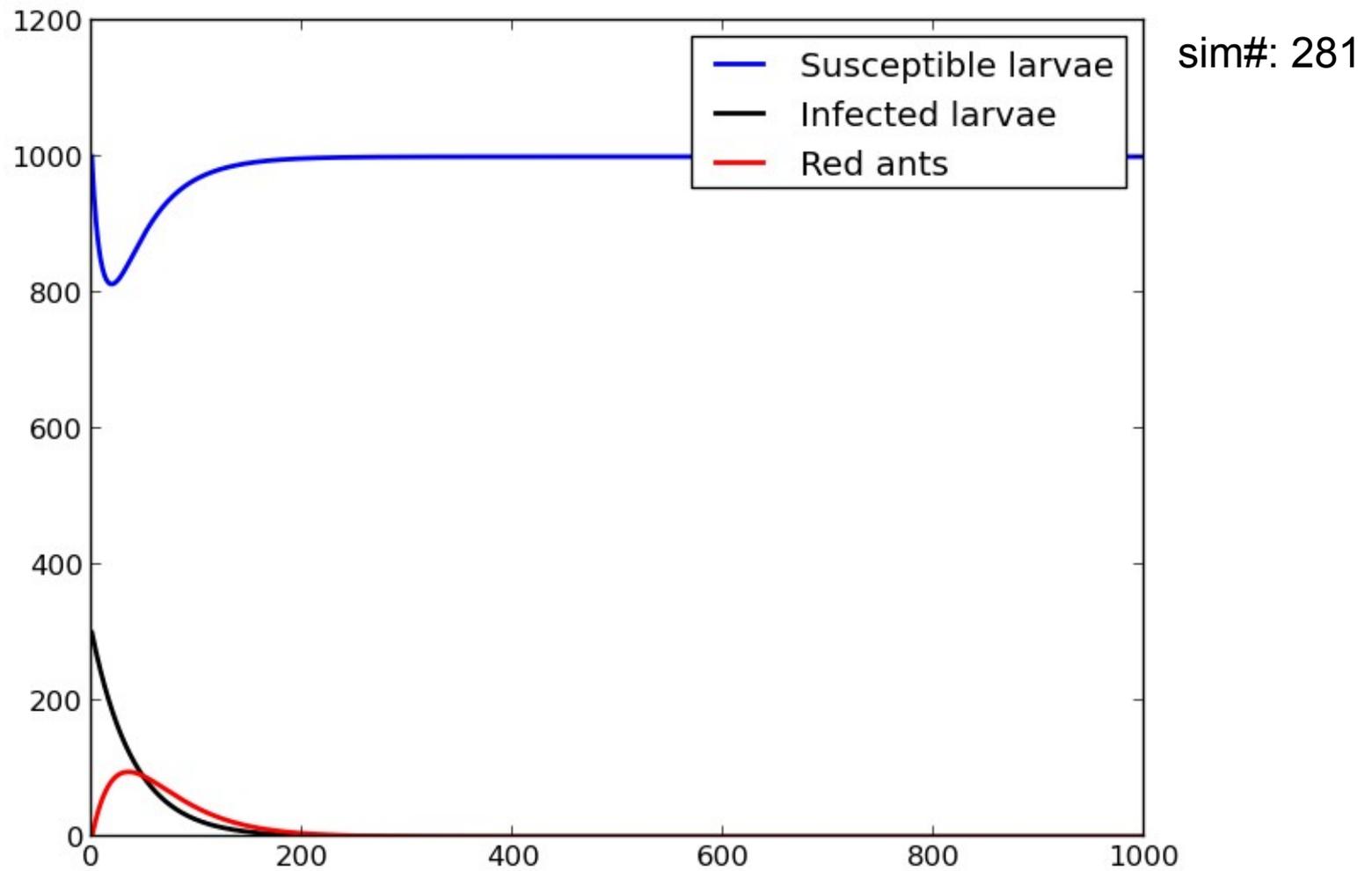
sim#: 269



$\alpha = 0.01$   
 $\Pi = 0.39$   
 $\delta = 0.025$

$\mu: 0.025$   
 $K = 1000$   
 $r = 0.11$

$L_s = 1000$   
 $L_i = 90$   
 $R = 0$

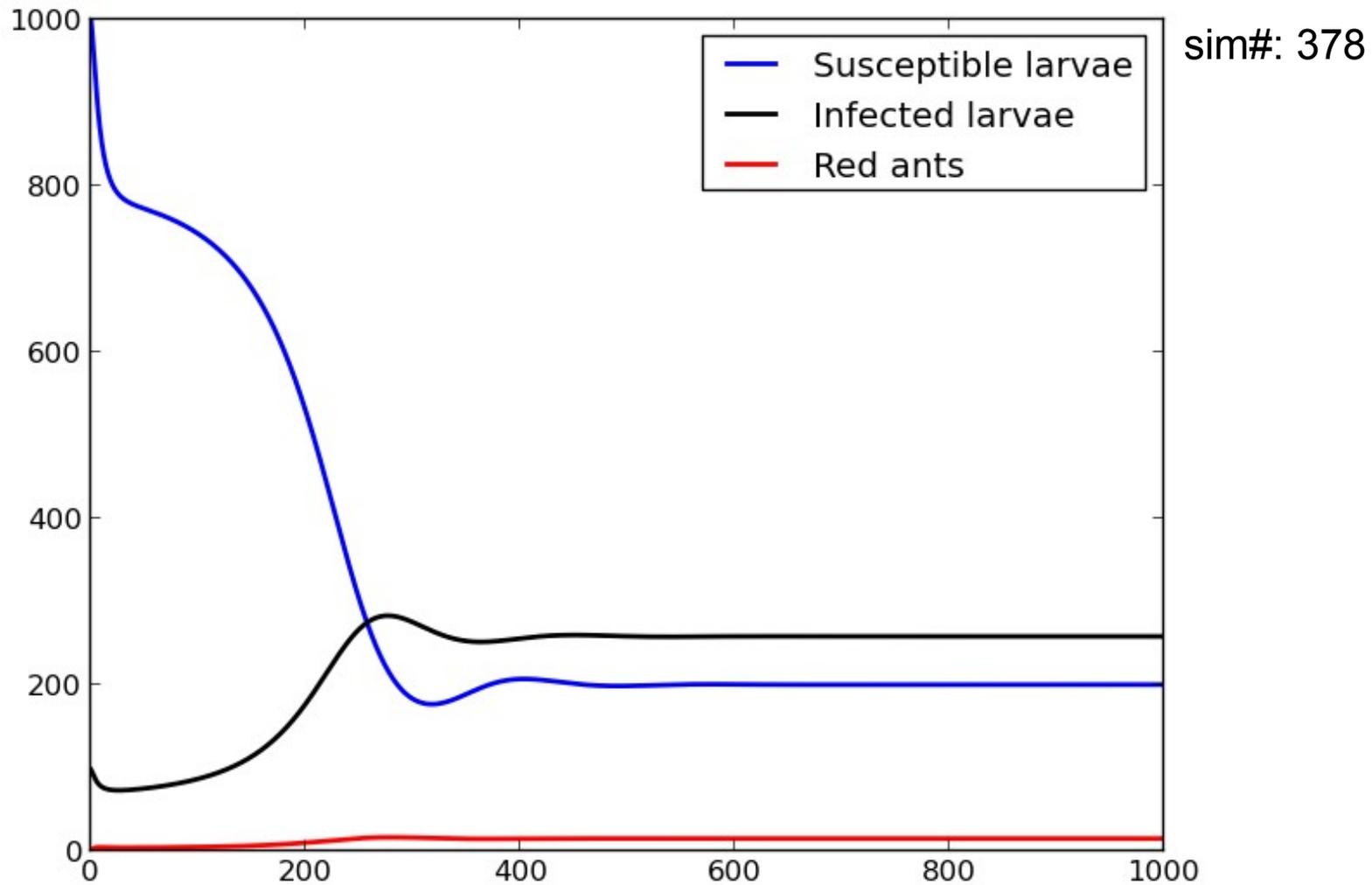


→  $\alpha = 0.01$   
 $\Pi = 0.0$   
 $\delta = 0.025$

$\mu = 0.025$   
 $K = 1000$   
 $r = 0.11$

$L_s = 1000$   
 $L_i = 300$  ←  
 $R = 0$

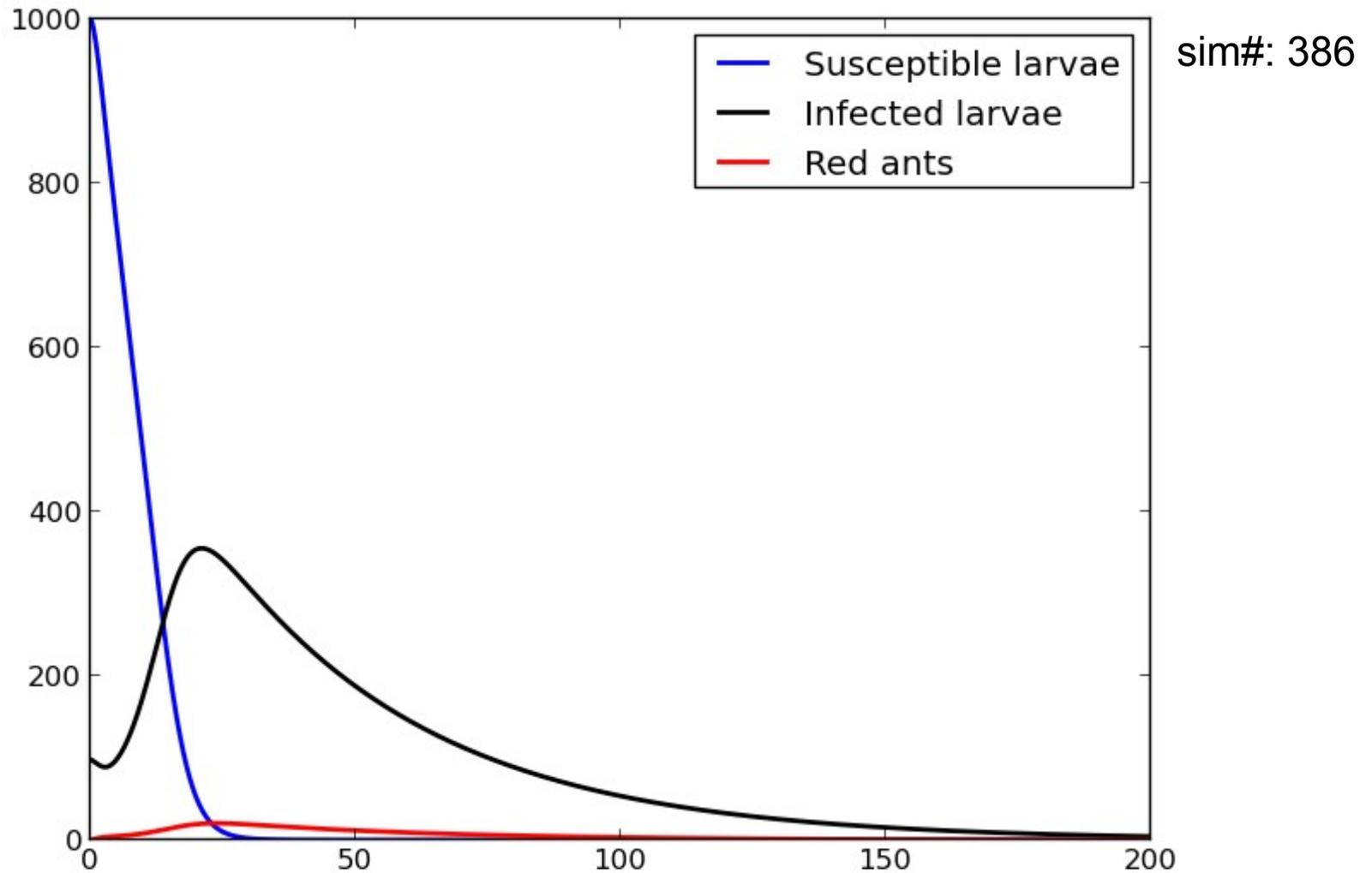
**What infection rate makes the colony collapse?**



$\alpha = 0.01$   
 $\Pi = 0.39$   
 $\delta = 0.025$

$\mu = 0.025$   
 $K = 1000$   
 $r = 0.11$

$L_s = 1000$   
 $L_i = 98$   
 $R = 0$



$\alpha = 0.05$   
 $\Pi = 0.39$   
 $\delta = 0.025$

$\mu: 0.025$   
 $K = 1000$   
 $r = 0.11$

$L_s = 1000$   
 $L_i = 98$   
 $R = 0$

## **CONCLUSIONS**

**Predation of infected ants and infectivity of the parasite seem to play an important role in the stabilization of the population dynamics of host and parasite.**

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**Depending on the population parameters, the initial infection rate is essential for the establishment of the parasite population in the colony (coexistence).**

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Predation of infected ants and infectivity of the parasite seem to play an important role in the stabilization of the population dynamics of host and parasite.

Manipulative parasites can drive host population sizes down to levels considerably below the carrying capacity of the host population, and possibly to extinction.

Depending on the population parameters, the initial infection rate is essential for the establishment of the parasite population in the colony (coexistence).

<u>Collapse</u>	<u>Coexistence</u>	<u>No Infection</u>
$\uparrow \alpha$		$\downarrow \alpha$
$\uparrow \pi$	$> \pi \rightarrow <$ time to <u>equilibrium</u>	$\downarrow \pi$
$\downarrow r$	$< r \rightarrow L_s$ nearer <u><math>L_i</math></u>	$\uparrow r$

# LIMITATIONS

**Resistance.**

**Single colony.**

**Dependence of alpha on R.  $\rightarrow \alpha \leq 1/(\pi \cdot R)$**

**No spatial structure of populations.**

**No basal infection rate.**

# Thank you!

